High-spin mesons below 3 GeV

Cheng-Qun Pang^{1,2},* Bo Wang^{1,2},† Xiang Liu^{1,2}; § and Takayuki Matsuki^{3,4}¶

¹School of Physical Science and Technology, Lanzhou University, Lanzhou 730000, China

²Research Center for Hadron and CSR Physics, Lanzhou University & Institute of Modern Physics of CAS, Lanzhou 730000, China

³Tokyo Kasei University, 1-18-1 Kaga, Itabashi, Tokyo 173-8602, Japan

⁴Theoretical Research Division, Nishina Center, RIKEN, Saitama 351-0198, Japan

In this work, we study the high-spin states with masses below 3 GeV observed in experiments and we perform analysis of mass spectrum and investigation of strong decay behaviors of the high-spin states. Comparing our results with the experimental data, we can reveal the underlying properties of these high-spin states; more importantly, we also predict their abundant decay features, which can provide valuable information for experimental exploration of these high-spin states.

PACS numbers: 14.40.Be, 12.38.Lg, 13.25.Jx

I. INTRODUCTION

With the experimental progress of recent decades, the light-flavor meson family has become increasingly abundant (see the Particle Data Group (PDG) [1]), there is a large amount of high-spin states with spin $J \geq 3$ available among the observed mesons listed in the PDG [1](see Table I for more details). Although 26 high-spin states are collected in PDG, their properties are not presently well established. Therefore it is necessary to determine how to categorize these high-spin states into meson families.

To provide a solution to this problem of studying high-spin states, we need to carry out a systematic and phenomenological investigation and combine it with the present experimental data.

For a $q\bar{q}$ meson system, the orbital quantum number of a meson is at least L=2, corresponding to the D-wave family when the spin quantum number is J=3. Thus, the high-spin states under discussion have close a relationship to D-wave, F-wave, G-wave and H-wave meson families.

In the following, we first focus on how to categorize these high-spin states into the conventional meson family, where the mass spectrum analysis is performed via the Regge trajectory. Furthermore, we calculate the Okubo-Zweig-Iizuka (OZI)-allowed two-body strong decay widths of these highspin states, which can further test their possible meson assignments in combination with the present experimental data. We accordingly predict their abundant decay behaviors, which is important information for experimental exploration of highspin mesons in future.

This paper is organized as follows. After a brief review, we present in Sec. II the experimental and theoretical research status. In Sec. III, we adopt the Regge trajectory and the quark pair creation (QPC) model to study the high-spin states observed. The paper ends with conclusion and discussions in

Sec. IV.

II. CONCISE REVIEW OF THE PRESENT RESEARCH STATUS

Before illustrating our calculation, we first give a brief review of the research status of the high-spin states observed, which we hope is convenient for the readers.

A. States with J=3

An obvious peak signal was observed in the reaction $p\bar{p} \rightarrow$ $\eta \pi^0 \pi^0$, $\pi^0 \pi^0$, $\pi^+ \pi^-$, $\eta \eta$, and $\eta \eta'$ [8] which is named as $f_3(2050)$. Another f_3 state $f_3(2300)$ was introduced by performing the partial wave analysis (PWA) of the data of $p\bar{p} \to \Lambda\bar{\Lambda}$ [6]. In Refs. [8, 30], $f_3(2050)$ was suggested to be a ground state of the F-wave meson family, with $f_3(2300)$ as its first radial excitation. In Ref. [31], different from Ref. [8], $f_3(2050)$ and $f_3(2300)$ were proposed as the first and the second radial excitations of the f_3 meson family, and an unobserved ground f₃ state with mass around 1.7 GeV was predicted. Reference. [30] obtained the same assignment as Ref. [8] by using the similar method to Ref. [31]. Ebert et al. obtained the mass spectrum of some high-spin states via the relativistic quark model based on the quasipotential approach [32], where the mass spectrum calculation shows that $f_3(2300)$ can be a ground state in the f_3 meson family, which has dominant $s\bar{s}$ component.

There are three observed a_3 states. In the process $\pi^-p \to \pi^+\pi^-\pi^-p$, the E852 experiment reported a resonance $a_3(1875)$, and some ratios were measured. Two other states, $a_3(2030)$ and $a_3(2275)$, were observed in the $p\bar{p}$ annihilation by SPEC [25, 33]. In Ref. [31], the authors suggested that $a_3(1875)$ and $a_3(2030)$ might be the same state, which could be a ground state, with $a_3(2275)$ is the first radial excitation in the a_3 family. Additionally, the mass of the $n^{2s+1}L^J=1^3F_3$ state calculated by the relativistic quark model is 1910 MeV which corresponds to $a_3(1875)$ [32].

The SPEC experiment [5, 10, 11] observed $h_3(2025)$, $h_3(2275)$, $h_3(2030)$, and $h_3(2245)$ by analyzing the new Crystal Barrel data in the $p\bar{p}$ annihilation. These papers suggested

[‡]Corresponding author.

^{*}Electronic address: pangchq13@lzu.edu.cn †Electronic address: wangb13@lzu.edu.cn §Electronic address: xiangliu@lzu.edu.cn ¶Electronic address: matsuki@tokyo - kasei.ac.jp

TABLE I: The observed high-spin states collected in the PDG [1]. Here, the states listed as further states in the PDG are marked by the superscript f. The C parity is valid only for the corresponding neutral states where the J^{PC} quantum numbers of these high-spin states appear with isospin I = 1. We need to emphasize that $\rho_3(1690)$, $\rho_3(1990)$, and $\rho_3(2250)$ are not listed here since these three states have been studied in our former work [2]. In the fifth column, we list some branching ratios and decay modes observed experimentally . In this work we adopt the abbreviations, ω , ρ , η' , a_0 , b_1 , f_2 , and a_2 for $\omega(782)$, $\rho(770)$, $\eta'(958)$, $a_0(980)$, $b_1(1260)$, $f_2(1270)$, and $a_2(1320)$, respectively.

$I(J^{PC})$	State	Mass (MeV)	Width (MeV)	Other information
0(3)	$\omega_3(1670)$	1667 ± 4	168 ± 10	$\Gamma_{\omega\pi\pi}/\Gamma_{\rho\pi} = 0.71 \pm 0.27$ [3], πb_1 [4]
0(3)	$\omega_3(1945)^{\dagger}$	1945 ± 20	115 ± 22	$\eta\omega$ [5]
0(3)	$\omega_3(2255)^{\dagger}$	2255 ± 15	170 ± 30	$\eta\omega$ [5, 6]
0(3)	$\omega_3(2285)^{f}$	2278 ± 28	224 ± 50	$\eta\omega$ [5, 6]
0(3)	$\phi_3(1850)$	1854 ± 7	87^{+28}_{-23}	$\Gamma_{KK^*}/\Gamma_{KK} = 0.55^{+0.85}_{-0.45}$ [7]
0(3++)	$f_3(2050)^{\dagger}$	2048 ± 8	213 ± 34	$[\eta f_2]_{L=1,3}, \pi a_2$ [8]
0(3 ⁺⁺)	$f_3(2300)^{\dagger}$	2334 ± 2	200 ± 20	$[\eta f_2]_{L=1,3}, \eta \prime f_2$ [6]
1(3++)	$a_3(1875)^{\dagger}$	$1874 \pm 43 \pm 96$	$384 \pm 121 \pm 114$	$\Gamma_{f_2\pi}/\Gamma_{\rho\pi} = 0.8 \pm 0.2, \Gamma_{\rho_3(1690)\pi}/\Gamma_{\rho\pi} = 0.9 \pm 0.3$ [9]
1(3++)	$a_3(2030)^{\dagger}$	2031 ± 12	150 ± 18	$\eta a_2,\pi f_2$ [10]
1(3++)	$a_3(2275)^{\dagger}$	2275 ± 35	350^{+100}_{-50}	$a_0\eta,\eta f_2$ [10]
0(3+-)	$h_3(2025)^{\dagger}$	2025 ± 20	145 ± 30	$\eta\omega$ [5]
0(3+-)	$h_3(2275)^{\dagger}$	2275 ± 25	190 ± 45	$\eta\omega$ [5]
1(3+-)	$b_3(2030)^{\dagger}$	2032 ± 12	117 ± 11	$\omega\pi^0$, $\pi^+\pi^-$ [11]
1(3+-)	$b_3(2245)^{\dagger}$	2245 ± 50	320 ± 70	$\omega a_2, \ \omega \pi, \ b_1 \eta, \ \pi \omega (1650) \ [10]$
0(4++)	$f_4(2050)$	2018 ± 11	237 ± 18	$\Gamma_{\omega\omega}/\Gamma_{\pi\pi} = 1.5 \pm 0.3$ [12], $\Gamma_{\pi\pi}/\Gamma_{Total} = 0.170 \pm 0.015$ [1]
				$\Gamma_{\eta\eta}/\Gamma_{\text{Total}} = (2.1 \pm 0.8) \times 10^{-3} \text{ [13]}, \Gamma_{KK}/\Gamma_{\pi\pi} = 0.04^{+0.02}_{-0.01} \text{ [14]}$
0(4++)	$f_4(2300)$	2320 ± 60	250 ± 80	$\Gamma_{\rho\rho}/\Gamma_{\omega\omega} = 2.8 \pm 0.5 \ [15], K^+K^- \ [16], \pi\pi \ [17, 18], \eta\eta \ [19], \eta f_2 \ [10]$
1(4++)	a ₄ (2040)	1996^{+10}_{-9}	255^{+28}_{-24}	$\Gamma_{\pi\rho}/\Gamma_{\pi f_2} = 1.1 \pm 0.2 \pm 0.2 \ [9], \ KK \ [20, 21], \rho\omega \ [22], \eta\pi^0 \ [23-25], \eta'\pi \ [25, 26]$
1(4++)	$a_4(2255)^{\dagger}$	2237 ± 5	291 ± 12	$\pi\eta,\pi\eta',\pi f_2$ [10]
$0(4^{-+})$	$\eta_4(2330)^{\dagger}$	2328 ± 38	240 ± 90	$a_0\pi$ [8], πa_2 [8], ηf_2 [10]
1(4 ⁻⁺)	$\pi_4(2250)^{\dagger}$	2250 ± 15	215 ± 25	$a_0\eta$ [10]
0(4)	$\omega_4(2250)^{\dagger}$	2250 ± 30	150 ± 50	$\eta\omega$ [5]
1(4)	$\rho_4(2230)^{\dagger}$	2230 ± 25	210 ± 30	$\omega\pi^0,~\pi^+\pi^-$ [11]
0(5)	$\omega_5(2250)^{\dagger}$	2250 ± 70	320 ± 95	$\eta\omega,\pi b_1[10]$
1(5)	$\rho_5(2350)$	2330 ± 35	260 ± 70	$\omega \pi^0$ [11], $\pi \pi$ [11, 17, 18], $K^+ K^-$ [27, 28]
0(6++)	$f_6(2510)$	2469 ± 29	283 ± 40	$\Gamma_{\pi\pi}/\Gamma_{\text{Total}} = 0.06 \pm 0.01[29]$
1(6++)	$a_6(2450)$	2450 ± 130	400 ± 250	KK [20]

that $h_3(2275)$ and $b_3(2245)$ are the first radial excitations of $h_3(2025)$ and $b_3(2030)$, which are the ground states in the h_3 and b_3 meson families, respectively. In Refs. [30, 31], it is suggested that that we regard $h_3(2025)/b_3(2030)$ and $h_3(2275)/b_3(2245)$ as the first and second radial excitations in the h_3/b_3 meson families, where the corresponding ground states were predicted. The $b_1(1640)$ state was predicted in Refs. [34, 35]. The study in Ref. [32] indicates that $h_3(2275)$ and $b_3(2245)$ could be the ground states with a component $s\bar{s}$.

The $\omega_3(1670)$ state was first found in the $\pi^+ n \to p3\pi^0$ process [36] and has been studied by other experiments (the details for the experimental information on $\omega_3(1670)$ are listed

in the PDG [1]). $\omega_3(1670)$ can decay into $\rho\pi$ and $\pi\omega\pi$. The first radial excitation of ω_3 is $\omega_3(1945)$, which was reported by SPEC [5]. At the same time, Ref.[5] also found $\omega_3(2255)$ and $\omega_3(2285)$, which were later confirmed by RVUE [6] and $\omega_3(1670)$ was suggested to be the ground state of the ω_3 family. Combining the PWA with the n- M^2 plot, the authors of Ref. [5] proposed that $\omega_3(1945)$ and $\omega_3(2285)$ are 2^3D_3 and 3^3D_3 states, respectively [5], while $\omega_3(2285)$ is a 3G_3 state. Reference [30] suggested $\omega_3(2285)$ could be the 1^3G_3 states, respectively.

HBC found $\phi_3(1850)$ in the KK and KK^* channels from the K^-p collision [37], and it was confirmed by OMEGA [38] and LASS [7]. Both the J- M^2 plot analysis in Refs. [31, 34, 35] and the calculation of the mass spectrum in [32] show that $\phi_3(1850)$ is a good candidate for the 1^3D_3 state.

B. States with J=4

The Serpukhov-CERN Collaboration [39] and CERN-Munich Collaboration [40] observed a peak structure in the processes $\pi^-p \to n2\pi^0$ and $\pi^-p \to nK^+K^-$, which was named $f_4(2050)$. Other experiments relevant to the observation of $f_4(2050)$ can be found in PDG [1]. Some observed channels and branching ratios are listed in Table I. CNTR [41] first reported the resonance $f_4(2300)$; in the past decades, it has appeared in the reactions, $p\bar{p} \to K^+K^-$ [42], $\pi\pi$ [17, 18, 43], $\eta\pi^0\pi^0$ [8], and $\pi^-p \to K^+K^-$ [19].

There are some theoretical studies on the properties of the observed f_4 states. The $f_4(2050)$ is treated as a molecule state composed of three ρ mesons [44]. Ebert et~al. obtained a 1^3F_4 $q\bar{q}$ state with mass M=2018 MeV and a 2^3F_4 $q\bar{q}$ state with mass M=2284 MeV which correspond to $f_4(2050)$ and $f_4(2300)$, respectively [32]. Many studies support this assignment [30, 34, 35, 45]. Additionally, in Ref. [31], the Regge trajectory analysis shows that $f_4(2050)$ and $f_4(2300)$ are the ground states dominated by the $q\bar{q}$ and $s\bar{s}$ components, respectively.

There are many experiments relevant to $a_4(2040)$. OMEGA observed a resonance with mass around 2030 MeV by the PWA of $\pi^-p \to n3\pi$ [46]. Later, $a_4(2040)$ was also found in the reactions, $\pi p \to K_s K^{\pm} p$ [20], $\pi^- p \to \eta \pi^0 n$ [24], $\pi^- A \to \omega \pi^- \pi^0 A^*$ [47], $\pi^- p \to \eta' \pi^- p$ [26], $\pi^- p \to \omega \pi^- \pi^0 p$ [22], and $\pi^- P_b \to \omega \pi^- \pi^- \pi^+ P_b'$ [22]. The observed decay modes are listed in Table I.SPEC also reported $a_4(2255)$ in $p\bar{p} \to \pi^0 \eta$, $3\pi^0$, $\pi^0 \eta'$ [25] and E835 confirmed the state $a_4(2255)$ in the reaction $p\bar{p} \to \eta \eta \pi^0$ [23]. All Regge trajectory studies show that $a_4(2040)$ is the ground state of the a_4 family, and $a_4(2255)$ is its first radial excitation [30, 31, 34, 35, 45]. Ebert et al. obtained a $1^3 H_4$ state with mass M=2234 MeV which is very close to $a_4(2255)$ [32]. However, in Ref. [25], the PWA shows that $a_4(2255)$ is a 3F_4 state.

In the reactions $p\bar{p}\to\eta\pi^0\pi^0,\pi^0,\pi^0\pi^0,\pi^+\pi^-,\eta\eta,\eta\eta\nu$, SPEC reported a 1G_4 state with the mass 2328 ± 38 MeV and width 240 ± 90 MeV in the final states $(\pi a_2)_{L=4}$ and $(\pi a_0)_{L=4}$, where L=4 denotes G wave [8], which was named $\eta_4(2330)$. They also reported the resonance $\pi_4(2250)$ in the $p\bar{p}$ annihilation through studying the Crystal Barrel data [25]. The Regge trajectory analysis shows that both $\pi_4(2250)$ and $\eta_4(2330)$ are the ground states in the π_4 and η_4 families [30, 31, 34, 35] with different isospins I=1 and 0, respectively. The study of mass spectrum of high-spin states in Ref. [32] indicates that $\pi_4(2250)$ and $\eta_4(2330)$ are the first radial excitations of G-wave mesons, where a mass of 2092 MeV for the corresponding ground states was predicted.

 $\omega_4(2250)$ [5] and $\rho_4(2230)$ [11] were reported by SPEC. Both the mass spectrum calculation in Ref. [32] and the $J-M^2$ plot in Ref. [30, 31] support that $\omega_4(2250)$ and $\rho_4(2230)$ are

the 1^3G_4 states with different isospins, as above.

C. States with J = 5

Analyzing the $\eta\omega$ and $\omega\pi^0\pi^0$ data, SPEC strongly required a 3G_5 state around 2250 MeV [5], which corresponds to $\omega_5(2250)$. The mass error of $\omega_5(2250)$ was later given in Ref. [10].

An isospin I=1 and J=5 structure $\rho_5(2350)$ was observed in the $p\bar{p}$ total cross section [27], which can decay into $\omega\pi^0, \pi^+\pi^-, \pi^0\pi^0$, and K^+K^- [11, 17, 18, 28, 42, 48, 49].

The present theoretical studies support $\omega_5(2250)$ as a ground state [31, 32]. $\rho_5(2350)$ is also a ground state, which was suggested in Refs. [30–32, 34, 35, 45]. The authors of Ref. [44], however, treated $\rho_5(2350)$ as a molecule of four ρ mesons.

D. States with J = 6

GAM2 observed a J=6 neutral meson R(2510) [29]; it is now named $f_6(2510)$ due to the contribution by Ref. [50], where the branching ratio of its $\pi\pi$ mode was given. The $f_6(2510)$ was confirmed in the reaction $\pi^-p \to 2\pi^0n$ [51] and SPEC also found it in the $p\bar{p}$ annihilation [8].

There is only one experiment about $a_6(2450)$, which was observed by SPEC in the reaction $\pi p \to K_s^0 K^{\pm} p$ [52].

From the mass spectrum analysis in Refs. [32, 34, 35], the $f_6(2510)$ is a good candidate of the 1^3H_6 $q\bar{q}$ state. The $a_6(2450)$ is the isospin partner of $f_6(2510)$ [31, 32, 34, 35, 45]. A different explanation for $f_6(2510)$, i.e., a molecular state of five ρ mesons, was proposed in Ref. [44].

From the above review, we can find that the present status of the high-spin states is still in disorder, where different groups gave different theoretical explanations. This situation inspires us to carry out a systematic study of these high-spin states, in order to improve our understanding of the properties of these states.

III. PHENOMENOLOGICAL ANALYSIS

The phenomenological analysis presented in this work includes two methodologies. First, the analysis of Regge trajectories is adopted to study possible meson assignments to the high-spin states under discussion. Second, we use the QPC model to obtain their OZI-allowed two-body decay behaviors. In the following, we give a brief introduction to these methods.

The analysis of Regge trajectory provides a general method to study the meson spectrum [45]. The excited states and ground states satisfy a simple relation

$$M^2 = M_0^2 + \mu^2(n-1),\tag{1}$$

where M_0 and M are the masses of ground state and excited state, respectively. The μ^2 gives a slope of a trajectory with

the value $\mu^2 = 1.25 \pm 0.15 \text{ GeV}^2$ suggested in Ref. [45]. Via the above equation, we obtain the $n\text{-}M^2$ plot of the mesons under discussion, where the radial quantum number n of these states can be obtained when mass is given, this is important information regarding the underlying structure of mesons.

In addition to the relation in Eq. (1), there exists a similar relation

$$M_I^2 = M_{I'}^2 + \alpha^2 (J - J'), \tag{2}$$

where J or J' denotes the spin of a meson. $M_{J'}$ and M_J are the masses of mesons with different spins and with the same P and C quantum numbers. Via Eq. (2), the corresponding $J-M_J^2$ plot can be obtained, which provides an extra test of the conclusion from the $n-M^2$ plot.

When further checking the relation of masses of high-spin mesons with the principle quantum number N = n+J, we find that there exists a symmetry of the spectrum in the form

$$M_N^2 = M_0^2 + \beta^2 N, (3)$$

where this phenomenon argues in favor of the existence of the principle quantum that governs the spectrum of excited mesons indicated in Refs. [53, 54].

In the following, we briefly explain the QPC model adopted in this work. After the QPC model was proposed by Micu [55], it was further developed by the Orsay group [56–60]. Later, the model was widely applied to study the OZI-allowed strong decay of hadrons [2, 61–81].

For a two-body strong decay process $A \rightarrow B + C$, the corresponding transition matrix element can be written as

$$\langle BC|T|A\rangle = \delta^3(\mathbf{P}_B + \mathbf{P}_C)\mathcal{M}^{M_{J_A}M_{J_B}M_{J_C}},\tag{4}$$

where $\mathbf{P}_{B(C)}$ denotes the three-momentum of a final particle B(C). M_{J_i} (i = A, B, C) is an orbital magnetic momentum of the corresponding meson in the decay. $\mathcal{M}^{M_{J_A}M_{J_B}M_{J_C}}$ is the amplitude we calculate. The T operator reads as

$$T = -3\gamma \sum_{m} \langle 1m; 1 - m|00 \rangle \int d\mathbf{p}_{3} d\mathbf{p}_{4} \delta^{3}(\mathbf{p}_{3} + \mathbf{p}_{4})$$
$$\times \mathcal{Y}_{1m} \left(\frac{\mathbf{p}_{3} - \mathbf{p}_{4}}{2} \right) \chi_{1,-m}^{34} \phi_{0}^{34} \left(\omega_{0}^{34} \right)_{ij} b_{3i}^{\dagger}(\mathbf{p}_{3}) d_{4j}^{\dagger}(\mathbf{p}_{4}), \quad (5)$$

where γ is a parameter that takes the value 8.7 or 8.7/ $\sqrt{3}$ when the quark-antiquark pair created from the vacuum is $u\bar{u}(d\bar{d})$ or $s\bar{s}$ [75]. The quark and antiquark created from the vacuum are marked by the subscripts 3 and 4, respectively. i/j denotes the color indexes, χ , ϕ , and ω are the spin, flavor and color wave functions, respectively, and $\mathcal{Y}_{\ell m}(\mathbf{p}) = |\mathbf{p}|^{\ell} Y_{lm}(\mathbf{p})$ is the solid harmonic polynomial (see Refs. [82, 83] for more details). Using the Jacob-Wick formula [84], the amplitude $\mathcal{M}^{M_{J_A}M_{J_B}M_{J_C}}$ can be converted into the partial wave amplitude $M^{JL}(\mathbf{P})$, i.e.,

$$\mathcal{M}^{JL}(\mathbf{P}) = \frac{\sqrt{4\pi(2L+1)}}{2J_A+1} \sum_{M_{J_B}M_{J_C}} \langle L0; JM_{J_A} | J_A M_{J_A} \rangle \times \langle J_B M_{J_B}; J_C M_{J_C} | J_A M_{J_A} \rangle \mathcal{M}^{M_{J_A}M_{J_B}M_{J_C}}.$$
(6)

Finally, the decay width can be given by

$$\Gamma = \frac{\pi |\mathbf{P}|}{4m_A^2} \sum_{JL} |\mathcal{M}^{JL}(\mathbf{P})|^2, \tag{7}$$

where m_A is the mass of the initial meson A. In the concrete calculation, we use the harmonic oscillator wave function to describe the meson spatial wave function. The harmonic oscillator wave function has the following expression $\Psi_{nlm}(R, \mathbf{p}) = \mathcal{R}_{nl}(R, \mathbf{p})\mathcal{Y}_{lm}(\mathbf{p})$, with R being a parameter, which is given in Ref. [66] for the mesons involved in our calculation.

Before performing the phenomenological analysis of these high-spin mesons, we need to emphasize that the orbital quantum number for the high-spin mesons with $J^{PC}=3^{--}$, 4^{++} , 5^{--} , and 6^{++} cannot be fixed [53, 85, 86]. For example, the meson with $J^{PC}=3^{--}$ is the mixture between the L=2 and L=4 states¹. By our calculation, we find that the contribution of the higher orbital quantum number for these high-spin mesons with $J^{PC}=3^{--}$, 4^{++} , 5^{--} , and 6^{++} is far smaller than that of the lower orbital quantum number when we study their decay behavior. Thus, in the following, we will only consider contributions from the lower orbital quantum number for the discussed high-spin mesons with $J^{PC}=3^{--}$, 4^{++} , 5^{--} , and 6^{++} .

A. Twelve J^{--} states

In this subsection, we discuss twelve observed high-spin states with J^{--} (J=3,4,5) quantum numbers (see Table I). The corresponding analysis of Regge trajectories with the n- M^2 and J- M^2 plots are shown in Fig. 1.

There are eight high-spin states with $J^{PC}=3^{--}$, which are $\omega_3(1670)$, $\omega_3(1945)$, $\omega_3(2255)$, $\omega_3(2285)$, $\phi_3(1850)$, $\rho_3(1690)$, $\rho_3(1990)$, and $\rho_3(2250)$. As it is an effective approach to study the meson categorization, analysis of the Regge trajectory is applied to further discuss $\omega_3(1670)$, $\omega_3(1945)$, $\omega_3(2255)$, $\omega_3(2285)$, and $\phi_3(1850)$. In Ref. [2], the properties of $\rho_3(1690)$, $\rho_3(1990)$, and $\rho_3(2250)$ were studied, where they can be explained as n^3D_3 (n=1,2,3) states in the ρ_3 meson family, respectively. In Fig. 1 (a), we make a comparison of the observed ω_3 and ρ_3 states, which reflects the similarity between the ρ_3 and ω_3 meson families that is due to their similar values of the slope μ^2 . Thus, we can conclude that $\omega_3(1670)$, $\omega_3(1945)$, and $\omega_3(2285)$ are the isospin partners of $\rho_3(1690)$, $\rho_3(1990)$, and $\rho_3(2250)$, respectively.

As shown in Fig. 1 (b), we also give the J- M^2 plot analysis, which also supports the assignments of $\omega_3(1670)$, $\omega_3(1945)$, and $\omega_3(2285)$ as the ground state, first, and second radial excitations, respectively. In addition, the J- M^2 analysis also indicates that $\phi_3(1850)$ is the ground state in the ϕ_3 meson family.

¹ The meson with $J^{PC}=4^{++}$ is the mixture between the L=3 and L=5 states, the meson with $J^{PC}=5^{--}$ is from the mixture between the L=4 and L=6 states, and the meson with $J^{PC}=6^{++}$ is due to the mixture between the L=5 and L=7 states

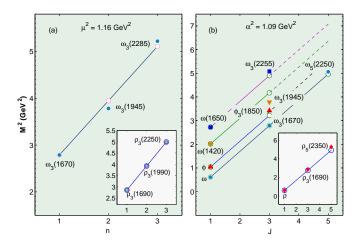


FIG. 1: (color online). Analysis of Regge trajectories for the observed states with J^{--} quantum numbers. Diagram (a) is he $n\text{-}M^2$ plots for ω_3 and ρ_3 states, while diagram (b) is the corresponding $J\text{-}M^2$ plots for ω , ϕ , and ρ . Here, open and filled circles are the theoretical and experimental values, respectively, and $\rho(770)$, $\omega(782)$, and $\phi(1020)$ are abbreviated as ρ , ω , and ω , respectively; these conventions are adopted in the following figures.

The partial wave analysis in Ref. [5] indicates that $\omega_3(2255)$ is a *G*-wave meson. Furthermore, $\omega_3(2255)$ corresponds to $\omega_3(1^3G_3)$, an assignment that is supported by the J- M^2 plot in Fig. 1 (b). Later, we will discuss the decay behavior of $\omega_3(2255)$ corresponding to this assignment.

We notice that the mass $\omega_4(2250)$ is close to that of $\rho_4(2230)$, which shows that it is reasonable to assign $\omega_4(2250)$ as the isospin partner of $\rho_4(2230)$. In this work, $\omega_4(2250)$ and $\rho_4(2230)$ are treated as $\omega_4(1^3G_4)$ and $\rho_4(1^3G_4)$, respectively.

According to the J- M^2 plot shown in Fig. 1 (b), we can conclude that $\omega_5(2250)$ and $\rho_5(2350)$ are mesons with quantum number 1^3G_5 .

In the following, we further present the study of their twobody OZI-allowed decays.

1.
$$\omega_3(1670)$$
, $\omega_3(1945)$, $\omega_3(2255)$, $\omega_3(2285)$, and $\phi_3(1850)$

As for $\omega_3(1670)$, its two-body OZI-allowed strong decays with a 1^3D_3 assignment are given in Fig. 2. When taking $R=4.0-5.4~{\rm GeV^{-1}}$, our theoretical result overlaps with the experimental width of $\omega_3(1670)$ [87]². Here, $\pi\rho$ and πb_1 are main decay modes of $\omega_3(1670)$; this is consistent with the experimental observation because $\pi\rho$ and $\pi\omega\pi$ channels were reported in experiment and $b_1(1235)$ dominantly decays into

 $\pi\omega$. In summary, $\omega_3(1670)$ as $\omega_3(1^3D_3)$ meson is possible: this was addressed in Refs. [6, 31, 34, 88].

We present the decay behavior of $\omega_3(1945)$ under the 2^3D_3 state assignment, in Fig. 2. The obtained total decay width can reproduce the experimental width of $\omega_3(1945)$ measured in Ref. [5] if R = 4.5 - 4.7 GeV⁻¹. Our results also show that $\pi\rho$, πb_1 , and $\eta\omega$ are its main decay channels. As $\omega_3(1945) \to \eta\omega$ was reported in Ref. [5], we thus suggest further experimental searches for decay channels $\pi\rho$ and πb_1 , which would be useful to test the underlying structure of $\omega_3(1945)$.

The decay properties of $\omega_3(2285)$ are given in Fig. 2. When taking $R=4.7-5.0~{\rm GeV}^{-1}$, our theoretical results are consistent with the measured experimental width [5]. In addition, $\omega_3(2285)$ mainly decays into $\pi\rho$, πb_1 , and $\eta\omega$, which could explain why $\omega_3(2285)$ was first observed in the $\eta\omega$ channel [5]. Experimental exploration of $\omega_3(2285)$ via the several remaining main decay modes predicted in this work would be an an interesting area for investigation.

The above studies indicate that description of $\omega_3(1670)$, $\omega_3(1945)$, and $\omega_3(2285)$ as the ground state, first and second radial excitations, respectively, should be further tested.

Next, we illustrate the decay behaviors of $\omega_3(2255)$ under the $\omega_3(1^3G_3)$ assignment (see Fig. 3 for the details). Its dominant decay channels are ρa_1 , πb_1 , $\eta \omega$, and ρa_2 . Additionally, the channels ωf_2 , and ηh_1 also contribute, mainly to the total width. These quantitative predictions can serve as further experimental investigation of $\omega_3(2255)$. We need to specify that the obtained total decay width is strongly dependent on the range of R value. Experimental data of the width of $\omega_3(2255)$ was given by Ref. [5], which can be reproduced by our calculation with $R \sim 7 \text{ GeV}^{-1}$. For the experimental study of $\omega_3(2255)$, a crucial task is the precise measurement of its resonance parameter, which can provide more abundant information for identifying $\omega_3(2255)$ as the 1^3G_3 assignment.

There is only one ϕ_3 state listed in the PDG, i.e., $\phi_3(1850)$. We calculate its two-body decays under the $\phi_3(1^3D_3)$ assignment, listed in Fig. 3. Here, K^*K^* , KK^* , KK, and $KK_1(1270)$ are the main decay modes of $\phi_3(1850)$. We notice that experimental data of ratio $\Gamma_{KK^*}/\Gamma_{KK}=0.55^{+0.85}_{-0.45}$ [7] shows that the partial width of the KK mode is larger than that of the KK^* mode. However, our result shows that the partial width of the KK mode is smaller than that of the KK* mode for $\phi_3(1850)$, since we obtain $\Gamma_{KK^*}/\Gamma_{KK}=3.5-18$. Our conclusion of the KK and KK^* channels is also supported by the study presented in Ref. [89], where the authors obtained $\Gamma_{KK} = 43 \pm 4$ MeV and $\Gamma_{KK^*} = 55 \pm 10$ MeV. Because there is only one experimental measurement for this ratio at present, we expect future experiments to clarify the above inconsistency between theoretical and experimental results. Additionally, when we take $R = 5.3 - 7.0 \,\text{GeV}^{-1}$, we can find a common range where the theoretical result is consistent with the experimental width given in Ref. [38].

2. $\omega_4(2250)$, $\rho_4(2230)$, $\omega_5(2250)$ and $\rho_5(2350)$

As the candidates of $\omega_4(1^3G_4)$ and $\rho_4(1^3G_4)$, respectively, $\omega_4(2250)$ and $\rho_4(2230)$ have the decay behaviors listed in Fig.

² Just shown in PDG [1], different experiments gave different results of the width of $\omega_3(1670)$. When comparing our calculation with experimental data, we adopt the result in Ref. [87] since the corresponding R value is reasonable. In the following discussion, we notice the adopted R ranges for $\omega_3(1945)$ and $\omega_3(2285)$, which satisfy the requirement that the R range becomes more larger with increasing the radial quantum number.

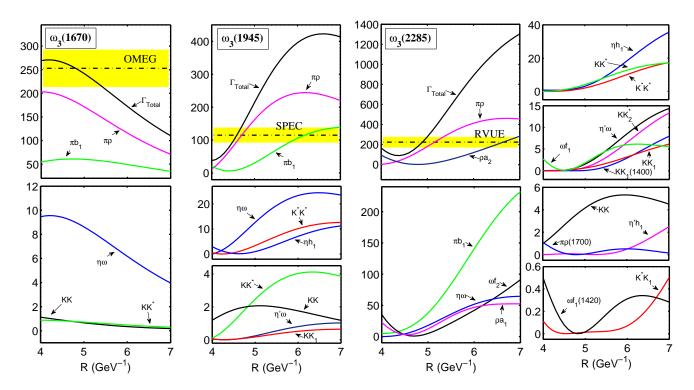


FIG. 2: (color online). The *R*-value dependence of the partial and total decay widths of $\omega_3(1670)$, $\omega_3(1945)$, and $\omega_3(2285)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are the corresponding experimental widths of $\omega_3(1670)$ [87], $\omega_3(1945)$ [5], and $\omega_3(2285)$ [5]. Here, $a_1(1260)$, $h_1(1170)$, $f_1(1285)$, $K^*(892)$, $K_1(1270)$, and $K_2^*(1430)$ are abbreviated as a_1 , h_1 , f_1 , K^* , K_1 , and K_2^* , respectively; these conventions are adopted in the following figures.

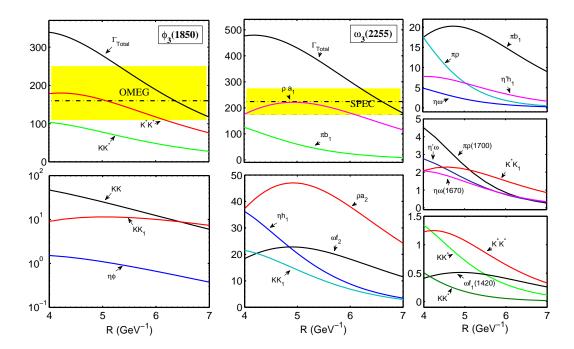


FIG. 3: (color online). The *R*-value dependence of the partial and total decay widths of the $\omega_3(2255)$ and $\phi_3(1850)$ states under discussion. All results are in units of MeV. The dot-dashed lines with yellow bands are the corresponding experimental widths of $\omega_3(2255)$ [5] and $\phi_3(1850)$ [38].

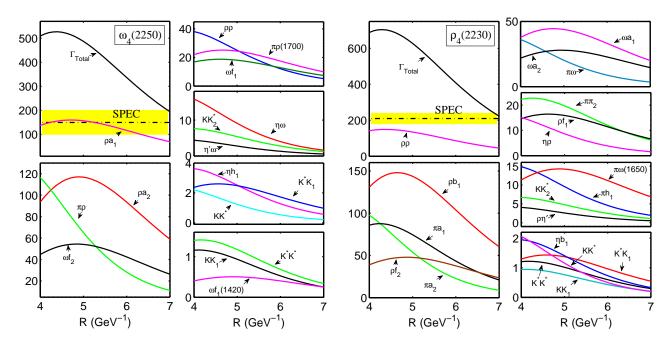


FIG. 4: (color online). The *R*-value dependence of the partial and total decay widths of $\omega_4(2250)$ and $\rho_4(2230)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands denote the corresponding experimental widths of $\omega_4(2250)$ [5] and $\rho_4(2230)$ [11]. Here, $\pi_2(1670)$ is abbreviated as π_2 .

4, we conclude, with this study, that ρa_1 , ρa_2 , and $\pi \rho$ are the main decay modes of $\omega_4(2250)$, while $\rho_4(2230)$ mainly decays into $\rho \rho$, ρb_1 , πa_2 , and πa_1 . At present, experimental information for $\omega_4(2250)$ and $\rho_4(2230)$ is still scarce. For example, there is only one experimental measurement for the widths of $\omega_4(2250)$ and $\rho_4(2230)$. When $R \approx 7 \text{ GeV}^{-1}$ is adopted, theoretical total decay widths can overlap with the experimental data for $\omega_4(2250)$ [5] and $\rho_4(2230)$ [11].

Both $\omega_5(2250)$ and $\rho_5(2350)$ are good candidates for G-wave mesons. In Fig. 5, we present their decay features. Here, the main decay modes of $\omega_5(2250)$ include ρa_2 , ωf_2 , πb_1 and $\pi \rho$, among which πb_1 was reported in experiment [90]. The dominant decay modes of $\rho_5(2350)$ are ρf_2 and ωa_2 , while $\rho \rho$, πa_2 and πh_1 are also important contributions to the total decay width. Because the experimental status of $\omega_5(2250)$ and $\rho_5(2350)$ is similar to that of $\omega_4(2250)$ and $\rho_4(2230)$, there is not enough information on their experimental data. Thus, we compare the obtained total widths of $\omega_5(2250)$ and $\rho_5(2350)$ with the present experimental data [48, 90] (see Fig. 5 for more details).

These theoretical predictions of the decay behaviors of $\omega_4(2250)$, $\rho_4(2230)$, $\omega_5(2250)$ and $\rho_5(2350)$ will be useful for future experimental studies.

B. Eleven J^{++} states

As listed in Table I, 11 high-spin states with the J^{++} (J = 3,4,6) quantum numbers were reported in experiments. In Fig. 6, we present the systematic analysis of Regge trajectories with the n- M^2 and J- M^2 plots, which is helpful for obtaining the information regarding their classification into meson families.

Figure. 6 (a) shows that $f_3(2050)$ is the ground state of the f_3 family, while $f_3(2300)$ is the radial excitation, which is in good agreement with the conclusion in Refs. [8, 30]. As the isospin parters of $f_3(2050)$ and $f_3(2300)$, $a_3(2030)$ and $a_3(2275)$ are the ground state and the first radial excitation in the a_3 meson family, respectively, which is reflected in Fig. 6 (a). In addition, we notice the $a_3(1875)$ state, which cannot be categorized into the a_3 meson family. Thus, in the following discussion of their decay behaviors, we will mainly focus on $f_3(2050)$, $f_3(2300)$, $a_3(2030)$, and $a_3(2275)$.

When checking $a_4(2040)$ and $a_4(2255)$ and their isospin partners $f_4(2050)$ and $f_4(2300)$, we conclude that $a_4(2040)/f_4(2050)$ and $a_4(2255)/f_4(2300)$ are the ground state and the first radial excitation in the a_4/f_4 meson families, respectively; this can be supported by the analysis of the n- M^2 and J- M^2 plots shown in Fig. 6.

From the analysis shown in Fig. 6, we can conclude that $f_6(2510)$ is a candidate of the $f_6(1^3H_6)$ meson and that $a_6(2450)$ is the isospin partner of $f_6(2510)$.

In the following, we further test the above-mentioned meson assignments to the states with J^{++} quantum numbers by studying their two-body OZI-allowed strong decays.

1. $f_3(2050)$, $f_3(2300)$, $a_3(2030)$, and $a_3(2275)$

In Figs 7-9, the decay behaviors of $f_3(2050)$, $f_3(2300)$, $a_3(2030)$, and $a_3(2275)$ are given, where their partial and total decay widths are obtained by the QPC model. We also compare our results with the experimental data.

 $f_3(2050)$ and $f_3(2300)$ are treated as $f_3(1^3F_3)$ and $f_3(2^3F^3)$, respectively, with isospin I = 0. Our calculation for $f_3(2050)$ indicates that $\rho\rho$, πa_2 , ρb_1 , and πa_1 are its main decay channels, and $f_3(2050) \rightarrow \eta f_2$ is a sizable contribution to its total decay width, this could explain why experiments reported $f_3(2050)$ in its πa_2 and ηf_2 decay modes. However, the obtained total decay width of $f_3(2050)$ is far larger than the experimental width given in Ref. [8] when taking R = 4 - 7GeV⁻¹. For $f_3(2300)$, the main decay channels include $\rho\rho$, ρb_1 , $\pi \pi_2$, and $\omega \omega$. The calculated total decay width of $f_3(2300)$ is also larger than the experimental data [8] (see Fig. 7). The situation of $f_3(2050)$ is similar, to an extent, to that of $f_3(2050)$. To further clarify the above inconsistency between the experimental width and the theoretical result, further experimental measurement of $f_3(2050)$ and $f_3(2300)$ is encouraged.

Before illustrating the decay properties of $a_3(2030)$, and $a_3(2275)$, the isospin partners of $f_3(2050)$ and $f_3(2300)$, we still need to discuss $a_3(1875)$. Although $a_3(1875)$ cannot be grouped into the a_3 meson family in term of the analysis of the Regge trajectories only, the authors of Ref. [31] suggest that $a_3(1875)$ and $a_3(2030)$ are the same state. If $a_3(1875)$ is $a_3(1^3F_3)$, our calculated results of the branching ratio $B(a_3(1875) \rightarrow f_2(1270)\pi)/B(a_3(1875) \rightarrow \pi\rho)$ is about 1, which is consistent with the experimental data 0.8 ± 0.2 given in Ref. [9]. Additionally, $B(a_3(1875) \rightarrow$ $\rho_3(1690)\pi)/B(a_3(1875) \rightarrow \pi\rho)$ in Ref. [9] is about 0.9 ± 0.3, where our calculation gives 1.9 - 2.4 for this ratio. The $a_3(1^3F_3)$ assignment to $a_3(1875)$, therefor, seems to be reasonable. Thus, measuring the resonance parameters of $a_3(1875)$ and $a_3(2030)$ is crucial to test whether $a_3(1875)$ and $a_3(2030)$ are the same state.

 $a_3(2030)$ mainly decays into $\rho\omega$, $\pi\rho$, and ρh_1 , and ηa_2 and πf_2 sizably contribute to the total width. Here, the $a_3(2030)$ decays into ηa_2 and πf_2 were observed in experiment [1]. The theoretical total decay width of $a_3(2030)$ with the range $R=4-7~{\rm GeV^{-1}}$ is far larger than the experimental measurement [25]. Under the $a_3(1^3F_3)$ meson assignment, $a_3(2275)$ has main decay modes $\rho\omega$, ρa_1 , and $\pi\rho$. Figure. 8 displays the R dependence of the partial decay width of $a_3(2275)$; this shows that the calculated total width overlaps with the experimental data [33] when $R=4.6-5~{\rm GeV^{-1}}$.

2. $f_4(2050)$, $f_4(2300)$, $a_4(2040)$, and $a_4(2255)$

In this subsection, we present the decay properties for four 4^{++} states $f_4(2050)$, $f_4(2300)$, $a_4(2040)$, and $a_4(2255)$, which are shown in Figs. 9-10.

The results of $f_4(2050)$ shown in Fig. 9 indicate that $\rho\rho$, πa_2 , and $\omega\omega$ are its dominant decay channels. Furthermore, we also obtain some typical ratios, which are comparable with

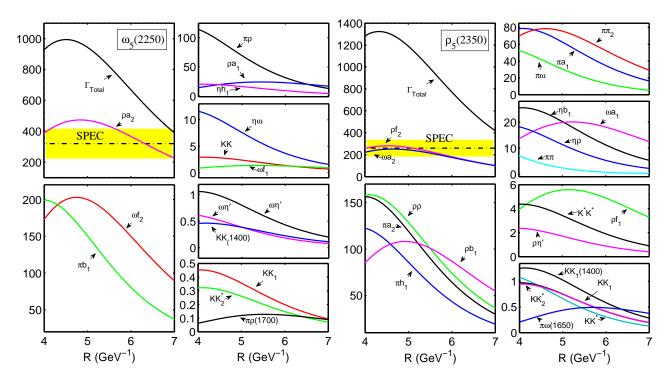


FIG. 5: (color online). The *R*-value dependence of the partial and total decay widths of $\omega_5(2250)$ and $\rho_5(2350)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are experimental widths of $\omega_5(2250)$ [90] and $\rho_5(2350)$ [48].

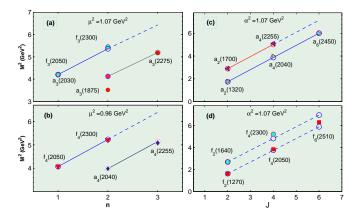


FIG. 6: (color online). The analysis of Regge trajectories for the observed states with J^{++} quantum numbers. (a) and (b) are the n- M^2 plots for the 3^{++} and 4^{++} states, respectively, while (c) and (d) are the corresponding J- M^2 plots. For (a) and (b), the $I = 1 \ n$ - M^2 trajectories are displaced one unit to the right in n in order to resolve them from I = 0.

the experimental data (see Table II for more details). For $f_4(2300)$, πa_2 and $\rho \rho$ are its dominant decay channels, and the obtained ratio $\Gamma_{f_4(2300) \to \rho \rho} / \Gamma_{f_4(2300) \to \omega \omega} = 0.6 - 3.1$ is consistent with the experimental value 2.8 ± 0.5 [15]. The total decay widths of $f_4(2050)$ and $f_4(2300)$ overlap with the corresponding experimental widths when R = 4 - 7 GeV⁻¹. Thus, these studies support $f_4(2050)$ and $f_4(2300)$ as the candidates

TABLE II: Comparison between the calculated and experimental results for some typical ratios of $f_4(2050)$. Here, the theoretical results are obtained by taking $R=4.0-7.0~{\rm GeV}^{-1}$.

Ratios	This work	Experiment
$\Gamma_{KK}/\Gamma_{\pi\pi}$	0.019 - 0.025	$0.04^{+0.02}_{-0.01}$ [14]
$\Gamma_{\pi\pi}/\Gamma_{Total}$	0.006 - 0.036	0.170 ± 0.015 [1]
$\Gamma_{\omega\omega}/\Gamma_{\pi\pi}$	3.9 - 21	1.5 ± 0.3 [14]
$\Gamma_{\eta\eta}/\Gamma_{Total}$	$(0.25-1.3)\times 10^{-3}$	$(2.1 \pm 0.8) \times 10^{-3}$ [13]

of $f_4(1^3F_4)$ and $f_4(2^3F_4)$, respectively.

As isospin partners of $f_4(2050)$ and $f_4(2300)$, the decay features of $a_4(2040)$ and $a_4(2255)$ are similar to those of $f_4(2050)$ and $f_4(2300)$, respectively. Overlap exists between the experimental and calculated results of the total decay width for $a_4(2040)$ when R=4.0-5.8 GeV⁻¹. The dominant decay channels of $a_4(2040)$ are $\rho\omega$ and πb_1 as given in Fig. 10. The ratio $\Gamma_{\pi\rho}/\Gamma_{\pi f_2}=1.1\pm0.2\pm0.2$ was obtained in Ref. [9], this can be well reproduced by our calculations, with the value 1.2-2.1. In addition, we obtain the partial widths of $a_4(2040)$ decaying into $\pi\rho$ and KK, i.e., $\Gamma_{a_4(2040)\to\pi\rho}=19-57$ MeV and $\Gamma_{a_4(2040)\to KK}=0.035-0.43$ MeV, which deviates from the experimental data $\Gamma_{a_4(2040)\to\pi\rho}=10\pm3$ MeV and $\Gamma_{a_4(2040)\to KK}=6\pm2$ MeV, respectively in Ref. [89]. Further experimental study of $a_4(2040)$ would, thus, be useful.

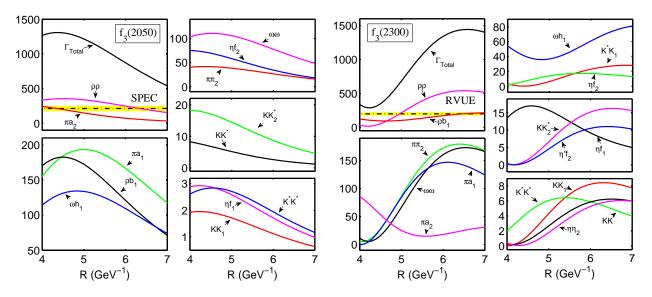


FIG. 7: (color online). The *R* dependence of the partial and total decay widths of $f_3(2050)$ and $f_3(2300)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are the corresponding experimental widths of $f_3(2050)$ [8], and $f_3(2300)$ [6]. Here, $\eta_2(1645)$ is abbreviated as η_2 , as adopted though this work.

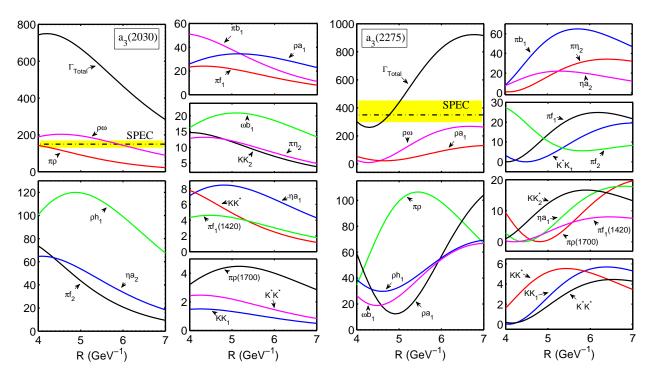


FIG. 8: (color online). The R dependence of the partial and total decay widths of $a_3(2030)$ and $a_3(2275)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are the corresponding experimental widths of $a_3(2030)$ [25], and $a_3(2275)$ [33]. Here, $K_2(1580)$ is abbreviated as K_2 adopted in this work.

In the results given in Fig. 10, one notices the overlap between calculated total widths and experimental data [23, 25]. Here, πb_1 and $\rho \omega$ are the main decay modes of $a_4(2255)$, while $\pi \rho$ and πf_2 are sizable decay channels. Only $a_4(2255) \rightarrow \pi f_2$ was reported in Ref. [10]. Thus, we also suggest searching for the πb_1 and $\rho \omega$ modes for $a_4(2255)$ if it

is a $a_4(2^3F_4)$ state.

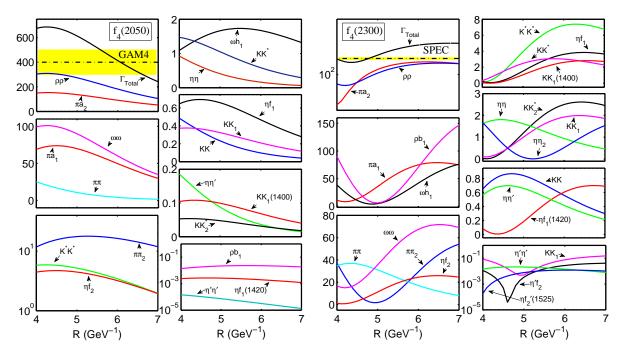


FIG. 9: (color online). The R dependence of the partial and total decay widths of $f_4(2050)$ and $f_4(2300)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are experimental widths of $f_4(2050)$ [13] and $f_4(2300)$ [8].

3. $f_6(2510)$ and $a_6(2450)$

There are two 6^{++} states, $f_6(2510)$ and its isospin partner $a_6(2450)$, which are treated as 1^3H_6 states. We calculate their partial and total decay widths, presented in Fig. 11.

The results in Fig. 11 show that there is an overlap between experimental value [8] and our calculation of the total decay width of $f_6(2510)$ when R in the range of 5.2-6.0 GeV⁻¹, this gives a direct support for the $f_6(1^3H_6)$ assignment to $f_6(2510)$. Unfortunately, the obtained branching ratio $B(f_6(2510) \rightarrow \pi\pi) = 3.7 \times 10^{-4} - 3.2 \times 10^{-3}$ is smaller than the experimental value in Ref. [29] (see Table I). Since there is only one experimental measurement for this branching ratio, this ratio should be confirmed by other experiments. In addition to the above information, we also get the dominant decay channel of $f_6(2510)$, i.e., ρb_1 and we find that $\rho \rho$, πa_2 , and $\pi \pi_2$ are its important channels.

Under the $a_6(1^3H_6)$ assignment, $a_6(2450)$ has a total decay width consistent with the experimental result in Ref. [20] if we take $R=4-7~{\rm GeV^{-1}}$, where experimental data of the width has a large error bar. The main decay channels are ρa_2 , πb_1 , $\rho \omega$, and ρh_1 . The remaining OZI-allowed decay information can be found in Fig. 11.

C. Four 3⁺⁻ states

In Fig. 12 (a), we first give the n- M^2 plot analysis for four observed 3⁺⁻ states $h_3(2025)$, $h_3(2275)$, $b_3(2030)$, and $b_3(2245)$. Here, $h_3(2025)$ and $h_3(2275)$ are the ground state and first radial excitation in the h_3 meson family, while

 $b_3(2030)$ and $b_3(2245)$ are the isospin partners of $h_3(2025)$ and $h_3(2275)$, respectively.

With the above assignments to the observed 3^{+-} states, we further discuss their strong decay behaviors.

As illustrated in Fig. 13, $\pi\rho$, $\eta\omega$, and ρa_1 are the main decay channels of $h_3(2025)$, which can explain why this was observed in the $\eta\omega$ channel. In addition, we find that a theoretical result overlaps with the experimental width [5]. Thus, we suggest future experimental study of $h_3(2025)$ by its other dominant decay modes $\pi\rho$ and ρa_1 , which are still missing in experiment.

 $h_3(2275)$ mainly decays into ρa_2 , $\pi \rho$, ρa_1 , ωf_2 , and $\eta \omega$. This state was observed in the processes $p\bar{p} \to \eta \omega$, $\omega \pi^0 \pi^0$ [5]. The detailed decay information of $h_3(2275)$ can be found in Fig. 13. We notice that inconsistency exists inconsistency between the experimental width and the obtained total decay width, since the calculated total decay width under R=4-7 GeV⁻¹ is larger than the experimental data [5].

From the results in Fig. 14, we conclude that the main decay modes of $b_3(2030)$ are πa_2 and $\rho \rho$, and πa_1 , $\pi \omega$, ρb_1 , and $\eta \rho$ have sizable contributions to the total decay width. Here, $\pi \omega$ and $\pi^+\pi^-$ decay channels of $b_3(2030)$ were observed in experiment [11], where $\pi^+\pi^-$ can be from ρ . This experimental phenomenon does not contradict our theoretical result. However, the obtained total decay width of $b_3(2030)$ cannot fall into the range of experimental width when taking R=4-7 GeV⁻¹, which is a situation similar to $h_3(2275)$. In future, we need more experimental measurements of the resonance parameters of $h_3(2275)$ and $b_3(2030)$.

Another observed b_3 state is $b_3(2245)$. As displayed in Fig. 14, there is an overlap between calculated total width and ex-

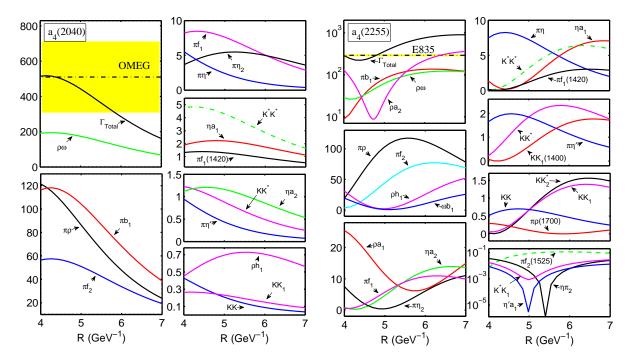


FIG. 10: (color online). The *R* dependence of the partial and total decay widths of $a_4(2040)$ and $a_4(2255)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are the corresponding experimental widths of $a_4(2040)$ [46] and $a_4(2255)$ [23].

perimental data [10]. Its main decay channels are $\rho\rho$, ρb_1 , and πa_2 ; the πa_1 , ρf_2 , ωa_2 and $\pi \omega$ channels have important contributions to the total decay width, where ωa_2 and $\pi \omega$ are the observed channels [10].

D. Two 4^{-+} states

In this subsection, we discuss the last two observed highspin states, $\eta_4(2330)$ and $\pi_4(2250)$, which have 4^{-+} quantum numbers (see Table I). The corresponding analysis of Regge trajectories with the J- M^2 plot is shown in Fig. 12 (b); this was used to study 2^{-+} states in our previous work [79]. π and π_2 [79] are the ground states of their own families. Thus, Fig. 12 (b) indicates that $\eta_4(2330)$ and $\pi_4(2250)$ are the ground states of the η_4 and π_4 meson families. In fact, Refs. [30, 34, 45, 88] gave the same suggestion. In the following, we calculate their two-body strong decays with the assignments $\eta_4(1^1G_4)$ and $\pi_4(1^1G_4)$ to $\eta_4(2330)$ and $\pi_4(2250)$, respectively.

Our calculated theoretical total width of $\eta_4(2330)$ is larger than experimental data [8], where the main decay channels are ρb_1 , $\rho \rho$ and πa_2 , while πa_1 , ωh_1 , $\omega \omega$, and ηf_2 are its important decay channels. $\eta_4(2330)$ was first reported in the final states $(\pi a_2)_{L=4}$ and $(a_0\pi)_{L=4}$, and was also observed in the ηf_2 channel [10]. The information from its partial decay width shows that $\eta_4(2330)$ as 1^1G_4 is reasonable. At present, a crucial task is to further check the resonance parameters of $\eta_4(2330)$.

Figure. 15 present the decays of $\pi_4(2250)$. We find the theoretical total width is larger than the SPEC data [25] if we take the R = 4 - 7 GeV⁻¹ range. $\pi_4(2250)$ mainly decays into

 $\rho\omega$, ρa_2 , ρh_1 and ρa_1 .

Before closing this section, we list some additional important ratios in Table III, where we collect the corresponding *R* values that can be adopted to reproduce the experimental data.

IV. CONCLUSIONS AND DISCUSSION

In this work, we have mainly focused on the study of 26 high-spin states reported in experiments; we have performed the mass spectrum analysis and have carried out the calculation of their two-body OZI-allowed strong decays, which is helpful in revealing their underlying features. The first task is to explore whether the observed high-spin states can be categorized into conventional meson families.

The analysis of Regge trajectories with the n- M^2 and J- M^2 plots has provided an effective approach to study the meson categorization phenomenologically. We have discussed the possible meson assignments to the observed high-spin states listed in PDG [1]. The main task of the present work has been the calculation of the two-body OZI-allowed strong decays of the high-spin states, which can be applied to test the possible meson assignments. In Sec. III, we have discussed this point in detail. The predicted decay behaviors of the discussed high-spin states can provide valuable information for further experimental study in the future.

At present, most of the high-spin states reported in experiments are collected into the further states in the PDG [1], because the experimental information of these high-spin unflavored states is not abundant. Thus, we suggest that more ex-

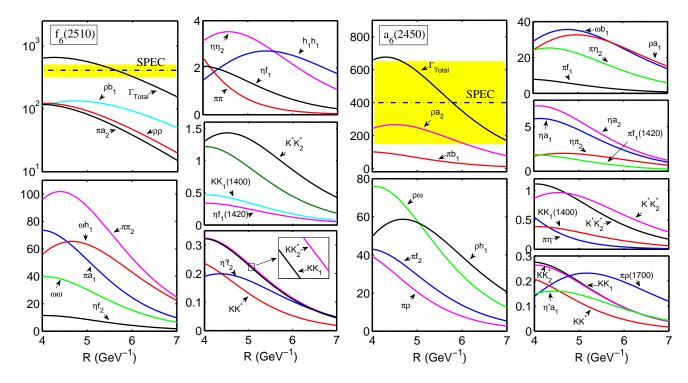


FIG. 11: (color online). The *R* dependence of the partial and total decay widths of the $f_6(2510)$ and $a_6(2450)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are experimental widths of $f_6(2510)$ [8] and $a_6(2450)$ [20].

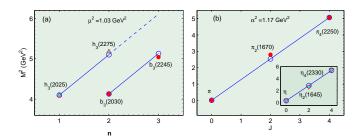


FIG. 12: (color online). The analysis of Regge trajectories for the observed states with 3^{+-} and J^{-+} quantum numbers. Diagram (a) is the n- M^2 plot for the 3^{+-} states, while a diagram (b) is the corresponding J- M^2 plot for the J^{-+} states. In (a), the n- M^2 trajectory with I=1 is displaced one unit to the right in n in order to resolve it from I=0.

perimental measurements of the resonance parameters should be obtained, and the missing main decay channels searched for. Such efforts will be helpful in establishing these high-spin states in experiments.

With the experimental progress, the exploration of high-spin mesons is becoming an important issue in hadron physics, with good platforms in BESIII, BelleII, and COMPASS experiments. We hope that inspired by this work, more experimental and theoretical studies of high-spin states are conducted in the future.

Acknowledgments

This project is supported by the National Science Foundation for Fostering Talents in Basic Research of the National Natural Science Foundation of China and the National Natural Science Foundation of China under Grants No. 11222547 and No. 11175073, the Ministry of Education of China (SRFDP under Grant No. 2012021111000), and the Fok Ying Tung Education Foundation (Grant No. 131006).

K. A. Olive *et al.* [Particle Data Group Collaboration], Chin. Phys. C 38, 090001 (2014). Phys. Rev. Lett. 94, 032002 (2005)

^[2] L. -P. He, X. Wang and X. Liu, Phys. Rev. D 88, no. 3, 034008 (2013) [arXiv:1306.5562 [hep-ph]].

^[3] J. Diaz, F. A. Dibianca, W. J. Fickinger, J. A. Malko, D. K. Robinson, C. R. Sullivan, J. C. Anderson and A. Engler et al., Phys. Rev. Lett. 32, 260 (1974).

^[4] M. Baubillier et al. [Birmingham-CERN-Glasgow-Michigan

State-Paris Collaboration], Phys. Lett. B 89, 131 (1979).

^[5] A. V. Anisovich, C. A. Baker, C. J. Batty, D. V. Bugg, L. Montanet, V. A. Nikonov, A. V. Sarantsev and V. V. Sarantsev *et al.*, Phys. Lett. B **542**, 19 (2002) [arXiv:1109.5817 [hep-ex]].

^[6] D. V. Bugg, Eur. Phys. J. C 36, 161 (2004) [hep-ph/0406292].

^[7] D. Aston, N. Awaji, T. Bienz, F. Bird, J. D'Amore, W. M. Dunwoodie, R. Endorf and K. Fujii *et al.*, Phys. Lett. B 208, 324 (1988).

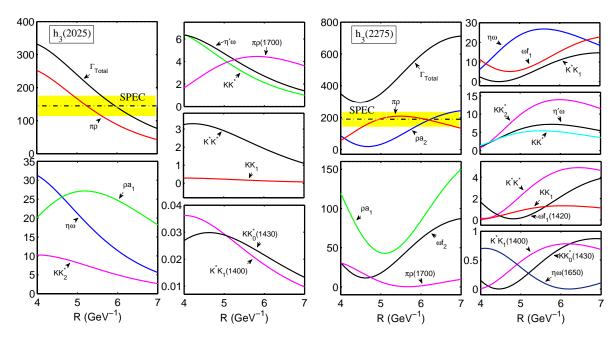


FIG. 13: (color online). The *R* dependence of the partial and total decay widths of $h_3(2025)$ and $h_3(2275)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are the corresponding experimental widths of $h_3(2025)$ and $h_3(2275)$ [5].

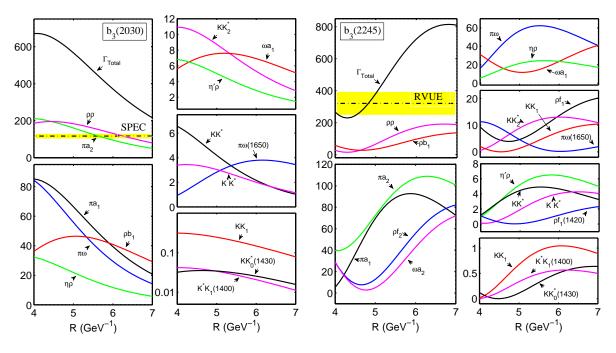


FIG. 14: (color online). The *R* dependence of the partial and total decay widths of $b_3(2030)$ and $b_3(2245)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are the corresponding experimental widths of $b_3(2030)$ [11], and $b_3(2245)$ [10].

- [8] A. V. Anisovich, C. A. Baker, C. J. Batty, D. V. Bugg, C. Hodd, H. C. Lu, V. A. Nikonov and A. V. Sarantsev *et al.*, Phys. Lett. B 491, 47 (2000) [arXiv:1109.0883 [hep-ex]].
- [9] S. U. Chung, K. Danyo, R. W. Hackenburg, C. Olchanski, J. S. Suh, H. J. Willutzki, S. P. Denisov and V. Dorofeev *et al.*, Phys. Rev. D **65**, 072001 (2002).
- [10] D. V. Bugg, Phys. Rept. 397, 257 (2004) [hep-ex/0412045].
- [11] A. V. Anisovich, C. A. Baker, C. J. Batty, D. V. Bugg, L. Montanet, V. A. Nikonov, A. V. Sarantsev and V. V. Sarantsev *et al.*, Phys. Lett. B **542**, 8 (2002) [arXiv:1109.5247 [hep-ex]].
- [12] D. Alde *et al.* [IHEP-IISN-LANL-LAPP-TSUIHEP Collaboration], Phys. Lett. B **241**, 600 (1990).
- [13] D. Alde *et al.* [Serpukhov-Brussels-Los Alamos-Annecy(LAPP) Collaboration], Nucl. Phys. B **269**, 485

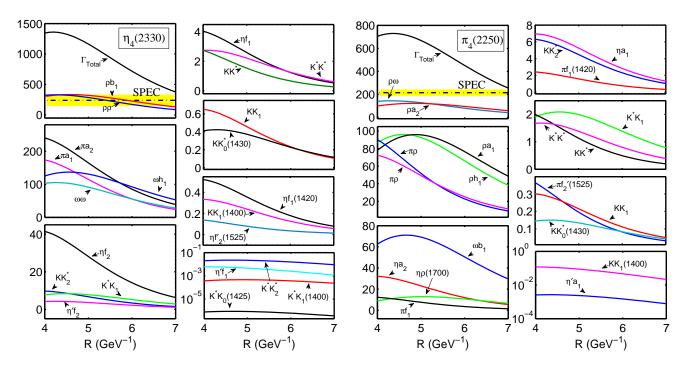


FIG. 15: (color online). The *R* dependence of the and total decay widths of $\pi_4(2250)$ and $\eta_4(2330)$ states. All results are in units of MeV. The dot-dashed lines with yellow bands are the corresponding experimental widths of $\pi_4(2250)$ [5] and $\eta_4(2330)$ [8].

(1986).

- [14] A. Etkin, K. J. Foley, R. S. Longacre, W. A. Love, T. W. Morris, S. Ozaki, E. D. Platner and V. A. Polychronakos *et al.*, Phys. Rev. D 25, 1786 (1982).
- [15] D. Barberis *et al.* [WA102 Collaboration], Phys. Lett. B **484**, 198 (2000) [hep-ex/0005027].
- [16] D. Cutts, M. L. Good, P. D. Grannis, D. Green, Y. Y. Lee, R. Pittman, J. Storer and A. C. Benvenuti *et al.*, Phys. Rev. D 17, 16 (1978).
- [17] A. Hasan and D. V. Bugg, Phys. Lett. B 334, 215 (1994).
- [18] A. A. Carter, M. Coupland, E. Eisenhandler, W. R. Gibson, P. I. P. Kalmus, D. P. Kimber, A. Astbury and D. P. Jones, Phys. Lett. B 67, 117 (1977).
- [19] D. V. Amelin *et al.* [VES Collaboration], Nucl. Phys. A 668, 83 (2000).
- [20] W. E. Cleland, A. Delfosse, P. a. Dorsaz, J. l. Gloor, M. n. Kienzle-Focacci, G. Mancarella, A. D. Martin and M. Martin et al., Nucl. Phys. B 208, 228 (1982).
- [21] R. Baldi, T. Bohringer, P. A. Dorsaz, V. Hungerbuhler, M. N. Kienzle-Focacci, M. Martin, A. Mermoud and C. Nef et al., Phys. Lett. B 74, 413 (1978).
- [22] M. Lu et al. [E852 Collaboration], Phys. Rev. Lett. 94, 032002 (2005) [hep-ex/0405044].
- [23] I. Uman, D. Joffe, Z. Metreveli, K. K. Seth, A. Tomaradze and P. K. Zweber, Phys. Rev. D 73, 052009 (2006) [hepex/0607034].
- [24] D. Alde *et al.* [GAMS Collaboration], Phys. Atom. Nucl. **59**, 982 (1996) [Yad. Fiz. **59N6**, 1027 (1996)].
- [25] A. V. Anisovich, C. A. Baker, C. J. Batty, D. V. Bugg, V. A. Nikonov, A. V. Sarantsev, V. V. Sarantsev and B. S. Zou, Phys. Lett. B 517, 261 (2001) [arXiv:1110.0278 [hep-ex]].
- [26] E. I. Ivanov et al. [E852 Collaboration], Phys. Rev. Lett. 86, 3977 (2001) [hep-ex/0101058].

- [27] R. J. Abrams, R. L. Cool, G. Giacomelli, T. F. Kycia, B. A. Leontic, K. K. Li and D. N. Michael, Phys. Rev. Lett. 18, 1209 (1967).
- [28] B. Alper *et al.* [Amsterdam-CERN-Cracow-Munich-Oxford-Rutherford Collaboration], Phys. Lett. B **94**, 422 (1980).
- [29] F. G. Binon *et al.* [Serpukhov-Brussels-Annecy(LAPP) Collaboration], Lett. Nuovo Cim. **39**, 41 (1984) [Yad. Fiz. **38**, 1199 (1983)] [Sov. J. Nucl. Phys. **38**, 723 (1983)].
- [30] S. S. Afonin, Phys. Rev. C **76**, 015202 (2007) [arXiv:0707.0824 [hep-ph]].
- [31] P. Masjuan, E. R. Arriola and W. Broniowski, Phys. Rev. D 85, 094006 (2012) [arXiv:1203.4782 [hep-ph]].
- [32] D. Ebert, R. N. Faustov and V. O. Galkin, Phys. Rev. D 79, 114029 (2009) [arXiv:0903.5183 [hep-ph]].
- [33] A. V. Anisovich, C. A. Baker, C. J. Batty, D. V. Bugg, V. A. Nikonov, A. V. Sarantsev, V. V. Sarantsev and B. S. Zou, Phys. Lett. B 517, 273 (2001) [arXiv:1109.6817 [hep-ex]].
- [34] V. V. Anisovich, Phys. Usp. 47, 45 (2004) [Usp. Fiz. Nauk 47, 49 (2004)] [hep-ph/0208123].
- [35] V. V. Anisovich, AIP Conf. Proc. 717, 441 (2004) [hep-ph/0310165].
- [36] N. Armenise, A. Forino and A. M. Cartacci, Phys. Lett. B 26, 336 (1968).
- [37] S. Al- Harran *et al.* [BIRMINGHAM-CERN-GLASGOW-MICHIGAN STATE-PARIS Collaboration], Phys. Lett. B 101, 357 (1981).
- [38] T. Armstrong *et al.* [BARI-BIRMINGHAM-CERN-MILAN-PARIS-PAVIA Collaboration], Phys. Lett. B **110**, 77 (1982).
- [39] W. D. Apel *et al.* [Serpukhov-CERN Collaboration], Phys. Lett. B 57, 398 (1975).
- [40] W. Blum *et al.* [CERN-MUNICH Collaboration], Phys. Lett. B 57, 403 (1975).
- [41] R. J. Abrams, R. L. Cool, G. Giacomelli, T. F. Kycia,

TABLE III: The typical branching ratios of these discussed high-spin mesons corresponding to the successful R values.

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	States	$R (\text{GeV}^{-1})$	Ratios
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	<i>a</i> ₃ (1875)	4.0 – 4.6	$\Gamma_{\pi f_2}/\Gamma_{\text{Total}} = 0.33 - 0.34, \Gamma_{\pi \rho}/\Gamma_{\text{Total}} = 0.3 - 0.33, \Gamma_{\pi \rho}/\Gamma_{\pi f_2} = 0.91 - 0.98, \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.22 - 0.27$
$ \begin{array}{c} \omega_{3}(1670) 4.0 - 5.4 \\ & \Gamma_{\eta\rho}/\Gamma_{Total} = 0.69 - 0.75, \Gamma_{ab}/\Gamma_{Total} = 0.2 - 0.26, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.035 - 0.036, \\ & \Gamma_{\eta\rho}/\Gamma_{Total} = 0.81 - 0.81, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.13 - 0.17, \Gamma_{KK^*}/\Gamma_{Total} = 0.0028 - 0.0032 \\ & \Gamma_{\eta\rho}/\Gamma_{Total} = 0.81 - 0.84, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.073 - 0.092, \Gamma_{ab}, \Gamma_{ap} = 0.087 - 0.11, \\ & \Gamma_{\eta\rho}/\Gamma_{Total} = 0.05 - 0.056, \Gamma_{\eta\rho}/\Gamma_{\eta\rho} = 0.059 - 0.068, \Gamma_{\eta\rho}/\Gamma_{total} = 0.073 - 0.092, \Gamma_{ab}, \Gamma_{ap} = 0.069 - 0.069 \\ & \Phi_{3}(1850) 5.3 - 7.0 \Gamma_{K^*K^*}/\Gamma_{Total} = 0.05 - 0.05, \Gamma_{K^*K^*}/\Gamma_{Total} = 0.24 - 0.27, \Gamma_{K^*K^*}/\Gamma_{K^*K^*} = 0.36 - 0.46 \\ & U_{3}(2285) 4.7 - 5.0 \Gamma_{\eta\rho}/\Gamma_{total} = 0.7 - 0.71, \Gamma_{\pi}h, \Gamma_{total} = 0.13 - 0.13, \Gamma_{\pi\rho}, \Gamma_{Total} = 0.18 - 0.19, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.18 - 0.18, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.18 - 0.19, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.18 - 0.19, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.029 - 0.065, \Gamma_{\kappa}K^*/\Gamma_{Total} = 0.18 - 0.19, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.039 - 0.065, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.029 - 0.021, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.08 - 0.021, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.018 - 0.019, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.039 - 0.065, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.019 - 0.031, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.027 - 0.044, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.019 - 0.031, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.027 - 0.044, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.043 - 0.052, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.043 - 0.052, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.045 - 0.045, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.045 - 0.052, \Gamma_{\eta\rho}/\Gamma_{Total} = 0.027 - 0.045, \Gamma_{\eta\rho}/\Gamma_{\eta\rho$	$a_3(2030)$	4.0 - 7.0	$\Gamma_{\rho\omega}/\Gamma_{\text{Total}} = 0.26 - 0.32, \Gamma_{\rho h_1}/\Gamma_{\rho\omega} = 0.53 - 0.75, \Gamma_{\pi f_2}\Gamma_{\pi\rho} = 0.41 - 0.51, \Gamma_{\eta a_2}/\Gamma_{\text{Total}} = 0.065 - 0.087$
$ \Gamma_{g\omega}/\Gamma_{gp} = 0.046 - 0.051, \ \Gamma_{g\omega}/\Gamma_{rbal} = 0.13 - 0.17, \ \Gamma_{KK'}/\Gamma_{total} = 0.0028 - 0.0032 $ $ \omega_{3}(1945) 5.3 - 7.0 $ $ \Gamma_{g\omega}/\Gamma_{Total} = 0.81 - 0.84, \ \Gamma_{sh}/\Gamma_{Total} = 0.073 - 0.092, \ \Gamma_{sh}\Gamma_{Rp} = 0.087 - 0.11, $ $ \Gamma_{g\omega}/\Gamma_{total} = 0.05 - 0.056, \ \Gamma_{g\omega}/\Gamma_{tp} = 0.059 - 0.068, \ \Gamma_{g\omega}/\Gamma_{sp} = 0.069 - 0.669 $ $ \omega_{3}(2285) 4.7 - 5.0 $ $ \Gamma_{g\omega}/\Gamma_{gp} = 0.083 - 0.092, \ \Gamma_{g\omega}/\Gamma_{gp} = 0.087 - 0.61, $ $ \Gamma_{g\omega}/\Gamma_{gp} = 0.083 - 0.092, \ \Gamma_{g\omega}/\Gamma_{gp} = 0.081 - 0.013, \ \Gamma_{sh}/\Gamma_{total} = 0.024 - 0.27, \ \Gamma_{KK'}/\Gamma_{Kext} = 0.36 - 0.046 $ $ \omega_{3}(2255) 6.2 - 7.0 $ $ \Gamma_{g\omega}/\Gamma_{fp} = 0.083 - 0.092, \ \Gamma_{g\omega}/\Gamma_{gp} = 0.047 - 0.04, \ \Gamma_{g\omega}/\Gamma_{total} = 0.019 - 0.031, \ \Gamma_{g\omega}/\Gamma_{gp} = 0.027 - 0.044 $ $ \omega_{3}(2255) 6.2 - 7.0 $ $ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.27 - 0.36, \ \Gamma_{g\omega}/\Gamma_{gp} = 0.088 - 0.44, \ \Gamma_{gb}/\Gamma_{total} = 0.088 - 0.044, \ \Gamma_{gb}/\Gamma_{gp} = 0.087 - 0.044 $ $ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.045 - 0.48, \ \Gamma_{sh}/\Gamma_{gp} = 0.088 - 0.47, \ \Gamma_{gg}/\Gamma_{total} = 0.043 - 0.052, \ \Gamma_{gg}/\Gamma_{gp} = 0.049 - 0.55 $ $ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.043 - 0.45, \ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.023, \ \Gamma_{g\omega}/\Gamma_{gp} = 0.049 - 0.55 $ $ \Gamma_{g\omega}/\Gamma_{total} = 0.040 - 0.25, \ \Gamma_{gg}/\Gamma_{ftotal} = 0.040 - 0.15, \ \Gamma_{g\omega}/\Gamma_{gp} = 0.033, \ \Gamma_{g\omega}/\Gamma_{gp} = 0.049 - 0.5 $ $ \Gamma_{g\omega}/\Gamma_{total} = 0.020 - 0.25, \ \Gamma_{gg}/\Gamma_{ftotal} = 0.020 - 0.21, \ \Gamma_{gg}/\Gamma_{gp} = 0.049 - 0.5 $ $ \Gamma_{g\omega}/\Gamma_{total} = 0.020 - 0.25, \ \Gamma_{gg}/\Gamma_{ftotal} = 0.020 - 0.21, \ \Gamma_{gg}/\Gamma_{gp} = 0.049 - 0.64, \ \Gamma_{sh}/\Gamma_{gp} = 0.020 - 0.075 $ $ \alpha_{4}(2040) \ 4.0 - 5.8 $ $ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.035 - 0.38, \ \Gamma_{gg}/\Gamma_{ftotal} = 0.14 - 0.15, \ \Gamma_{gg}/\Gamma_{gp} = 0.042 - 0.64, \ \Gamma_{sh}/\Gamma_{gp} = 0.22 - 0.29 $ $ \alpha_{4}(2250) \ 4.0 - 7.0 $ $ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.035 - 0.38, \ \Gamma_{gg}/\Gamma_{ftotal} = 0.14 - 0.23, \ \Gamma_{gg}/\Gamma_{gp} = 0.42 - 0.64, \ \Gamma_{sh}/\Gamma_{gp} = 0.22 - 0.29 $ $ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.015 - 0.19, \ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.14 - 0.23, \ \Gamma_{gg}/\Gamma_{ftotal} = 0.11, \ \Gamma_{gg}/\Gamma_{gp} = 0.22 - 0.29 $ $ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.015 - 0.19, \ \Gamma_{g\omega}/\Gamma_{ftotal} = 0.14 - 0.23, \ \Gamma_{gg}/\Gamma_{ftotal} = 0.$	$a_3(2275)$	4.6 - 5	$\Gamma_{\rho a_1}/\Gamma_{\text{Total}} = 0.066 - 0.077, \Gamma_{\pi \rho}/\Gamma_{\text{Total}} = 0.23 - 0.27, \Gamma_{\pi \rho}/\Gamma_{\rho a_1} = 3.3 - 3.8, \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.075 - 0.099$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\omega_3(1670)$	4.0 - 5.4	$\Gamma_{\pi\rho}/\Gamma_{\text{Total}} = 0.69 - 0.75, \Gamma_{\pi b_1}/\Gamma_{\text{Total}} = 0.2 - 0.26, \Gamma_{\eta\omega}/\Gamma_{\text{Total}} = 0.035 - 0.036,$
$ \Gamma_{gol}/\Gamma_{total} = 0.05 - 0.056, \ \Gamma_{gol}/\Gamma_{gol} = 0.059 - 0.068, \ \Gamma_{gol}/\Gamma_{gol} = 0.6 - 0.69 $ $ \phi_3(1850) 5.3 - 7.0 $ $ \Gamma_{Fer}/\Gamma_{ftotal} = 0.59 - 0.65, \ \Gamma_{KF}/\Gamma_{ftotal} = 0.24 - 0.27, \ \Gamma_{KF}/\Gamma_{Fer}/\Gamma_{Fer} = 0.36 - 0.46 $ $ \omega_3(2285) 4.7 - 5.0 $ $ \Gamma_{gol}/\Gamma_{gol} = 0.083 - 0.092, \ \Gamma_{gol}/\Gamma_{final} = 0.13 - 0.13, \ \Gamma_{sip}/\Gamma_{fotal} = 0.19, \ \Gamma_{gol}/\Gamma_{fotal} = 0.059 - 0.065, $ $ \Gamma_{gol}/\Gamma_{fotal} = 0.27 - 0.70, \ \Gamma_{gol}/\Gamma_{fin} = 0.47 - 0.49, \ \Gamma_{gol}/\Gamma_{fotal} = 0.019 - 0.031, \ \Gamma_{gol}/\Gamma_{gol} = 0.032 - 0.038, $ $ \Gamma_{gol}/\Gamma_{fotal} = 0.27 - 0.36, \ \Gamma_{gol}/\Gamma_{gol} = 0.68 - 0.84, \ \Gamma_{uf/2}/\Gamma_{fotal} = 0.0049 - 0.052, \ \Gamma_{gol}/\Gamma_{gol} = 0.32 - 0.38, $ $ \Gamma_{uf/2}/\Gamma_{gol} = 0.45 - 0.48, \ \Gamma_{sol}/\Gamma_{gol} = 0.33 - 0.47, \ \Gamma_{gol}/\Gamma_{fotal} = 0.043 - 0.052, \ \Gamma_{gol}/\Gamma_{gol} = 0.32 - 0.38, $ $ \Gamma_{uf/2}/\Gamma_{gol} = 0.45 - 0.48, \ \Gamma_{sol}/\Gamma_{gol} = 0.33 - 0.47, \ \Gamma_{gol}/\Gamma_{gol} = 0.043 - 0.052, \ \Gamma_{gol}/\Gamma_{gol} = 0.032 - 0.038, $ $ \Gamma_{uf/2}/\Gamma_{gol} = 0.45 - 0.48, \ \Gamma_{sol}/\Gamma_{gol} = 0.34 - 0.45, \ \Gamma_{sol}/\Gamma_{gol} = 0.042 - 0.052, \ \Gamma_{gol}/\Gamma_{gol} = 0.042 - 0.041, \ \Gamma_{gol}/\Gamma_{gol} = 0.042 - 0.041, \ \Gamma_{gol}/\Gamma_{gol} = 0.042 - 0.044, \ \Gamma_{gol}/\Gamma_{gol} = 0.020 - 0.075, \ \Gamma_{gol}/\Gamma_{gol} = 0.042 - 0.041, \ \Gamma_{gol}/\Gamma_{gol} = 0.042 - 0.044, \ \Gamma_{gol}/\Gamma_{gol} = 0.0$			$\Gamma_{\eta\omega}/\Gamma_{\pi\rho} = 0.046 - 0.051, \Gamma_{\eta\omega}/\Gamma_{\pi b_1} = 0.13 - 0.17, \Gamma_{KK^*}/\Gamma_{Total} = 0.0028 - 0.0032$
$ \begin{aligned} \phi_1(1850) & 5.3 - 7.0 \\ \omega_2(2285) & 4.7 - 5.0 \\ & \Gamma_{\pi\rho}/\Gamma_{Total} = 0.59 - 0.65, \ \Gamma_{KK'}/\Gamma_{Total} = 0.24 - 0.27, \ \Gamma_{KK'}/\Gamma_{K'K'} = 0.36 - 0.46 \\ \omega_3(2285) & 4.7 - 5.0 \\ & \Gamma_{\pi\rho}/\Gamma_{Total} = 0.7 - 0.71, \ \Gamma_{\pi\rho}/\Gamma_{Total} = 0.13 - 0.13, \ \Gamma_{\pi\rho}/\Gamma_{Total} = 0.19 - 0.031, \ \Gamma_{\rho\omega}/\Gamma_{Total} = 0.059 - 0.065, \\ & \Gamma_{\mu\nu}/\Gamma_{\mu\nu} = 0.083 - 0.092, \ \Gamma_{\mu\nu}/\Gamma_{\pi\rho l} = 0.47 - 0.49, \ \Gamma_{\rho\pi l}/\Gamma_{Total} = 0.019 - 0.031, \ \Gamma_{\rho\omega}/\Gamma_{\rho\mu} = 0.027 - 0.044 \\ \omega_3(2255) & 6.2 - 7.0 \\ & \Gamma_{\mu\nu l}/\Gamma_{Total} = 0.27 - 0.36, \ \Gamma_{\rho\nu l}/\Gamma_{\rho\mu} = 0.68 - 0.84, \ \Gamma_{\omega l}/\Gamma_{Total} = 0.088 - 0.14, \ \Gamma_{\omega l}/\Gamma_{\rho\nu} = 0.32 - 0.38, \\ & \Gamma_{\omega l}/\Gamma_{\rho\nu} = 0.45 - 0.48, \ \Gamma_{\sigma l}/\Gamma_{\rho\nu} = 0.33 - 0.47, \ \Gamma_{\kappa\rho}/\Gamma_{Total} = 0.043 - 0.052, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.14 - 0.16 \\ & \Gamma_{\rho\mu}/\Gamma_{Total} = 0.45 - 0.48, \ \Gamma_{\pi\nu}/\Gamma_{Total} = 0.44 - 0.15, \ \Gamma_{\omega\nu}/\Gamma_{Total} = 0.22, \ \Gamma_{\pi\nu}/\Gamma_{\rho\nu} = 0.33, \ \Gamma_{\omega\nu}/\Gamma_{\rho\nu} = 0.39, \ \Gamma_{\omega\nu}/\Gamma_{\rho\nu} = 0.092 - 0.21, \ \Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.42 - 0.64, \ \Gamma_{\kappa\nu}/\Gamma_{\rho\nu} = 0.99 - 0.14, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.29 - 0.3 \\ \alpha_4(2250) & 4.0 - 7.0 & \Gamma_{\rho\nu}/\Gamma_{Total} = 0.15 - 0.19, \ \Gamma_{\rho\nu}/\Gamma_{Total} = 0.14 - 0.23, \ \Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.99 - 0.14, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.29 - 0.29, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.41 - 0.57, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.99 - 0.14, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.99 - 0.14, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.99 - 0.99, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.99 - 0.99, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.15, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.15, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.15, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.15, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.14 - 0.23, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.15, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu} = 0.29 - 0.21, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.29 - 0.21, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.29 - 0.21, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.39 - 0.14, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.39 - 0.14, \ \Gamma_{\kappa\rho}/\Gamma_{\rho\nu}/\Gamma_{\rho\nu} = 0.39 - 0.14, \ \Gamma_{$	$\omega_3(1945)$	5.3 - 7.0	$\Gamma_{\pi\rho}/\Gamma_{\text{Total}} = 0.81 - 0.84, \Gamma_{\pi b_1}/\Gamma_{\text{Total}} = 0.073 - 0.092, \Gamma_{\pi b_1}\Gamma_{\pi\rho} = 0.087 - 0.11,$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			$\Gamma_{\eta\omega}/\Gamma_{\text{Total}} = 0.05 - 0.056, \Gamma_{\eta\omega}/\Gamma_{\pi\rho} = 0.059 - 0.068, \Gamma_{\eta\omega}/\Gamma_{\pi b_1} = 0.6 - 0.69$
$\begin{array}{c} \Gamma_{\rho\rho}/\Gamma_{\pi\rho} = 0.083 - 0.092, \ \Gamma_{\rho\rho}/\Gamma_{\pi\rho_1} = 0.47 - 0.49, \ \Gamma_{\rho\sigma_1}/\Gamma_{Total} = 0.019 - 0.031, \ \Gamma_{\rho\sigma_1}/\Gamma_{\pi\rho_1} = 0.027 - 0.044 \\ \Gamma_{\rho\sigma_1}/\Gamma_{Total} = 0.27 - 0.36, \ \Gamma_{\rho\sigma_2}/\Gamma_{\rho\sigma_1} = 0.68 - 0.84, \ \Gamma_{\nu\rho_2}/\Gamma_{Total} = 0.088 - 0.14, \ \Gamma_{\nu\rho_2}/\Gamma_{\rho\sigma_1} = 0.32 - 0.38, \\ \Gamma_{\nu\rho_2}/\Gamma_{\rho\sigma_2} = 0.45 - 0.48, \ \Gamma_{\pi\rho_1}/\Gamma_{\pi\rho_2} = 0.33 - 0.47, \ \Gamma_{\pi\rho_1/1000}/\Gamma_{Total} = 0.043 - 0.052, \ \Gamma_{\pi\rho_1/1000}/\Gamma_{\rho\sigma_1} = 0.14 - 0.16 \\ \Gamma_{\rho\rho_2}/\Gamma_{Total} = 0.43 - 0.45, \ \Gamma_{\pi\rho_2}/\Gamma_{Total} = 0.22, \ \Gamma_{\pi\rho_2}/\Gamma_{\pi\rho_2} = 0.49 - 0.5 \\ \Gamma_{\nu\rho_2}/\Gamma_{Total} = 0.14 - 0.15, \ \Gamma_{\nu\rho_2}/\Gamma_{Total} = 0.22, \ \Gamma_{\pi\rho_2}/\Gamma_{\pi\rho_2} = 0.49 - 0.5 \\ \Gamma_{\rho\rho_2}/\Gamma_{Total} = 0.020 - 0.25, \ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.092 - 0.21, \ \Gamma_{\rho\rho}/\Gamma_{\pi\rho_2} = 0.77 - 4.3, \ \Gamma_{\pi\rho_1}/\Gamma_{Total} = 0.020 - 0.075 \\ a_4(2040) \ 4.0 - 5.8 \ \Gamma_{\rho\rho_1}/\Gamma_{Total} = 0.36 - 0.38, \ \Gamma_{\pi\rho}/\Gamma_{Total} = 0.16 - 0.23, \ \Gamma_{\pi\rho}/\Gamma_{\rho\nu} = 0.42 - 0.64, \ \Gamma_{\pi\rho_1}/\Gamma_{Total} = 0.22, \\ \Gamma_{\pi\rho_1}/\Gamma_{\rho\nu} = 0.59 - 0.61, \ \Gamma_{\pi\rho}/\Gamma_{\pi\rho_2} = 0.99 - 0.14, \ \Gamma_{\pi\rho_2}/\Gamma_{Total} = 0.11, \ \Gamma_{\pi\rho}/\Gamma_{\rho\nu} = 0.29 - 0.3 \\ a_4(2255) \ 4.7 - 4.8 \ \Gamma_{\pi\rho_2}/\Gamma_{Total} = 0.15 - 0.19, \ \Gamma_{\rho\rho_2}/\Gamma_{Total} = 0.14 - 0.23, \ \Gamma_{\rho\rho_1}/\Gamma_{Total} = 0.12 - 0.14, \ \Gamma_{\pi\rho_1}/\Gamma_{\pi\rho_2} = 0.09 - 0.14, \ \Gamma_{\pi\rho_1}/\Gamma_{\pi\rho_1} = 0.22 - 0.29 \\ \pi_{2}(2250) \ 4.0 - 7.0 \ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.15 - 0.19, \ \Gamma_{\rho\rho}/\Gamma_{\rho\tau_2} = 0.78 - 0.82, \ \Gamma_{\rho\sigma_1}/\Gamma_{\rho\sigma_1} = 0.9 - 1.3, \ \Gamma_{\pi\rho_1}/\Gamma_{\rho\sigma_2} = 0.62 - 0.92, \\ \Gamma_{\rho\rho_1}/\Gamma_{Total} = 0.23 - 0.35, \ \Gamma_{\rho\rho}/\Gamma_{\rho\tau_0} = 0.23 - 0.25, \ \Gamma_{\pi\rho_1}/\Gamma_{\rho\rho_1} = 0.9 - 1.3, \ \Gamma_{\pi\rho_1}/\Gamma_{\rho\sigma_2} = 0.61 - 0.72, \\ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.23 - 0.35, \ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.14 - 0.41, \ \Gamma_{\nu\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho} = 0.45 - 0.74, \ \Gamma_{\pi\rho_1}/\Gamma_{\rho\rho} = 0.46 - 0.72, \\ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.23 - 0.35, \ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.19 - 0.27, \ \Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho} = 0.49 - 0.12, \\ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.29 - 0.21, \ \Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho} = 0.89, \ \Gamma_{\rho\rho}/\Gamma_{\rho\rho} = 0.49 - 0.12, \\ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.29 - 0.35, \ \Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{\rho\rho}/\Gamma_{$	$\phi_3(1850)$	5.3 - 7.0	$\Gamma_{K^*K^*}/\Gamma_{\text{Total}} = 0.59 - 0.65, \ \Gamma_{KK^*}/\Gamma_{\text{Total}} = 0.24 - 0.27, \ \Gamma_{KK^*}/\Gamma_{K^*K^*} = 0.36 - 0.46$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\omega_{3}(2285)$	4.7 - 5.0	$\Gamma_{\pi\rho}/\Gamma_{\text{Total}} = 0.7 - 0.71, \Gamma_{\pi b_1}\Gamma_{\text{Total}} = 0.13 - 0.13, \Gamma_{\pi b_1}/\Gamma_{\pi\rho} = 0.18 - 0.19, \Gamma_{\eta\omega}/\Gamma_{\text{Total}} = 0.059 - 0.065,$
$ \Gamma_{\omega f_2} / \Gamma_{\rho \omega_2} = 0.45 - 0.48, \Gamma_{\pi b_1} / \Gamma_{\pi p} = 0.33 - 0.47, \Gamma_{\pi \rho_1 / 1700} / \Gamma_{Total} = 0.043 - 0.052, \Gamma_{\pi \rho_1 / 1700} / \Gamma_{\rho \omega_1} = 0.14 - 0.16 $ $ \Gamma_{\rho \rho} / \Gamma_{Total} = 0.43 - 0.45, \Gamma_{\pi \omega_2} / \Gamma_{Total} = 0.22, \Gamma_{\pi \omega_2} / \Gamma_{\rho \rho} = 0.49 - 0.5 $ $ \Gamma_{\omega \omega} / \Gamma_{Total} = 0.14 - 0.15, \Gamma_{\omega \omega} / \Gamma_{\rho \rho} = 0.33, \Gamma_{\omega \omega} / \Gamma_{\pi \omega_2} = 0.66 $ $ \Gamma_{\pi \omega_2} / \Gamma_{Total} = 0.020 - 0.25, \Gamma_{\rho \rho} / \Gamma_{Total} = 0.092 - 0.21, \Gamma_{\rho \rho} / \Gamma_{\pi \omega_2} = 0.77 - 4.3, \Gamma_{\pi \omega_1} / \Gamma_{Total} = 0.020 - 0.075 $ $ a_d (2040) 4.0 - 5.8 \qquad \Gamma_{\rho \omega} / \Gamma_{Total} = 0.36 - 0.38, \Gamma_{\pi \rho} / \Gamma_{Total} = 0.16 - 0.23, \Gamma_{\pi \rho} / \Gamma_{\pi \omega_2} = 0.42 - 0.64, \Gamma_{\pi h_1} / \Gamma_{Total} = 0.22, $ $ \Gamma_{\pi h_1} / \Gamma_{\rho \omega} = 0.59 - 0.61, \Gamma_{\pi h_1} / \Gamma_{\pi \rho_1} = 0.96 - 1.4, \Gamma_{\pi h_1} / \Gamma_{\pi \rho_1} = 0.41 - 0.57, \Gamma_{\pi h_1} / \Gamma_{\pi h_2} = 0.092 - 0.14, \Gamma_{\pi h_1} / \Gamma_{\pi \rho_2} = 0.22 - 0.29 $ $ \pi_d (2250) 4.0 - 7.0 \qquad \Gamma_{\rho \omega} / \Gamma_{Total} = 0.15 - 0.19, \Gamma_{\rho \omega_2} / \Gamma_{Total} = 0.14 - 0.23, \Gamma_{\rho h_1} / \Gamma_{Total} = 0.12 - 0.15, \Gamma_{\rho h_1} / \Gamma_{\rho \omega_2} = 0.66 - 0.92, $ $ \Gamma_{\rho h_1} / \Gamma_{\rho \omega_2} = 0.64 - 0.87, \Gamma_{\rho \mu_1} / \Gamma_{\rho \mu_2} = 0.78 - 0.82, \Gamma_{\rho \omega_1} / \Gamma_{\rho h_1} = 0.9 - 1.3, \Gamma_{\pi h_1} / \Gamma_{\rho \omega} = 0.62 - 0.92, $ $ \Gamma_{\rho h_1} / \Gamma_{\rho \omega_2} = 0.64 - 0.87, \Gamma_{\rho \mu_1} / \Gamma_{\rho \mu_2} = 0.78 - 0.82, \Gamma_{\rho \omega_1} / \Gamma_{\rho h_1} = 0.9 - 1.3, \Gamma_{\pi h_1} / \Gamma_{\rho \omega_2} = 0.66 - 0.72, $ $ \Gamma_{\rho h_1} / \Gamma_{Total} = 0.023 - 0.35, \Gamma_{\rho \rho} / \Gamma_{Total} = 0.23 - 0.25, \Gamma_{\pi \omega_1} / \Gamma_{\rho \rho} = 0.39 - 0.61, \Gamma_{\sigma \omega_1} / \Gamma_{\tau h_2} = 0.61 - 0.72, $ $ \Gamma_{\omega h_1} / \Gamma_{\tau total} = 0.093 - 0.14, \Gamma_{\omega h_1} / \Gamma_{\rho h_1} = 0.4 - 0.41, \Gamma_{\omega h_1} / \Gamma_{\rho \rho} = 0.39 - 0.61, \Gamma_{\omega \omega_1} / \Gamma_{\tau total} = 0.094 - 0.12, $ $ \Gamma_{\rho \mu_1} / \Gamma_{\tau total} = 0.2 - 0.21, \Gamma_{\rho h_1} / \Gamma_{\tau total} = 0.19 - 0.27, \Gamma_{\rho h_1} / \Gamma_{\rho \rho} = 0.92 - 1.3, \Gamma_{\pi \mu_1} / \Gamma_{\tau total} = 0.094 - 0.12, $ $ \Gamma_{\mu \mu_1} / \Gamma_{\tau total} = 0.2 - 0.36, \Gamma_{\mu \mu_2} / \Gamma_{\tau total} = 0.19 - 0.27, \Gamma_{\rho h_1} / \Gamma_{\rho total} = 0.088 - 0.14, \Gamma_{\omega h_2} / \Gamma_{\rho h_1} = 0.35 - 0.58, $ $ \Gamma_{\omega h_2} / \Gamma_{\tau t$			$\Gamma_{\eta\omega}/\Gamma_{\pi\rho} = 0.083 - 0.092, \Gamma_{\eta\omega}/\Gamma_{\pi b_1} = 0.47 - 0.49, \Gamma_{\rho a_1}/\Gamma_{\text{Total}} = 0.019 - 0.031, \Gamma_{\rho a_1}/\Gamma_{\pi\rho} = 0.027 - 0.044$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\omega_{3}(2255)$	6.2 - 7.0	$\Gamma_{\rho a_1}/\Gamma_{\text{Total}} = 0.27 - 0.36, \Gamma_{\rho a_2}/\Gamma_{\rho a_1} = 0.68 - 0.84, \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.088 - 0.14, \Gamma_{\omega f_2}/\Gamma_{\rho a_1} = 0.32 - 0.38,$
$ \Gamma_{\omega\omega}/\Gamma_{\text{Total}} = 0.14 - 0.15, \ \Gamma_{\omega\omega}/\Gamma_{\rho\rho} = 0.33, \ \Gamma_{\omega\omega}/\Gamma_{\pi\alpha_2} = 0.66 $ $ f_4(2300) \ 4.0 - 7.0 \ \Gamma_{\pi\alpha_2}/\Gamma_{\text{Total}} = 0.020 - 0.25, \ \Gamma_{\rho\rho}/\Gamma_{\text{Total}} = 0.092 - 0.21, \ \Gamma_{\rho\rho}/\Gamma_{\pi\alpha_2} = 0.77 - 4.3, \ \Gamma_{\pi\alpha_1}/\Gamma_{\text{Total}} = 0.020 - 0.075 $ $ a_4(2040) \ 4.0 - 5.8 \ \Gamma_{\rho\omega}/\Gamma_{\text{Total}} = 0.36 - 0.38, \ \Gamma_{\pi\rho}/\Gamma_{\text{Total}} = 0.16 - 0.23, \ \Gamma_{\pi\rho}/\Gamma_{\rho\omega} = 0.42 - 0.64, \ \Gamma_{\pi h_1}/\Gamma_{\text{Total}} = 0.22, $ $ \Gamma_{\pi h_1}/\Gamma_{\rho\omega} = 0.59 - 0.61, \ \Gamma_{\pi h_1}/\Gamma_{\pi \rho} = 0.96 - 1.4, \ \Gamma_{\pi f_2}/\Gamma_{\text{Total}} = 0.11, \ \Gamma_{\pi f_2}/\Gamma_{\rho\omega} = 0.29 - 0.3 $ $ a_4(2255) \ 4.7 - 4.8 \ \Gamma_{\pi f_2}/\Gamma_{\pi h_1} = 0.41 - 0.57, \ \Gamma_{\pi f_1}/\Gamma_{\pi f_2} = 0.092 - 0.14, \ \Gamma_{\pi f_1}/\Gamma_{\pi g_1} = 0.22 - 0.29 $ $ \pi_4(2250) \ 4.0 - 7.0 \ \Gamma_{\rho\omega}/\Gamma_{\text{Total}} = 0.15 - 0.19, \ \Gamma_{\rho\alpha_2}/\Gamma_{\text{Total}} = 0.14 - 0.23, \ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.12 - 0.15, \ \Gamma_{\rho h_1}/\Gamma_{\rho\omega} = 0.62 - 0.92, $ $ \Gamma_{\rho h_1}/\Gamma_{\rho \alpha_2} = 0.64 - 0.87, \ \Gamma_{\rho \alpha_1}/\Gamma_{\rho \alpha_2} = 0.78 - 0.82, \ \Gamma_{\rho \alpha_1}/\Gamma_{\rho h_1} = 0.9 - 1.3, \ \Gamma_{\pi f_2}/\Gamma_{\pi \rho} = 0.8 - 1.3 $ $ \eta_4(2330) \ 4.0 - 7.0 \ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.093 - 0.14, \ \Gamma_{\omega h_1}/\Gamma_{\rho h_2} = 0.4 - 0.41, \ \Gamma_{\omega h_1}/\Gamma_{\rho \rho} = 0.39 - 0.61, \ \Gamma_{\omega \omega}/\Gamma_{\text{Total}} = 0.075 - 0.079 $ $ \rho_4(2230) \ 6.8 - 7.0 \ \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.22 - 0.21, \ \Gamma_{\rho h_1}/\Gamma_{\rho h_1} = 0.4 - 0.41, \ \Gamma_{\omega h_1}/\Gamma_{\rho \rho} = 0.39 - 0.61, \ \Gamma_{\omega \omega}/\Gamma_{\text{Total}} = 0.094 - 0.12, $ $ \Gamma_{\mu \alpha_1}/\Gamma_{\rho \rho} = 0.46 - 0.60, \ \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.19 - 0.27, \ \Gamma_{\rho h_1}/\Gamma_{\rho \rho} = 0.92 - 1.3, \ \Gamma_{\pi \alpha_1}/\Gamma_{\text{Total}} = 0.094 - 0.12, $ $ \Gamma_{\mu \alpha_1}/\Gamma_{\rho \rho} = 0.46 - 0.60, \ \Gamma_{\rho \rho}/\Gamma_{\rho h_1} = 0.3 - 0.39, \ \Gamma_{\omega \alpha_1}/\Gamma_{\rho h_1} = 0.29 - 0.33 $ $ \omega_4(2250) \ 4.0 - 7.0 \ \Gamma_{\rho \alpha_1}/\Gamma_{\text{Total}} = 0.27 - 0.36, \ \Gamma_{\rho \alpha_2}/\Gamma_{\rho \mu_1} = 0.68 - 0.84, \ \Gamma_{\nu \rho}/\Gamma_{\text{Total}} = 0.088 - 0.14, \ \Gamma_{\omega \rho}/\Gamma_{\rho \mu_1} = 0.32 - 0.38, $ $ \Gamma_{\omega \beta_1}/\Gamma_{\rho \alpha_2} = 0.45 - 0.48, \ \Gamma_{\pi h_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \ \Gamma_{\pi \rho}/\Gamma_{\text{Total}} = 0.088 - 0.14, \ \Gamma_{\omega \rho}/\Gamma_{\rho \mu_1} = 0.32 - 0.38, $ $ \Gamma_{\omega \beta_1}/\Gamma_{\rho \alpha_2} = 0.45 - 0.48, \ \Gamma_{\pi h_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \ \Gamma_{\pi \rho}/\Gamma_{\pi \rho}/\Gamma_{$			$\Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.45 - 0.48, \Gamma_{\pi b_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \Gamma_{\pi \rho (1700)}/\Gamma_{Total} = 0.043 - 0.052, \Gamma_{\pi \rho (1700)}/\Gamma_{\rho a_1} = 0.14 - 0.16$
$ f_4(2300) 4.0 - 7.0 \qquad \Gamma_{\pi \sigma_2}/\Gamma_{\text{Total}} = 0.020 - 0.25, \Gamma_{\rho\rho}/\Gamma_{\text{Total}} = 0.092 - 0.21, \Gamma_{\rho\rho}/\Gamma_{\pi \sigma_2} = 0.77 - 4.3, \Gamma_{\pi \sigma_1}/\Gamma_{\text{Total}} = 0.020 - 0.075 \\ a_4(2040) 4.0 - 5.8 \qquad \Gamma_{\rho\nu}/\Gamma_{\text{Total}} = 0.36 - 0.38, \Gamma_{\pi\rho}/\Gamma_{\text{Total}} = 0.16 - 0.23, \Gamma_{\pi\rho}/\Gamma_{\rho\omega} = 0.42 - 0.64, \Gamma_{\pi h_1}/\Gamma_{\text{Total}} = 0.22, \\ \Gamma_{\pi h_1}/\Gamma_{\rho\omega} = 0.59 - 0.61, \Gamma_{\pi h_1}/\Gamma_{\pi \rho} = 0.96 - 1.4, \Gamma_{\pi f_2}/\Gamma_{\text{Total}} = 0.11, \Gamma_{\pi f_2}/\Gamma_{\rho\omega} = 0.29 - 0.3 \\ a_4(2255) 4.7 - 4.8 \qquad \Gamma_{\pi f_2}/\Gamma_{\pi h_1} = 0.41 - 0.57, \Gamma_{\pi f_1}/\Gamma_{\pi f_2} = 0.092 - 0.14, \Gamma_{\pi \eta_1}/\Gamma_{\pi \eta} = 0.22 - 0.29 \\ \pi_4(2250) 4.0 - 7.0 \qquad \Gamma_{\rho\omega}/\Gamma_{\text{Total}} = 0.15 - 0.19, \Gamma_{\rho\sigma_1}/\Gamma_{\text{Total}} = 0.14 - 0.23, \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.12 - 0.15, \Gamma_{\rho h_1}/\Gamma_{\rho\omega} = 0.62 - 0.92, \\ \Gamma_{\rho h_1}/\Gamma_{\rho\omega_2} = 0.64 - 0.87, \Gamma_{\rho\sigma_1}/\Gamma_{\rho\omega_2} = 0.78 - 0.82, \Gamma_{\rho\sigma_1}/\Gamma_{\rho\mu_1} = 0.91 - 1.3, \Gamma_{\pi f_2}/\Gamma_{\rho\omega} = 0.8 - 1.3 \\ \eta_4(2330) 4.0 - 7.0 \qquad \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.23 - 0.35, \Gamma_{\rho\rho_1}/\Gamma_{\text{Total}} = 0.23 - 0.25, \Gamma_{\pi \sigma_2}/\Gamma_{\rho\rho} = 0.45 - 0.74, \Gamma_{\pi \sigma_1}/\Gamma_{\pi \sigma_2} = 0.61 - 0.72, \\ \Gamma_{\omega h_1}/\Gamma_{\text{Total}} = 0.093 - 0.14, \Gamma_{\omega h_1}/\Gamma_{\rho h_1} = 0.40 - 0.41, \Gamma_{\omega h_1}/\Gamma_{\rho\rho} = 0.39 - 0.61, \Gamma_{\omega\omega}/\Gamma_{\text{Total}} = 0.075 - 0.079 \\ \rho_4(2230) 6.8 - 7.0 \qquad \Gamma_{\rho\rho}/\Gamma_{\text{Total}} = 0.2 - 0.21, \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.19 - 0.27, \Gamma_{\rho h_1}/\Gamma_{\rho\rho} = 0.39 - 0.61, \Gamma_{\omega\omega}/\Gamma_{\text{Total}} = 0.094 - 0.12, \\ \Gamma_{\pi \sigma_1}/\Gamma_{\rho\omega} = 0.45 - 0.48, \Gamma_{\pi h_1}/\Gamma_{\rho\omega} = 0.33 - 0.47, \Gamma_{\pi \rho(1700)}/\Gamma_{\text{Total}} = 0.088 - 0.14, \Gamma_{\omega f_2}/\Gamma_{\rho\sigma_1} = 0.32 - 0.38, \\ \Gamma_{\omega f_2}/\Gamma_{\rho\omega_2} = 0.45 - 0.48, \Gamma_{\pi h_1}/\Gamma_{\pi\rho} = 0.33 - 0.47, \Gamma_{\pi \rho(1700)}/\Gamma_{\text{Total}} = 0.043 - 0.052, \Gamma_{\pi \rho(1700)}/\Gamma_{\rho\sigma_1} = 0.14 - 0.16 \\ \omega_5(22250) 4.0 - 7.0 \qquad \Gamma_{\rho\omega_1}/\Gamma_{\text{Total}} = 0.20 - 0.21, \Gamma_{\omega\sigma_2}/\Gamma_{\tauotal} = 0.19 - 0.23, \Gamma_{\omega f_2}/\Gamma_{\rho\omega_2} = 0.4 - 0.45, \Gamma_{\pi \rho}/\Gamma_{\pi h_1} = 0.35 - 0.58 \\ \rho_5(2350) 4.0 - 7.0 \qquad \Gamma_{\rho\mu_1}/\Gamma_{\text{Total}} = 0.20 - 0.21, \Gamma_{\omega\mu_2}/\Gamma_{\text{Total}} = 0.17 - 0.24, \Gamma_{\omega\omega_2}/\Gamma_{\rho\omega_2} = 0.46 - 0.78, \Gamma_{\rho\mu}/\Gamma_{\rho h_1} = 0.3$	$f_4(2050)$	4.0 -7.0	$\Gamma_{\rho\rho}/\Gamma_{\text{Total}} = 0.43 - 0.45, \Gamma_{\pi a_2}/\Gamma_{\text{Total}} = 0.22, \Gamma_{\pi a_2}/\Gamma_{\rho\rho} = 0.49 - 0.5$
$\begin{array}{c} a_4(2040) 4.0 - 5.8 \Gamma_{\rho\omega}/\Gamma_{\text{Total}} = 0.36 - 0.38, \; \Gamma_{\pi\rho}/\Gamma_{\text{Total}} = 0.16 - 0.23, \; \Gamma_{\pi\rho}/\Gamma_{\rho\omega} = 0.42 - 0.64, \; \Gamma_{\pi b_1}/\Gamma_{\text{Total}} = 0.22, \\ \Gamma_{\pi b_1}/\Gamma_{\rho\omega} = 0.59 - 0.61, \; \Gamma_{\pi b_1}/\Gamma_{\pi p} = 0.96 - 1.4, \; \Gamma_{\pi f_2}/\Gamma_{\text{Total}} = 0.11, \; \Gamma_{\pi f_2}/\Gamma_{\rho\omega} = 0.29 - 0.3 \\ a_4(2255) 4.7 - 4.8 \Gamma_{\pi f_2}/\Gamma_{\pi b_1} = 0.41 - 0.57, \; \Gamma_{\pi f_1}/\Gamma_{\pi f_2} = 0.092 - 0.14, \; \Gamma_{\pi \eta^*}/\Gamma_{\pi \eta} = 0.22 - 0.29 \\ \pi_4(2250) 4.0 - 7.0 \Gamma_{\rho\omega}/\Gamma_{\text{Total}} = 0.15 - 0.19, \; \Gamma_{\rho\omega_2}/\Gamma_{\text{Total}} = 0.14 - 0.23, \; \Gamma_{\rho\mu_1}/\Gamma_{\text{Total}} = 0.12 - 0.15, \; \Gamma_{\rho h_1}/\Gamma_{\rho\omega} = 0.62 - 0.92, \\ \Gamma_{\rho h_1}/\Gamma_{\rho\omega_2} = 0.64 - 0.87, \; \Gamma_{\rho\alpha_1}/\Gamma_{\rho\alpha_2} = 0.78 - 0.82, \; \Gamma_{\rho\alpha_1}/\Gamma_{\rho h_1} = 0.9 - 1.3, \; \Gamma_{\pi f_2}/\Gamma_{\pi\rho} = 0.8 - 1.3 \\ \eta_4(2330) 4.0 - 7.0 \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.23 - 0.35, \; \Gamma_{\rho\rho}/\Gamma_{\text{Total}} = 0.23 - 0.25, \; \Gamma_{\pi\alpha_2}/\Gamma_{\rho\rho} = 0.45 - 0.74, \; \Gamma_{\pi\alpha_1}/\Gamma_{\pi\alpha_2} = 0.61 - 0.72, \\ \Gamma_{\omega h_1}/\Gamma_{\text{Total}} = 0.093 - 0.14, \; \Gamma_{\omega h_1}/\Gamma_{\rho h_1} = 0.4 - 0.41, \; \Gamma_{\omega h_1}/\Gamma_{\rho\rho} = 0.39 - 0.61, \; \Gamma_{\omega\omega}/\Gamma_{\text{Total}} = 0.075 - 0.079 \\ \rho_4(2230) 6.8 - 7.0 \Gamma_{\rho\rho}/\Gamma_{\text{Total}} = 0.2 - 0.21, \; \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.19 - 0.27, \; \Gamma_{\rho h_1}/\Gamma_{\rho\rho} = 0.92 - 1.3, \; \Gamma_{\pi\alpha_1}/\Gamma_{\text{Total}} = 0.094 - 0.12, \\ \Gamma_{\pi\alpha_1}/\Gamma_{\rho\omega} = 0.46 - 0.60, \; \Gamma_{\rho\beta_2}/\Gamma_{\rho h_1} = 0.3 - 0.39, \; \Gamma_{\omega\alpha_1}/\Gamma_{\rho h_1} = 0.29 - 0.33 \\ \omega_4(2250) 4.0 - 7.0 \Gamma_{\rho\alpha_1}/\Gamma_{\text{Total}} = 0.27 - 0.36, \; \Gamma_{\rho\alpha_2}/\Gamma_{\rho\alpha_1} = 0.68 - 0.84, \; \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.088 - 0.14, \; \Gamma_{\omega f_2}/\Gamma_{\rho\alpha_1} = 0.32 - 0.38, \\ \Gamma_{\omega f_2}/\Gamma_{\rho\omega_2} = 0.45 - 0.48, \; \Gamma_{\pi h_1}/\Gamma_{\pi\rho} = 0.33 - 0.47, \; \Gamma_{\pi \rho(1700)}/\Gamma_{\text{Total}} = 0.043 - 0.052, \; \Gamma_{\pi \rho(1700)}/\Gamma_{\rho\alpha_1} = 0.14 - 0.16 \\ \omega_5(22250) 4.0 - 7.0 \Gamma_{\rho\alpha_2}/\Gamma_{\text{Total}} = 0.42 - 0.58, \; \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.19 - 0.23, \; \Gamma_{\omega f_2}/\Gamma_{\rho\alpha_2} = 0.4 - 0.45, \; \Gamma_{\pi \rho}/\Gamma_{\pi h_1} = 0.35 - 0.58 \\ \rho_5(2350) 4.0 - 7.0 \Gamma_{\rho\alpha_2}/\Gamma_{\text{Total}} = 0.32 - 0.21, \; \Gamma_{\omega\alpha_2}/\Gamma_{\text{Total}} = 0.19 - 0.23, \; \Gamma_{\omega\beta_2}/\Gamma_{\rho\alpha_2} = 0.4 - 0.45, \; \Gamma_{\rho\omega}/\Gamma_{\pi h_1} = 0.35 - 0.58 \\ \rho_5(2350) 4.0 - 7.0 \Gamma_{\rho\alpha_2}/\Gamma_{$			$\Gamma_{\omega\omega}/\Gamma_{\text{Total}} = 0.14 - 0.15, \Gamma_{\omega\omega}/\Gamma_{\rho\rho} = 0.33, \Gamma_{\omega\omega}/\Gamma_{\pi a_2} = 0.66$
$\Gamma_{nb_1}/\Gamma_{\rho\omega} = 0.59 - 0.61, \ \Gamma_{nb_1}/\Gamma_{\pi\rho} = 0.96 - 1.4, \ \Gamma_{nf_2}/\Gamma_{Total} = 0.11, \ \Gamma_{nf_2}/\Gamma_{\rho\omega} = 0.29 - 0.3$ $a_4(2255) 4.7 - 4.8 \qquad \Gamma_{nf_2}/\Gamma_{nb_1} = 0.41 - 0.57, \ \Gamma_{nf_1}/\Gamma_{nf_2} = 0.092 - 0.14, \ \Gamma_{n\eta}/\Gamma_{n\eta} = 0.22 - 0.29$ $\pi_4(2250) 4.0 - 7.0 \qquad \Gamma_{\rho\omega}/\Gamma_{Total} = 0.15 - 0.19, \ \Gamma_{\rho\alpha}/\Gamma_{Total} = 0.14 - 0.23, \ \Gamma_{\rho h_1}/\Gamma_{\rho tal} = 0.12 - 0.15, \ \Gamma_{\rho h_1}/\Gamma_{\rho\omega} = 0.62 - 0.92, \ \Gamma_{\rho h_1}/\Gamma_{\rho\alpha_2} = 0.64 - 0.87, \ \Gamma_{\rho\alpha}/\Gamma_{Total} = 0.23 - 0.82, \ \Gamma_{\rho\alpha_1}/\Gamma_{\rho\mu} = 0.9 - 1.3, \ \Gamma_{nf_2}/\Gamma_{\pi\rho} = 0.8 - 1.3$ $\eta_4(2330) 4.0 - 7.0 \qquad \Gamma_{\rho h_1}/\Gamma_{Total} = 0.23 - 0.35, \ \Gamma_{\rho\rho}/\Gamma_{Total} = 0.23 - 0.25, \ \Gamma_{\pi\alpha_2}/\Gamma_{\rho\rho} = 0.45 - 0.74, \ \Gamma_{\pi a_1}/\Gamma_{\pi\alpha_2} = 0.61 - 0.72, \ \Gamma_{\omega h_1}/\Gamma_{Total} = 0.093 - 0.14, \ \Gamma_{\omega h_1}/\Gamma_{\rho h_1} = 0.4 - 0.41, \ \Gamma_{\omega h_1}/\Gamma_{\rho\rho} = 0.39 - 0.61, \ \Gamma_{\omega\omega}/\Gamma_{Total} = 0.075 - 0.079$ $\rho_4(2230) 6.8 - 7.0 \qquad \Gamma_{\rho\rho}/\Gamma_{Total} = 0.2 - 0.21, \ \Gamma_{\rho h_1}/\Gamma_{Total} = 0.19 - 0.27, \ \Gamma_{\rho h_1}/\Gamma_{\rho\rho} = 0.92 - 1.3, \ \Gamma_{\pi a_1}/\Gamma_{Total} = 0.094 - 0.12, \ \Gamma_{\pi a_1}/\Gamma_{\rho\rho} = 0.46 - 0.60, \ \Gamma_{\rho f_2}/\Gamma_{\rho h_1} = 0.3 - 0.39, \ \Gamma_{\omega a_1}/\Gamma_{\rho h_1} = 0.29 - 0.33$ $\omega_4(2250) 4.0 - 7.0 \qquad \Gamma_{\rho\alpha_1}/\Gamma_{Total} = 0.27 - 0.36, \ \Gamma_{\rho\alpha_2}/\Gamma_{\rho\alpha_1} = 0.68 - 0.84, \ \Gamma_{\omega f_2}/\Gamma_{Total} = 0.088 - 0.14, \ \Gamma_{\omega f_2}/\Gamma_{\rho\alpha_1} = 0.32 - 0.38, \ \Gamma_{\omega f_2}/\Gamma_{\rho\alpha_2} = 0.45 - 0.48, \ \Gamma_{\pi h_1}/\Gamma_{\pi h_2} = 0.33 - 0.47, \ \Gamma_{\pi \rho(1700)}/\Gamma_{Total} = 0.043 - 0.052, \ \Gamma_{\pi \rho(1700)}/\Gamma_{\rho\alpha_1} = 0.14 - 0.16$ $\omega_5(22250) 4.0 - 7.0 \qquad \Gamma_{\rho\alpha_2}/\Gamma_{Total} = 0.42 - 0.58, \ \Gamma_{\omega f_2}/\Gamma_{Total} = 0.19 - 0.23, \ \Gamma_{\omega f_2}/\Gamma_{\rho\alpha_2} = 0.4 - 0.45, \ \Gamma_{\pi \rho}/\Gamma_{\pi h_1} = 0.35 - 0.57, \ \Gamma_{\eta h_1}/\Gamma_{\pi h_1} = 0.1 - 0.12, \ \Gamma_{\eta \omega}/\Gamma_{\pi h_1} = 0.042 - 0.58, \ \Gamma_{\pi \omega_2}/\Gamma_{\rho\rho} = 0.10 - 0.12, \ \Gamma_{\eta \omega}/\Gamma_{\eta h_1} = 0.35 - 0.58$ $\rho_5(2350) 4.0 - 7.0 \qquad \Gamma_{\rho f_2}/\Gamma_{Total} = 0.20 - 0.21, \ \Gamma_{\omega \alpha_2}/\Gamma_{Total} = 0.17 - 0.24, \ \Gamma_{\omega \alpha_2}/\Gamma_{\rho f_2} = 0.86 - 1, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.35 - 0.58$ $\rho_5(2350) 4.0 - 7.0 \qquad \Gamma_{\rho f_2}/\Gamma_{Total} = 0.20 - 0.21, \ \Gamma_{\omega \alpha_2}/\Gamma_{Total} = 0.17 - 0.24, \ \Gamma_{\omega \alpha_2}/\Gamma_{\rho f_2} = 0.86$	$f_4(2300)$	4.0 - 7.0	$\Gamma_{\pi a_2}/\Gamma_{Total} = 0.020 - 0.25, \Gamma_{\rho\rho}/\Gamma_{Total} = 0.092 - 0.21, \Gamma_{\rho\rho}/\Gamma_{\pi a_2} = 0.77 - 4.3, \Gamma_{\pi a_1}/\Gamma_{Total} = 0.020 - 0.075$
$\begin{array}{c} a_4(2255) 4.7 - 4.8 & \Gamma_{\pi f_2}/\Gamma_{\pi b_1} = 0.41 - 0.57, \ \Gamma_{\pi f_1}/\Gamma_{\pi f_2} = 0.092 - 0.14, \ \Gamma_{\pi \eta'}/\Gamma_{\pi \eta} = 0.22 - 0.29 \\ \pi_4(2250) 4.0 - 7.0 & \Gamma_{\rho \omega}/\Gamma_{Total} = 0.15 - 0.19. \ \Gamma_{\rho \omega}/\Gamma_{Total} = 0.14 - 0.23, \ \Gamma_{\rho h_1}/\Gamma_{Total} = 0.12 - 0.15, \ \Gamma_{\rho h_1}/\Gamma_{\rho \omega} = 0.62 - 0.92, \\ \Gamma_{\rho h_1}/\Gamma_{\rho \omega} = 0.64 - 0.87, \ \Gamma_{\rho \omega}/\Gamma_{Total} = 0.23 - 0.82, \ \Gamma_{\rho \omega_1}/\Gamma_{\rho h_1} = 0.9 - 1.3, \ \Gamma_{\pi f_2}/\Gamma_{\pi \rho} = 0.8 - 1.3 \\ \eta_4(2330) 4.0 - 7.0 & \Gamma_{\rho h_1}/\Gamma_{Total} = 0.23 - 0.35, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.23 - 0.25, \ \Gamma_{\pi \omega_2}/\Gamma_{\rho \rho} = 0.45 - 0.74, \ \Gamma_{\pi \alpha_1}/\Gamma_{\pi \alpha_2} = 0.61 - 0.72, \\ \Gamma_{\omega h_1}/\Gamma_{Total} = 0.093 - 0.14, \ \Gamma_{\omega h_1}/\Gamma_{\rho b_1} = 0.4 - 0.41, \ \Gamma_{\omega h_1}/\Gamma_{\rho \rho} = 0.39 - 0.61, \ \Gamma_{\omega \omega}/\Gamma_{Total} = 0.075 - 0.079 \\ \rho_4(2230) 6.8 - 7.0 & \Gamma_{\rho \rho}/\Gamma_{Total} = 0.2 - 0.21, \ \Gamma_{\rho h_1}/\Gamma_{Total} = 0.19 - 0.27, \ \Gamma_{\rho h_1}/\Gamma_{\rho \rho} = 0.92 - 1.3, \ \Gamma_{\pi \alpha_1}/\Gamma_{Total} = 0.094 - 0.12, \\ \Gamma_{\pi \alpha_1}/\Gamma_{\rho \rho} = 0.46 - 0.60, \ \Gamma_{\rho f_2}/\Gamma_{\rho h_1} = 0.3 - 0.39, \ \Gamma_{\omega \alpha_1}/\Gamma_{\rho h_1} = 0.29 - 0.33 \\ \omega_4(2250) 4.0 - 7.0 & \Gamma_{\rho \alpha_1}/\Gamma_{Total} = 0.27 - 0.36, \ \Gamma_{\rho \alpha_2}/\Gamma_{\rho \alpha_1} = 0.68 - 0.84, \ \Gamma_{\omega f_2}/\Gamma_{Total} = 0.088 - 0.14, \ \Gamma_{\omega f_2}/\Gamma_{\rho \alpha_1} = 0.32 - 0.38, \\ \Gamma_{\omega f_2}/\Gamma_{\rho \alpha_2} = 0.45 - 0.48, \ \Gamma_{\pi h_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \ \Gamma_{\pi \rho/17000}/\Gamma_{Total} = 0.043 - 0.052, \ \Gamma_{\pi \rho/17000}/\Gamma_{\rho \alpha_1} = 0.14 - 0.16 \\ \omega_5(22250) 4.0 - 7.0 & \Gamma_{\rho \alpha_2}/\Gamma_{Total} = 0.12 - 0.58, \ \Gamma_{\omega f_2}/\Gamma_{Total} = 0.19 - 0.23, \ \Gamma_{\omega f_2}/\Gamma_{\rho \sigma_2} = 0.4 - 0.45, \ \Gamma_{\pi \rho}/\Gamma_{\pi h_1} = 0.35 - 0.57, \\ \Gamma_{\eta h_1}/\Gamma_{\pi h_1} = 0.1 - 0.12, \ \Gamma_{\eta \omega}/\Gamma_{\pi h_1} = 0.042 - 0.058, \ \Gamma_{\eta \omega}/\Gamma_{\pi h_2} = 0.1 - 0.12, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.076 - 0.12, \\ \Gamma_{\pi \alpha_2}/\Gamma_{\rho \rho} = 0.82 - 0.99, \ \Gamma_{\pi h_1}/\Gamma_{\rho \rho} = 0.53 - 0.78, \ \Gamma_{\pi h_1}/\Gamma_{\pi \alpha_2} = 0.64 - 0.78, \ \Gamma_{\rho h_1}/\Gamma_{\tau \rho_2} = 0.33 - 0.54 \\ I_{\rho b_1}/\Gamma_{Total} = 0.28 - 0.3, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.14 - 0.14, \ \Gamma_{\rho \rho}/\Gamma_{\rho h_1} = 0.46 - 0.51, \ \Gamma_{\pi \alpha_2}/\Gamma_{\rho h_1} = 0.54 - 0.58 \\ I_{\rho b_2}/\Gamma_{\rho h_1} = 0.36 - 0.41, \ \Gamma_{\pi \alpha_2}/\Gamma_{\rho \rho} = 0.79 - 0.81, \ \Gamma_{\pi \pi_2}/\Gamma_{\tau h_1}$	$a_4(2040)$	4.0 - 5.8	$\Gamma_{\rho\omega}/\Gamma_{\text{Total}} = 0.36 - 0.38, \Gamma_{\pi\rho}/\Gamma_{\text{Total}} = 0.16 - 0.23, \Gamma_{\pi\rho}/\Gamma_{\rho\omega} = 0.42 - 0.64, \Gamma_{\pi b_1}/\Gamma_{\text{Total}} = 0.22,$
$ \begin{array}{c} \pi_4(2250) 4.0 - 7.0 \\ \hline \\ \pi_{\rho \omega}/\Gamma_{\text{Total}} = 0.15 - 0.19. \ \Gamma_{\rho \sigma_2}/\Gamma_{\text{Total}} = 0.14 - 0.23, \ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.12 - 0.15, \ \Gamma_{\rho h_1}/\Gamma_{\rho \omega} = 0.62 - 0.92, \\ \hline \\ \Gamma_{\rho h_1}/\Gamma_{\rho \sigma_2} = 0.64 - 0.87, \ \Gamma_{\rho \sigma_1}/\Gamma_{\rho \sigma_2} = 0.78 - 0.82, \ \Gamma_{\rho \sigma_1}/\Gamma_{\rho h_1} = 0.9 - 1.3, \ \Gamma_{\pi f_2}/\Gamma_{\pi \rho} = 0.8 - 1.3 \\ \hline \\ \eta_4(2330) 4.0 - 7.0 \\ \hline \\ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.23 - 0.35, \ \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.23 - 0.25, \ \Gamma_{\pi \sigma_2}/\Gamma_{\rho \rho} = 0.45 - 0.74, \ \Gamma_{\pi \sigma_1}/\Gamma_{\pi \sigma_2} = 0.61 - 0.72, \\ \hline \\ \Gamma_{\omega h_1}/\Gamma_{\text{Total}} = 0.093 - 0.14, \ \Gamma_{\omega h_1}/\Gamma_{\rho h_1} = 0.4 - 0.41, \ \Gamma_{\omega h_1}/\Gamma_{\rho \rho} = 0.39 - 0.61, \ \Gamma_{\omega \omega}/\Gamma_{\text{Total}} = 0.075 - 0.079 \\ \hline \\ \rho_4(2230) 6.8 - 7.0 \\ \hline \\ \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.2 - 0.21, \ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.19 - 0.27, \ \Gamma_{\rho h_1}/\Gamma_{\rho \rho} = 0.92 - 1.3, \ \Gamma_{\pi \sigma_1}/\Gamma_{\text{Total}} = 0.094 - 0.12, \\ \hline \\ \Gamma_{\pi \sigma_1}/\Gamma_{\rho \rho} = 0.46 - 0.60, \ \Gamma_{\rho f_2}/\Gamma_{\rho h_1} = 0.3 - 0.39, \ \Gamma_{\omega \sigma_1}/\Gamma_{\rho h_1} = 0.29 - 0.33 \\ \hline \\ \omega_4(2250) 4.0 - 7.0 \\ \hline \\ \Gamma_{\rho \sigma_1}/\Gamma_{\text{Total}} = 0.27 - 0.36, \ \Gamma_{\sigma \sigma_2}/\Gamma_{\rho \sigma_1} = 0.68 - 0.84, \ \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.088 - 0.14, \ \Gamma_{\omega f_2}/\Gamma_{\rho \sigma_1} = 0.32 - 0.38, \\ \hline \\ \Gamma_{\omega f_2}/\Gamma_{\rho \sigma_2} = 0.45 - 0.48, \ \Gamma_{\pi h_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \ \Gamma_{\pi \rho (1700)}/\Gamma_{\text{Total}} = 0.043 - 0.052, \ \Gamma_{\pi \rho (1700)}/\Gamma_{\rho \sigma_1} = 0.14 - 0.16 \\ \hline \\ \omega_5(22250) 4.0 - 7.0 \\ \hline \\ \Gamma_{\rho \sigma_2}/\Gamma_{\text{Total}} = 0.42 - 0.58, \ \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.19 - 0.23, \ \Gamma_{\omega f_2}/\Gamma_{\rho \sigma_2} = 0.4 - 0.45, \ \Gamma_{\pi \rho}/\Gamma_{\pi h_1} = 0.35 - 0.57, \\ \hline \\ \Gamma_{\eta h_1}/\Gamma_{\pi h_1} = 0.1 - 0.12, \ \Gamma_{\eta \omega}/\Gamma_{\pi h_1} = 0.042 - 0.058, \ \Gamma_{\eta \omega}/\Gamma_{\pi \rho} = 0.1042, \ \Gamma_{\sigma \omega_2}/\Gamma_{\rho \sigma_2} = 0.4 - 0.45, \ \Gamma_{\pi \rho}/\Gamma_{\pi h_1} = 0.35 - 0.58 \\ \hline \\ \rho_5(2350) 4.0 - 7.0 \\ \hline \\ \Gamma_{\rho f_2}/\Gamma_{\text{Total}} = 0.20 - 0.21, \ \Gamma_{\omega \sigma_2}/\Gamma_{\text{Total}} = 0.17 - 0.24, \ \Gamma_{\omega \sigma_2}/\Gamma_{\rho f_2} = 0.86 - 1, \ \Gamma_{\rho \rho}/\Gamma_{\pi h_1} = 0.35 - 0.58 \\ \hline \\ \rho_5(2510) 6.0 - 6.4 \\ \hline \\ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.28 - 0.3, \ \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.14 - 0.14, \ \Gamma_{\rho \rho}/\Gamma_{\rho h_1} = 0.46 - 0.51, \ \Gamma_{\pi \sigma_2}/\Gamma_{\text{Total}} = 0.11 - 0.12, \\ \hline \\ \Gamma_$			$\Gamma_{\pi b_1}/\Gamma_{\rho\omega} = 0.59 - 0.61, \Gamma_{\pi b_1}/\Gamma_{\pi\rho} = 0.96 - 1.4, \Gamma_{\pi f_2}/\Gamma_{\text{Total}} = 0.11, \Gamma_{\pi f_2}/\Gamma_{\rho\omega} = 0.29 - 0.3$
$\Gamma_{\rho h_1}/\Gamma_{\rho a_2} = 0.64 - 0.87, \ \Gamma_{\rho a_1}/\Gamma_{\rho a_2} = 0.78 - 0.82, \ \Gamma_{\rho a_1}/\Gamma_{\rho h_1} = 0.9 - 1.3, \ \Gamma_{\pi f_2}/\Gamma_{\pi \rho} = 0.8 - 1.3$ $\eta_4(2330) 4.0 - 7.0 \qquad \Gamma_{\rho h_1}/\Gamma_{Total} = 0.23 - 0.35, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.23 - 0.25, \ \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.45 - 0.74, \ \Gamma_{\pi a_1}/\Gamma_{\pi a_2} = 0.61 - 0.72,$ $\Gamma_{\omega h_1}/\Gamma_{Total} = 0.093 - 0.14, \ \Gamma_{\omega h_1}/\Gamma_{\rho h_1} = 0.4 - 0.41, \ \Gamma_{\omega h_1}/\Gamma_{\rho \rho} = 0.39 - 0.61, \ \Gamma_{\omega \omega}/\Gamma_{Total} = 0.075 - 0.079$ $\rho_4(2230) 6.8 - 7.0 \qquad \Gamma_{\rho \rho}/\Gamma_{Total} = 0.2 - 0.21, \ \Gamma_{\rho h_1}/\Gamma_{Total} = 0.19 - 0.27, \ \Gamma_{\rho h_1}/\Gamma_{\rho \rho} = 0.92 - 1.3, \ \Gamma_{\pi a_1}/\Gamma_{Total} = 0.094 - 0.12,$ $\Gamma_{\pi a_1}/\Gamma_{\rho \rho} = 0.46 - 0.60, \ \Gamma_{\rho f_2}/\Gamma_{\rho h_1} = 0.3 - 0.39, \ \Gamma_{\omega a_1}/\Gamma_{\rho h_1} = 0.29 - 0.33$ $\omega_4(2250) 4.0 - 7.0 \qquad \Gamma_{\rho a_1}/\Gamma_{Total} = 0.27 - 0.36, \ \Gamma_{\rho a_2}/\Gamma_{\rho a_1} = 0.68 - 0.84, \ \Gamma_{\omega f_2}/\Gamma_{Total} = 0.088 - 0.14, \ \Gamma_{\omega f_2}/\Gamma_{\rho a_1} = 0.32 - 0.38,$ $\Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.45 - 0.48, \ \Gamma_{\pi h_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \ \Gamma_{\pi \rho(1700)}/\Gamma_{Total} = 0.043 - 0.052, \ \Gamma_{\pi \rho(1700)}/\Gamma_{\rho a_1} = 0.14 - 0.16$ $\omega_5(22250) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{Total} = 0.42 - 0.58, \ \Gamma_{\omega f_2}/\Gamma_{Total} = 0.19 - 0.23, \ \Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.4 - 0.45, \ \Gamma_{\pi \rho}/\Gamma_{\pi h_1} = 0.35 - 0.58$ $\rho_5(2350) 4.0 - 7.0 \qquad \Gamma_{\rho h_1}/\Gamma_{\pi h_1} = 0.1 - 0.12, \ \Gamma_{\omega \sigma_2}/\Gamma_{Total} = 0.17 - 0.24, \ \Gamma_{\omega a_2}/\Gamma_{\rho f_2} = 0.86 - 1, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.087 - 0.12,$ $\Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.82 - 0.99, \ \Gamma_{\pi h_1}/\Gamma_{\rho \rho} = 0.53 - 0.78, \ \Gamma_{\pi h_1}/\Gamma_{\pi a_2} = 0.64 - 0.78, \ \Gamma_{\rho h_1}/\Gamma_{\rho h_1} = 0.35 - 0.58$ $\Gamma_{\rho h_2}/\Gamma_{Total} = 0.28 - 0.3, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.14 - 0.14, \ \Gamma_{\rho \rho}/\Gamma_{\rho h_1} = 0.46 - 0.51, \ \Gamma_{\pi a_2}/\Gamma_{Total} = 0.11 - 0.12,$ $\Gamma_{\pi a_2}/\Gamma_{\rho h_1} = 0.36 - 0.41, \ \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.79 - 0.81, \ \Gamma_{\pi \pi_2}/\Gamma_{Total} = 0.16, \ \Gamma_{\pi \pi_2}/\Gamma_{Total} = 0.11 - 0.12,$ $\Gamma_{\pi a_2}/\Gamma_{\rho h_1} = 0.36 - 0.41, \ \Gamma_{\pi \omega}/\Gamma_{\tau h_1} = 0.14 - 0.12, \ \Gamma_{\pi \omega}/\Gamma_{\tau h_1} = 0.16, \ \Gamma_{\pi \pi_2}/\Gamma_{\tau h_1} = 0.14 - 0.12,$ $\Gamma_{\pi a_2}/\Gamma_{\rho h_1} = 0.36 - 0.41, \ \Gamma_{\pi \omega}/\Gamma_{\rho \rho} = 0.79 - 0.81, \ \Gamma_{\pi \omega}/\Gamma_{\tau h_1} = $	$a_4(2255)$	4.7 - 4.8	$\Gamma_{\pi f_2}/\Gamma_{\pi b_1} = 0.41 - 0.57, \Gamma_{\pi f_1}/\Gamma_{\pi f_2} = 0.092 - 0.14, \Gamma_{\pi \eta^*}/\Gamma_{\pi \eta} = 0.22 - 0.29$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\pi_4(2250)$	4.0 - 7.0	$\Gamma_{\rho\omega}/\Gamma_{Total} = 0.15 - 0.19. \ \Gamma_{\rho a_2}/\Gamma_{Total} = 0.14 - 0.23, \ \Gamma_{\rho h_1}/\Gamma_{Total} = 0.12 - 0.15, \ \Gamma_{\rho h_1}/\Gamma_{\rho\omega} = 0.62 - 0.92,$
$ \Gamma_{\omega h_1}/\Gamma_{\text{Total}} = 0.093 - 0.14, \ \Gamma_{\omega h_1}/\Gamma_{\rho b_1} = 0.4 - 0.41, \ \Gamma_{\omega h_1}/\Gamma_{\rho \rho} = 0.39 - 0.61, \ \Gamma_{\omega \omega}/\Gamma_{\text{Total}} = 0.075 - 0.079 $ $ \rho_4(2230) 6.8 - 7.0 \qquad \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.2 - 0.21, \ \Gamma_{\rho b_1}/\Gamma_{\text{Total}} = 0.19 - 0.27, \ \Gamma_{\rho b_1}/\Gamma_{\rho \rho} = 0.92 - 1.3, \ \Gamma_{\pi a_1}/\Gamma_{\text{Total}} = 0.094 - 0.12, $ $ \Gamma_{\pi a_1}/\Gamma_{\rho \rho} = 0.46 - 0.60, \ \Gamma_{\rho f_2}/\Gamma_{\rho b_1} = 0.3 - 0.39, \ \Gamma_{\omega a_1}/\Gamma_{\rho b_1} = 0.29 - 0.33 $ $ \omega_4(2250) 4.0 - 7.0 \qquad \Gamma_{\rho a_1}/\Gamma_{\text{Total}} = 0.27 - 0.36, \ \Gamma_{\rho a_2}/\Gamma_{\rho a_1} = 0.68 - 0.84, \ \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.088 - 0.14, \ \Gamma_{\omega f_2}/\Gamma_{\rho a_1} = 0.32 - 0.38, $ $ \Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.45 - 0.48, \ \Gamma_{\pi b_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \ \Gamma_{\pi \rho(1700)}/\Gamma_{\text{Total}} = 0.043 - 0.052, \ \Gamma_{\pi \rho(1700)}/\Gamma_{\rho a_1} = 0.14 - 0.16 $ $ \omega_5(22250) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.42 - 0.58, \ \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.19 - 0.23, \ \Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.4 - 0.45, \ \Gamma_{\pi \rho}/\Gamma_{\pi b_1} = 0.35 - 0.57, $ $ \Gamma_{\eta h_1}/\Gamma_{\pi b_1} = 0.1 - 0.12, \ \Gamma_{\eta \omega}/\Gamma_{\pi b_1} = 0.042 - 0.058, \ \Gamma_{\eta \omega}/\Gamma_{\pi \rho} = 0.1 - 0.12, \ \Gamma_{\eta \omega}/\Gamma_{\eta h_1} = 0.35 - 0.58 $ $ \rho_5(2350) 4.0 - 7.0 \qquad \Gamma_{\rho f_2}/\Gamma_{\text{Total}} = 0.20 - 0.21, \ \Gamma_{\omega a_2}/\Gamma_{\text{Total}} = 0.17 - 0.24, \ \Gamma_{\omega a_2}/\Gamma_{\rho f_2} = 0.86 - 1, \ \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.087 - 0.12, $ $ \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.82 - 0.99, \ \Gamma_{\pi h_1}/\Gamma_{\rho \rho} = 0.53 - 0.78, \ \Gamma_{\pi h_1}/\Gamma_{\pi a_2} = 0.64 - 0.78, \ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.11 - 0.12, $ $ \Gamma_{\pi a_2}/\Gamma_{\rho h_1} = 0.36 - 0.41, \ \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.79 - 0.81, \ \Gamma_{\pi \pi_2}/\Gamma_{\text{Total}} = 0.16, \ \Gamma_{\pi \pi_2}/\Gamma_{\text{Potal}} = 0.54 - 0.58 $ $ \alpha_6(2450) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.37 - 0.46, \ \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \ \Gamma_{\rho \omega}/\Gamma_{\pi h_1} = 0.75 - 1.1, \ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.076 - 0.12, $			$\Gamma_{\rho h_1}/\Gamma_{\rho a_2} = 0.64 - 0.87, \Gamma_{\rho a_1}/\Gamma_{\rho a_2} = 0.78 - 0.82, \Gamma_{\rho a_1}/\Gamma_{\rho h_1} = 0.9 - 1.3, \Gamma_{\pi f_2}/\Gamma_{\pi \rho} = 0.8 - 1.3$
$\rho_{4}(2230) 6.8-7.0 \qquad \Gamma_{\rho\rho}/\Gamma_{Total} = 0.2-0.21, \ \Gamma_{\rho b_{1}}/\Gamma_{Total} = 0.19-0.27, \ \Gamma_{\rho b_{1}}/\Gamma_{\rho\rho} = 0.92-1.3, \ \Gamma_{\pi a_{1}}/\Gamma_{Total} = 0.094-0.12, \\ \Gamma_{\pi a_{1}}/\Gamma_{\rho\rho} = 0.46-0.60, \ \Gamma_{\rho f_{2}}/\Gamma_{\rho b_{1}} = 0.3-0.39, \ \Gamma_{\omega a_{1}}/\Gamma_{\rho b_{1}} = 0.29-0.33 \\ \omega_{4}(2250) 4.0-7.0 \qquad \Gamma_{\rho a_{1}}/\Gamma_{Total} = 0.27-0.36, \ \Gamma_{\rho a_{2}}/\Gamma_{\rho a_{1}} = 0.68-0.84, \ \Gamma_{\omega f_{2}}/\Gamma_{Total} = 0.088-0.14, \ \Gamma_{\omega f_{2}}/\Gamma_{\rho a_{1}} = 0.32-0.38, \\ \Gamma_{\omega f_{2}}/\Gamma_{\rho a_{2}} = 0.45-0.48, \ \Gamma_{\pi b_{1}}/\Gamma_{\pi \rho} = 0.33-0.47, \ \Gamma_{\pi \rho(1700)}/\Gamma_{Total} = 0.043-0.052, \ \Gamma_{\pi \rho(1700)}/\Gamma_{\rho a_{1}} = 0.14-0.16 \\ \omega_{5}(22250) 4.0-7.0 \qquad \Gamma_{\rho a_{2}}/\Gamma_{Total} = 0.42-0.58, \ \Gamma_{\omega f_{2}}/\Gamma_{Total} = 0.19-0.23, \ \Gamma_{\omega f_{2}}/\Gamma_{\rho a_{2}} = 0.4-0.45, \ \Gamma_{\pi \rho}/\Gamma_{\pi b_{1}} = 0.35-0.58 \\ \rho_{5}(2350) 4.0-7.0 \qquad \Gamma_{\rho f_{2}}/\Gamma_{Total} = 0.20-0.21, \ \Gamma_{\omega \alpha_{2}}/\Gamma_{Total} = 0.17-0.24, \ \Gamma_{\omega a_{2}}/\Gamma_{\rho f_{2}} = 0.86-1, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.087-0.12, \\ \Gamma_{\pi a_{2}}/\Gamma_{\rho \rho} = 0.82-0.99, \ \Gamma_{\pi h_{1}}/\Gamma_{\rho \rho} = 0.53-0.78, \ \Gamma_{\pi h_{1}}/\Gamma_{\pi a_{2}} = 0.64-0.78, \ \Gamma_{\rho b_{1}}/\Gamma_{\rho f_{2}} = 0.33-0.54 \\ f_{6}(2510) 6.0-6.4 \qquad \Gamma_{\rho b_{1}}/\Gamma_{Total} = 0.28-0.3, \ \Gamma_{\rho \rho}/\Gamma_{Total} = 0.14-0.14, \ \Gamma_{\rho \rho}/\Gamma_{\rho b_{1}} = 0.46-0.51, \ \Gamma_{\pi a_{2}}/\Gamma_{Total} = 0.11-0.12, \\ \Gamma_{\pi a_{2}}/\Gamma_{\rho b_{1}} = 0.36-0.41, \ \Gamma_{\pi a_{2}}/\Gamma_{\rho \rho} = 0.79-0.81, \ \Gamma_{\pi \pi_{2}}/\Gamma_{Total} = 0.16, \ \Gamma_{\pi \pi_{2}}/\Gamma_{Total} = 0.54-0.58 \\ a_{6}(2450) 4.0-7.0 \qquad \Gamma_{\rho a_{2}}/\Gamma_{Total} = 0.37-0.46, \ \Gamma_{\rho \omega}/\Gamma_{Total} = 0.074-0.12, \ \Gamma_{\rho \omega}/\Gamma_{\pi b_{1}} = 0.75-1.1, \ \Gamma_{\rho h_{1}}/\Gamma_{Total} = 0.076-0.12, \\ \Gamma_{\rho a_{2}}/\Gamma_{Total} = 0.37-0.46, \ \Gamma_{\rho \omega}/\Gamma_{Total} = 0.074-0.12, \ \Gamma_{\rho \omega}/\Gamma_{\pi b_{1}} = 0.75-1.1, \ \Gamma_{\rho h_{1}}/\Gamma_{Total} = 0.076-0.12, \\ \Gamma_{\rho a_{2}}/\Gamma_{Total} = 0.37-0.46, \ \Gamma_{\rho \omega}/\Gamma_{Total} = 0.074-0.12, \ \Gamma_{\rho \omega}/\Gamma_{\pi b_{1}} = 0.75-1.1, \ \Gamma_{\rho h_{1}}/\Gamma_{Total} = 0.076-0.12, \\ \Gamma_{\rho a_{2}}/\Gamma_{Total} = 0.37-0.46, \ \Gamma_{\rho \omega}/\Gamma_{Total} = 0.074-0.12, \ \Gamma_{\rho \omega}/\Gamma_{\pi b_{1}} = 0.75-1.1, \ \Gamma_{\rho h_{1}}/\Gamma_{Total} = 0.076-0.12, \\ \Gamma_{\rho \alpha}/\Gamma_{\tau \tau $	$\eta_4(2330)$	4.0 - 7.0	$\Gamma_{\rho b_1}/\Gamma_{Total} = 0.23 - 0.35, \Gamma_{\rho \rho}/\Gamma_{Total} = 0.23 - 0.25, \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.45 - 0.74, \Gamma_{\pi a_1}/\Gamma_{\pi a_2} = 0.61 - 0.72,$
$\Gamma_{\pi a_1}/\Gamma_{\rho\rho} = 0.46 - 0.60, \ \Gamma_{\rho f_2}/\Gamma_{\rho b_1} = 0.3 - 0.39, \ \Gamma_{\omega a_1}/\Gamma_{\rho b_1} = 0.29 - 0.33$ $\omega_4(2250) 4.0 - 7.0 \qquad \Gamma_{\rho a_1}/\Gamma_{\text{Total}} = 0.27 - 0.36, \ \Gamma_{\rho a_2}/\Gamma_{\rho a_1} = 0.68 - 0.84, \ \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.088 - 0.14, \ \Gamma_{\omega f_2}/\Gamma_{\rho a_1} = 0.32 - 0.38, \ \Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.45 - 0.48, \ \Gamma_{\pi b_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \ \Gamma_{\pi \rho (1700)}/\Gamma_{\text{Total}} = 0.043 - 0.052, \ \Gamma_{\pi \rho (1700)}/\Gamma_{\rho a_1} = 0.14 - 0.16$ $\omega_5(22250) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.42 - 0.58, \ \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.19 - 0.23, \ \Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.4 - 0.45, \ \Gamma_{\pi \rho}/\Gamma_{\pi b_1} = 0.35 - 0.57, \ \Gamma_{\eta h_1}/\Gamma_{\pi b_1} = 0.1 - 0.12, \ \Gamma_{\eta \omega}/\Gamma_{\pi b_1} = 0.042 - 0.058, \ \Gamma_{\eta \omega}/\Gamma_{\pi \rho} = 0.1 - 0.12, \ \Gamma_{\eta \omega}/\Gamma_{\eta h_1} = 0.35 - 0.58$ $\rho_5(2350) 4.0 - 7.0 \qquad \Gamma_{\rho f_2}/\Gamma_{\text{Total}} = 0.20 - 0.21, \ \Gamma_{\omega a_2}/\Gamma_{\text{Total}} = 0.17 - 0.24, \ \Gamma_{\omega a_2}/\Gamma_{\rho f_2} = 0.86 - 1, \ \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.087 - 0.12, \ \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.82 - 0.99, \ \Gamma_{\pi h_1}/\Gamma_{\rho \rho} = 0.53 - 0.78, \ \Gamma_{\pi h_1}/\Gamma_{\pi a_2} = 0.64 - 0.78, \ \Gamma_{\rho h_1}/\Gamma_{\rho f_2} = 0.33 - 0.54$ $f_6(2510) 6.0 - 6.4 \qquad \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.28 - 0.3, \ \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.14 - 0.14, \ \Gamma_{\rho \rho}/\Gamma_{\rho h_1} = 0.46 - 0.51, \ \Gamma_{\pi a_2}/\Gamma_{\text{Total}} = 0.11 - 0.12, \ \Gamma_{\pi a_2}/\Gamma_{\rho h_1} = 0.36 - 0.41, \ \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.79 - 0.81, \ \Gamma_{\pi \pi_2}/\Gamma_{\text{Total}} = 0.16, \ \Gamma_{\pi \pi_2}/\Gamma_{\rho h_1} = 0.54 - 0.58$ $a_6(2450) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.37 - 0.46, \ \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \ \Gamma_{\rho \omega}/\Gamma_{\pi h_1} = 0.75 - 1.1, \ \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.076 - 0.12,$			$\Gamma_{\omega h_1}/\Gamma_{Total} = 0.093 - 0.14, \Gamma_{\omega h_1}/\Gamma_{\rho b_1} = 0.4 - 0.41, \Gamma_{\omega h_1}/\Gamma_{\rho \rho} = 0.39 - 0.61, \Gamma_{\omega \omega}/\Gamma_{Total} = 0.075 - 0.079$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\rho_4(2230)$	6.8 - 7.0	$\Gamma_{\rho\rho}/\Gamma_{\text{Total}} = 0.2 - 0.21, \Gamma_{\rho b_1}/\Gamma_{\text{Total}} = 0.19 - 0.27, \Gamma_{\rho b_1}/\Gamma_{\rho\rho} = 0.92 - 1.3, \Gamma_{\pi a_1}/\Gamma_{\text{Total}} = 0.094 - 0.12,$
$\Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.45 - 0.48, \Gamma_{\pi b_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \Gamma_{\pi \rho(1700)}/\Gamma_{Total} = 0.043 - 0.052, \Gamma_{\pi \rho(1700)}/\Gamma_{\rho a_1} = 0.14 - 0.16$ $\omega_5(22250) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{Total} = 0.42 - 0.58, \Gamma_{\omega f_2}/\Gamma_{Total} = 0.19 - 0.23, \Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.4 - 0.45, \Gamma_{\pi \rho}/\Gamma_{\pi b_1} = 0.35 - 0.57,$ $\Gamma_{\eta h_1}/\Gamma_{\pi b_1} = 0.1 - 0.12, \Gamma_{\eta \omega}/\Gamma_{\pi b_1} = 0.042 - 0.058, \Gamma_{\eta \omega}/\Gamma_{\pi \rho} = 0.1 - 0.12, \Gamma_{\eta \omega}/\Gamma_{\eta h_1} = 0.35 - 0.58$ $\rho_5(2350) 4.0 - 7.0 \qquad \Gamma_{\rho f_2}/\Gamma_{Total} = 0.20 - 0.21, \Gamma_{\omega a_2}/\Gamma_{Total} = 0.17 - 0.24, \Gamma_{\omega a_2}/\Gamma_{\rho f_2} = 0.86 - 1, \Gamma_{\rho \rho}/\Gamma_{Total} = 0.087 - 0.12,$ $\Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.82 - 0.99, \Gamma_{\pi h_1}/\Gamma_{\rho \rho} = 0.53 - 0.78, \Gamma_{\pi h_1}/\Gamma_{\pi a_2} = 0.64 - 0.78, \Gamma_{\rho h_1}/\Gamma_{\rho f_2} = 0.33 - 0.54$ $f_6(2510) 6.0 - 6.4 \qquad \Gamma_{\rho b_1}/\Gamma_{Total} = 0.28 - 0.3, \Gamma_{\rho \rho}/\Gamma_{Total} = 0.14 - 0.14, \Gamma_{\rho \rho}/\Gamma_{\rho b_1} = 0.46 - 0.51, \Gamma_{\pi a_2}/\Gamma_{Total} = 0.11 - 0.12,$ $\Gamma_{\pi a_2}/\Gamma_{\rho h_1} = 0.36 - 0.41, \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.79 - 0.81, \Gamma_{\pi \pi_2}/\Gamma_{Total} = 0.16, \Gamma_{\pi \pi_2}/\Gamma_{\rho h_1} = 0.54 - 0.58$ $a_6(2450) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{Total} = 0.37 - 0.46, \Gamma_{\rho \omega}/\Gamma_{Total} = 0.074 - 0.12, \Gamma_{\rho \omega}/\Gamma_{\pi b_1} = 0.75 - 1.1, \Gamma_{\rho h_1}/\Gamma_{Total} = 0.076 - 0.12,$			$\Gamma_{\pi a_1}/\Gamma_{\rho\rho} = 0.46 - 0.60, \Gamma_{\rho f_2}/\Gamma_{\rho b_1} = 0.3 - 0.39, \Gamma_{\omega a_1}/\Gamma_{\rho b_1} = 0.29 - 0.33$
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	$\omega_4(2250)$	4.0- 7.0	$\Gamma_{\rho a_1}/\Gamma_{Total} = 0.27 - 0.36, \Gamma_{\rho a_2}/\Gamma_{\rho a_1} = 0.68 - 0.84, \Gamma_{\omega f_2}/\Gamma_{Total} = 0.088 - 0.14, \Gamma_{\omega f_2}/\Gamma_{\rho a_1} = 0.32 - 0.38,$
$\Gamma_{\eta h_1}/\Gamma_{\pi h_1} = 0.1 - 0.12, \Gamma_{\eta \omega}/\Gamma_{\pi h_1} = 0.042 - 0.058, \Gamma_{\eta \omega}/\Gamma_{\pi \rho} = 0.1 - 0.12, \Gamma_{\eta \omega}/\Gamma_{\eta h_1} = 0.35 - 0.58$ $\rho_5(2350) 4.0 - 7.0 \Gamma_{\rho f_2}/\Gamma_{\text{Total}} = 0.20 - 0.21, \Gamma_{\omega a_2}/\Gamma_{\text{Total}} = 0.17 - 0.24, \Gamma_{\omega a_2}/\Gamma_{\rho f_2} = 0.86 - 1, \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.087 - 0.12, \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.82 - 0.99, \Gamma_{\pi h_1}/\Gamma_{\rho \rho} = 0.53 - 0.78, \Gamma_{\pi h_1}/\Gamma_{\pi a_2} = 0.64 - 0.78, \Gamma_{\rho h_1}/\Gamma_{\rho f_2} = 0.33 - 0.54$ $f_6(2510) 6.0 - 6.4 \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.28 - 0.3, \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.14 - 0.14, \Gamma_{\rho \rho}/\Gamma_{\rho h_1} = 0.46 - 0.51, \Gamma_{\pi a_2}/\Gamma_{\text{Total}} = 0.11 - 0.12, \Gamma_{\pi a_2}/\Gamma_{\rho h_1} = 0.36 - 0.41, \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.79 - 0.81, \Gamma_{\pi \pi_2}/\Gamma_{\text{Total}} = 0.16, \Gamma_{\pi \pi_2}/\Gamma_{\rho h_1} = 0.54 - 0.58$ $a_6(2450) 4.0 - 7.0 \Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.37 - 0.46, \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \Gamma_{\rho \omega}/\Gamma_{\pi h_1} = 0.75 - 1.1, \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.076 - 0.12,$			$\Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.45 - 0.48, \Gamma_{\pi b_1}/\Gamma_{\pi \rho} = 0.33 - 0.47, \Gamma_{\pi \rho (1700)}/\Gamma_{Total} = 0.043 - 0.052, \Gamma_{\pi \rho (1700)}/\Gamma_{\rho a_1} = 0.14 - 0.16$
$\rho_{5}(2350) 4.0 - 7.0 \qquad \Gamma_{\rho f_{2}}/\Gamma_{\text{Total}} = 0.20 - 0.21, \Gamma_{\omega a_{2}}/\Gamma_{\text{Total}} = 0.17 - 0.24, \Gamma_{\omega a_{2}}/\Gamma_{\rho f_{2}} = 0.86 - 1, \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.087 - 0.12, \\ \Gamma_{\pi a_{2}}/\Gamma_{\rho \rho} = 0.82 - 0.99, \Gamma_{\pi h_{1}}/\Gamma_{\rho \rho} = 0.53 - 0.78, \Gamma_{\pi h_{1}}/\Gamma_{\pi a_{2}} = 0.64 - 0.78, \Gamma_{\rho b_{1}}/\Gamma_{\rho f_{2}} = 0.33 - 0.54$ $f_{6}(2510) 6.0 - 6.4 \qquad \Gamma_{\rho b_{1}}/\Gamma_{\text{Total}} = 0.28 - 0.3, \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.14 - 0.14, \Gamma_{\rho \rho}/\Gamma_{\rho b_{1}} = 0.46 - 0.51, \Gamma_{\pi a_{2}}/\Gamma_{\text{Total}} = 0.11 - 0.12, \\ \Gamma_{\pi a_{2}}/\Gamma_{\rho b_{1}} = 0.36 - 0.41, \Gamma_{\pi a_{2}}/\Gamma_{\rho \rho} = 0.79 - 0.81, \Gamma_{\pi \pi_{2}}/\Gamma_{\text{Total}} = 0.16, \Gamma_{\pi \pi_{2}}/\Gamma_{\rho b_{1}} = 0.54 - 0.58$ $a_{6}(2450) 4.0 - 7.0 \qquad \Gamma_{\rho a_{2}}/\Gamma_{\text{Total}} = 0.37 - 0.46, \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \Gamma_{\rho \omega}/\Gamma_{\pi b_{1}} = 0.75 - 1.1, \Gamma_{\rho h_{1}}/\Gamma_{\text{Total}} = 0.076 - 0.12,$	$\omega_5(22250)$	4.0-7.0	$\Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.42 - 0.58, \Gamma_{\omega f_2}/\Gamma_{\text{Total}} = 0.19 - 0.23, \Gamma_{\omega f_2}/\Gamma_{\rho a_2} = 0.4 - 0.45, \Gamma_{\pi \rho}/\Gamma_{\pi b_1} = 0.35 - 0.57,$
$\Gamma_{\pi a_2}/\Gamma_{\rho\rho} = 0.82 - 0.99, \Gamma_{\pi h_1}/\Gamma_{\rho\rho} = 0.53 - 0.78, \Gamma_{\pi h_1}/\Gamma_{\pi a_2} = 0.64 - 0.78, \Gamma_{\rho b_1}/\Gamma_{\rho f_2} = 0.33 - 0.54$ $f_6(2510) 6.0 - 6.4 \qquad \Gamma_{\rho b_1}/\Gamma_{\text{Total}} = 0.28 - 0.3, \Gamma_{\rho\rho}/\Gamma_{\text{Total}} = 0.14 - 0.14, \Gamma_{\rho\rho}/\Gamma_{\rho b_1} = 0.46 - 0.51, \Gamma_{\pi a_2}/\Gamma_{\text{Total}} = 0.11 - 0.12, \Gamma_{\pi a_2}/\Gamma_{\rho b_1} = 0.36 - 0.41, \Gamma_{\pi a_2}/\Gamma_{\rho\rho} = 0.79 - 0.81, \Gamma_{\pi \pi_2}/\Gamma_{\text{Total}} = 0.16, \Gamma_{\pi \pi_2}/\Gamma_{\rho b_1} = 0.54 - 0.58$ $a_6(2450) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.37 - 0.46, \Gamma_{\rho\omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \Gamma_{\rho\omega}/\Gamma_{\pi b_1} = 0.75 - 1.1, \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.076 - 0.12,$			$\Gamma_{\eta h_1}/\Gamma_{\pi h_1} = 0.1 - 0.12, \Gamma_{\eta \omega}/\Gamma_{\pi h_1} = 0.042 - 0.058, \Gamma_{\eta \omega}/\Gamma_{\pi \rho} = 0.1 - 0.12, \Gamma_{\eta \omega}/\Gamma_{\eta h_1} = 0.35 - 0.58$
$f_{6}(2510) 6.0 - 6.4 \qquad \Gamma_{\rho b_{1}}/\Gamma_{\text{Total}} = 0.28 - 0.3, \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.14 - 0.14, \Gamma_{\rho \rho}/\Gamma_{\rho b_{1}} = 0.46 - 0.51, \Gamma_{\pi a_{2}}/\Gamma_{\text{Total}} = 0.11 - 0.12,$ $\Gamma_{\pi a_{2}}/\Gamma_{\rho b_{1}} = 0.36 - 0.41, \Gamma_{\pi a_{2}}/\Gamma_{\rho \rho} = 0.79 - 0.81, \Gamma_{\pi \pi_{2}}/\Gamma_{\text{Total}} = 0.16, \Gamma_{\pi \pi_{2}}/\Gamma_{\rho b_{1}} = 0.54 - 0.58$ $a_{6}(2450) 4.0 - 7.0 \qquad \Gamma_{\rho a_{2}}/\Gamma_{\text{Total}} = 0.37 - 0.46, \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \Gamma_{\rho \omega}/\Gamma_{\pi b_{1}} = 0.75 - 1.1, \Gamma_{\rho h_{1}}/\Gamma_{\text{Total}} = 0.076 - 0.12,$	$\rho_5(2350)$	4.0 - 7.0	$\Gamma_{\rho f_2}/\Gamma_{\text{Total}} = 0.20 - 0.21, \Gamma_{\omega a_2}/\Gamma_{\text{Total}} = 0.17 - 0.24, \Gamma_{\omega a_2}/\Gamma_{\rho f_2} = 0.86 - 1, \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.087 - 0.12,$
$\Gamma_{\pi a_2}/\Gamma_{\rho b_1} = 0.36 - 0.41, \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.79 - 0.81, \Gamma_{\pi \pi_2}/\Gamma_{\text{Total}} = 0.16, \Gamma_{\pi \pi_2}/\Gamma_{\rho b_1} = 0.54 - 0.58$ $a_6(2450) 4.0 - 7.0 \qquad \Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.37 - 0.46, \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \Gamma_{\rho \omega}/\Gamma_{\pi b_1} = 0.75 - 1.1, \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.076 - 0.12,$			$\Gamma_{\pi a_2}/\Gamma_{\rho\rho} = 0.82 - 0.99, \Gamma_{\pi h_1}/\Gamma_{\rho\rho} = 0.53 - 0.78, \Gamma_{\pi h_1}/\Gamma_{\pi a_2} = 0.64 - 0.78, \Gamma_{\rho b_1}/\Gamma_{\rho f_2} = 0.33 - 0.54$
$a_{6}(2450) 4.0 - 7.0 \qquad \Gamma_{\rho a_{2}}/\Gamma_{\text{Total}} = 0.37 - 0.46, \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \Gamma_{\rho \omega}/\Gamma_{\pi b_{1}} = 0.75 - 1.1, \Gamma_{\rho h_{1}}/\Gamma_{\text{Total}} = 0.076 - 0.12,$	$f_6(2510)$	6.0 - 6.4	$\Gamma_{\rho b_1}/\Gamma_{\text{Total}} = 0.28 - 0.3, \Gamma_{\rho \rho}/\Gamma_{\text{Total}} = 0.14 - 0.14, \Gamma_{\rho \rho}/\Gamma_{\rho b_1} = 0.46 - 0.51, \Gamma_{\pi a_2}/\Gamma_{\text{Total}} = 0.11 - 0.12,$
			$\Gamma_{\pi a_2}/\Gamma_{\rho b_1} = 0.36 - 0.41, \Gamma_{\pi a_2}/\Gamma_{\rho \rho} = 0.79 - 0.81, \Gamma_{\pi \pi_2}/\Gamma_{\text{Total}} = 0.16, \Gamma_{\pi \pi_2}/\Gamma_{\rho b_1} = 0.54 - 0.58$
$\Gamma_{-k}/\Gamma_{-k} = 0.21 - 0.27$ $\Gamma_{-k}/\Gamma_{-k} = 0.43 - 0.48$ $\Gamma_{-k}/\Gamma_{-k} = 0.43 - 0.57$ $\Gamma_{-k}/\Gamma_{-k} = 0.24 - 0.39$	$a_6(2450)$	4.0 - 7.0	$\Gamma_{\rho a_2}/\Gamma_{\text{Total}} = 0.37 - 0.46, \Gamma_{\rho \omega}/\Gamma_{\text{Total}} = 0.074 - 0.12, \Gamma_{\rho \omega}/\Gamma_{\pi b_1} = 0.75 - 1.1, \Gamma_{\rho h_1}/\Gamma_{\text{Total}} = 0.076 - 0.12,$
$1 \rho n_1 / 1 \rho a_2 = 0.21 0.21 0.21 = 0.70 0.70 0.70 1 \pi j_2 / 1 \rho \omega = 0.70 0.51 1 \pi \rho / 1 \pi b_1 = 0.57$			$\Gamma_{\rho h_1}/\Gamma_{\rho a_2} = 0.21 - 0.27, \Gamma_{\pi f_2}/\Gamma_{\pi b_1} = 0.43 - 0.48, \Gamma_{\pi f_2}/\Gamma_{\rho \omega} = 0.43 - 0.57, \Gamma_{\pi \rho}/\Gamma_{\pi b_1} = 0.24 - 0.39$

B. A. Leontic, K. K. Li and D. N. Michael, Phys. Rev. D 1, 1917 (1970).

^[42] A. A. Carter, Nucl. Phys. B 141, 467 (1978).

^[43] R. S. Dulude, R. E. Lanou, J. T. Massimo, D. C. Peaslee,

R. K. Thornton, D. S. Barton, M. Marx and B. A. Nelson *et al.*, Phys. Lett. B **79**, 335 (1978).

^[44] L. Roca and E. Oset, Phys. Rev. D **82**, 054013 (2010) [arXiv:1005.0283 [hep-ph]].

- [45] A. V. Anisovich, V. V. Anisovich and A. V. Sarantsev, Phys. Rev. D 62, 051502 (2000) [hep-ph/0003113].
- [46] M. J. Corden, J. D. Dowell, J. Garvey, M. Jobes, I. R. Kenyon, J. Mawson, T. McMahon and I. F. Corbett *et al.*, Nucl. Phys. B 136, 77 (1978).
- [47] D. V. Amelin *et al.* [VES Collaboration], Phys. Atom. Nucl. **62**, 445 (1999) [Yad. Fiz. **62**, 487 (1999)].
- [48] D. Alde et al. [GAMS Collaboration], Nuovo Cim. A 107, 1867 (1994) [Z. Phys. C 66, 379 (1995)].
- [49] B. R. Martin and D. Morgan, Nucl. Phys. B 176, 355 (1980).
- [50] V. N. Bolotov, V. V. Isakov, D. B. Kakauridze, G. V. Khaustov,
 Y. D. Prokoshkin and S. A. Sadovsky, Phys. Lett. B 52, 489
 (1974) [Sov. J. Nucl. Phys. 20, 635 (1975)] [Yad. Fiz. 20, 1214
 (1974)].
- [51] D. Alde *et al.* [GAMS Collaboration], Eur. Phys. J. A **3**, 361 (1998)
- [52] A. A. Tseytlin, Phys. Lett. B 208, 228 (1988).
- [53] L. Y. Glozman and A. V. Nefediev, Phys. Rev. D 76, 096004 (2007) [arXiv:0704.2673 [hep-ph]].
- [54] S. S. Afonin, Eur. Phys. J. A 29, 327 (2006) [hep-ph/0606310].
- [55] L. Micu, Nucl. Phys. B 10, 521 (1969).
- [56] A. Le Yaouanc, L. Oliver, O. Pene and J. C. Raynal, Phys. Rev. D 8, 2223 (1973).
- [57] A. Le Yaouanc, L. Oliver, O. Pene and J. -C. Raynal, Phys. Rev. D 9, 1415 (1974).
- [58] A. Le Yaouanc, L. Oliver, O. Pene and J. C. Raynal, Phys. Rev. D 11, 1272 (1975).
- [59] A. Le Yaouanc, L. Oliver, O. Pene and J. -C. Raynal, Phys. Lett. B 71, 397 (1977).
- [60] A. Le Yaouanc, L. Oliver, O. Pene and J. C. Raynal, Phys. Lett. B 72, 57 (1977).
- [61] E. van Beveren, G. Rupp, T. A. Rijken and C. Dullemond, Phys. Rev. D 27, 1527 (1983).
- [62] S. Capstick and W. Roberts, Phys. Rev. D 49, 4570 (1994) [nucl-th/9310030].
- [63] H. G. Blundell and S. Godfrey, Phys. Rev. D 53, 3700 (1996) [hep-ph/9508264].
- [64] E. S. Ackleh, T. Barnes and E. S. Swanson, Phys. Rev. D 54, 6811 (1996) [hep-ph/9604355].
- [65] S. Capstick and B. D. Keister, [nucl-th/9611055].
- [66] F. E. Close and E. S. Swanson, Phys. Rev. D 72, 094004 (2005) [hep-ph/0505206].
- [67] B. Zhang, X. Liu, W. -Z. Deng and S. -L. Zhu, Eur. Phys. J. C 50, 617 (2007) [hep-ph/0609013].
- [68] J. Lu, W. -Z. Deng, X. -L. Chen and S. -L. Zhu, Phys. Rev. D

- 73, 054012 (2006) [hep-ph/0602167].
- [69] Z. -F. Sun and X. Liu, Phys. Rev. D 80, 074037 (2009) [arXiv:0909.1658 [hep-ph]].
- [70] X. Liu, Z. -G. Luo and Z. -F. Sun, Phys. Rev. Lett. 104, 122001 (2010) [arXiv:0911.3694 [hep-ph]].
- [71] Z. -F. Sun, J. -S. Yu, X. Liu and T. Matsuki, Phys. Rev. D 82, 111501 (2010) [arXiv:1008.3120 [hep-ph]].
- [72] T. A. Rijken, M. M. Nagels and Y. Yamamoto, Nucl. Phys. A 835, 160 (2010).
- [73] J. -S. Yu, Z. -F. Sun, X. Liu and Q. Zhao, Phys. Rev. D 83, 114007 (2011) [arXiv:1104.3064 [hep-ph]].
- [74] Z. -Y. Zhou and Z. Xiao, Phys. Rev. D 84, 034023 (2011) [arXiv:1105.6025 [hep-ph]].
- [75] Z. -C. Ye, X. Wang, X. Liu and Q. Zhao, Phys. Rev. D 86, 054025 (2012) [arXiv:1206.0097 [hep-ph]].
- [76] Y. Sun, X. Liu and T. Matsuki, Phys. Rev. D 88, 094020 (2013) [arXiv:1309.2203 [hep-ph]].
- [77] Y. Sun, Q. -T. Song, D. -Y. Chen, X. Liu and S. -L. Zhu, Phys. Rev. D **89**, 054026 (2014) [arXiv:1401.1595 [hep-ph]].
- [78] C. Q. Pang, L. P. He, X. Liu and T. Matsuki, Phys. Rev. D 90, 014001 (2014) [arXiv:1405.3189 [hep-ph]].
- [79] B. Wang, C. Q. Pang, X. Liu and T. Matsuki, Phys. Rev. D 91, 014025 (2015) [arXiv:1410.3930 [hep-ph]].
- [80] X. Wang, Z. F. Sun, D. Y. Chen, X. Liu and T. Matsuki, Phys. Rev. D 85, 074024 (2012) [arXiv:1202.4139 [hep-ph]].
- [81] K. Chen, C. Q. Pang, X. Liu and T. Matsuki, Phys. Rev. D 91, no. 7, 074025 (2015) [arXiv:1501.07766 [hep-ph]].
- [82] W. Roberts and B. Silvestre- Brac, Few Body Syst.11, 171 (1992).
- [83] H. G. Blundell, hep-ph/9608473.
- [84] M. Jacob and G. C. Wick, Annals Phys. 7, 404 (1959) [Annals Phys. 281, 774 (2000)].
- [85] L. Y. Glozman, Phys. Rept. 444, 1 (2007) [hep-ph/0701081].
- [86] L. Y. Glozman, Eur. Phys. J. A **51**, no. 3, 27 (2015) [arXiv:1407.2798 [hep-ph]].
- [87] M. J. Corden, J. D. Dowell, J. Garvey, M. Jobes, I. R. Kenyon, J. Mawson, T. McMahon and I. F. Corbett *et al.*, Nucl. Phys. B 138, 235 (1978).
- [88] E. Klempt and A. Zaitsev, Phys. Rept. **454**, 1 (2007) [arXiv:0708.4016 [hep-ph]].
- [89] A. Bramon and E. Masso, Z. Phys. C 8, 135 (1981).
- [90] D. V. Bugg, Phys. Lett. B 572, 1 (2003) [Erratum-ibid. B 595, 556 (2004)].