

Differential cross section for the Higgs boson production in 4-lepton channel and k_T -factorization

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We present our study of the differential cross section for the Higgs boson production in k_T -factorization framework. The k_T -factorization formalism includes a convolution over unintegrated parton distribution functions (uPDF) and off-shell parton level matrix element. The off-shell matrix element calculated considering initial gluons to be off-shell. We have considered only gluon fusion process which is dominant production mechanism for the Higgs boson production at LHC. We have used Ciafaloni-Catani-Fiorani-Marchesini (CCFM) uPDF based on CCFM evolution equations. We have compared our results with fixed order estimates up to NNLO+NNLL obtained using HRes tool within collinear factorization framework as well as with the ATLAS and CMS measurements of the corresponding differential distributions. This study will play an important role in understanding differential cross section within k_T -factorization framework.

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1. Introduction

The discovery of a 125 GeV candidate of the Standard Model (SM) Higgs boson by the ATLAS and CMS experiments [1, 2] opened a new plethora of studies. It has been established beyond doubt that the new particle is a spin-0 Higgs boson rather than a spin-2 particle [3]. In the minimal SM, the electroweak symmetry breaking is achieved via the Higgs mechanism through a single complex scalar doublet which leads to only one neutral physical scalar, *h*. Non-minimal models assume the existence of additional charged and neutral scalar Higgs particles. Hence on one hand we are concerned about its couplings to fermions and gauge bosons and the results seems to confirm consistency with the expected SM values so far [2]. On the other hand it opens the possibility to probe the production channel of the said Higgs boson. Here we are concerned with the latter aspect of the Higgs boson studies.

At the LHC conditions, the gluon-gluon fusion channel, $gg \to h$ is the most dominant one for the inclusive Higgs boson production [4]. Clearly, the gluon-gluon fusion to the Higgs production is strongly dependent on the gluon density $xf_g(x,\mu_F^2)$ in a proton which are usually described as a function of the Bjorken variable, x and hard scale, μ_F^2 within the framework of the DGLAP evolution equation [5]. The cross sections are calculated from the hard matrix elements convoluted with gluon density functions. This is the so called *collinear factorization* approach. However, at the LHC energies, it is more appropriate to use the parton densities which are explicit functions of it's transverse momentum, k_T [6] (the so called unintegrated, i.e., k_T dependent parton distribution functions or uPDFs in short). These parton densities are described by the BFKL evolution equation [7] for very small x or the CCFM evolution equation [8] which is valid for both small and large x^1 . As in the case of the collinear factorization, it is also possible to factorize the cross section into a convolution of the hard matrix elements and gluon uPDFs. However, in this case the matrix elements have to be taken off-shell and the convolution should also be over k_T . This generalized factorization is called k_T -factorization [9].

Recently the ATLAS and CMS collaborations at the LHC presented a measurement of fiducial differential cross section of the Higgs boson in the four-lepton decay channel [10, 11]. In particular, they presented a measurement of differential cross section in transverse momentum and rapidity of the Higgs boson decay into four-leptons. The measurements seems to be well in agreement with the theoretical calculation based on the collinear factorization approach with fixed order calculation up to the next to next leading order (NNLO) and including soft gluon resummation at small transverse momenta up to the next to next leading logarithm (NNLL). The k_T -factorization approach where the effect of intrinsic transverse momentum is taken into account has been a recent interest in the case of the Higgs boson production [12]. The k_T -factorization approach provides an advantage to understand an intrinsic dynamic of partons usually formulated in the form of uPDFs [13].

Here we have presented a study for the differential cross section of the Higgs boson in the four-lepton channel using k_T -factorization approach. We have used the CCFM evolution equations for the uPDFs. We have evaluated off-shell matrix element for the partonic subprocess $g^*g^* \to h \to ZZ \to 4\ell, \ell = e, \mu$. We presented our results for the differential cross section of the Higgs boson production in the four-lepton channel in the framework of k_T -factorization.

¹CCFM evolution is equivalent to BFKL evolution in the limit of very small x, whereas similar to the DGLAP evolution for large x and high μ_F^2

2. Formalism

To estimate differential cross section for the Higgs boson production in four-lepton decay channel, we have calculated off-shell matrix element for process $g^*g^* \to h \to ZZ \to 4\ell$. We have considered effective field theory approach in our calculation. Effective Lagrangian for the gluon coupling to the Higgs boson is

$$\mathcal{L}_{ggh} = \frac{\alpha_S}{12\pi} (\sqrt{2}G_F)^{1/2} G^a_{\mu\nu} G^{a\mu\nu} h, \tag{2.1}$$

where α_s and G_F are the strong coupling constant and Fermi coupling constant respectively. $G_{\mu\nu}^a$ is the gluon field strength tensor and h is the Higgs scalar field.

Triangle vertex for Hgg effective coupling in the infinite top mass limit is

$$T_{ggH}^{\mu\nu,ab}(k_1,k_2) = i\delta^{ab} \frac{\alpha_s}{3\pi} (\sqrt{2}G_F)^{1/2} \left[k_2^{\mu} k_1^{\nu} - (k_1 \cdot k_2) g^{\mu\nu} \right]. \tag{2.2}$$

Using Eq. (2.2) and considering transverse momentum of initial gluon to be non-zero $k_1^2 = -\mathbf{k}_{\perp 1}^2 \neq 0$ and $k_2^2 = -\mathbf{k}_{\perp 2}^2 \neq 0$ we derived matrix element for process $g^*(k_1)g^*(k_2) \to h \to ZZ \to \ell(p_1)\bar{\ell}(p_2)$ $\ell'(p_3)\bar{\ell}'(p_4)$. Matrix element we have obtained is

$$|\mathcal{M}|^{2} = \frac{2}{9} \frac{\alpha_{s}^{2}}{\pi^{2}} \frac{m_{Z}^{4}}{v^{4}} \frac{\left[(\mathbf{k}_{\perp 1} + \mathbf{k}_{\perp 2})^{2} + \hat{s} \right]^{2}}{(\hat{s} - m_{h}^{2})^{2} + \Gamma_{h}^{2} m_{h}^{2}} \cos^{2} \phi \times \frac{\left[(p_{1} \cdot p_{4})(p_{2} \cdot p_{3}) \left\{ 2g_{L}^{2}g_{R}^{2} \right\} + (p_{1} \cdot p_{3})(p_{2} \cdot p_{4}) \left\{ g_{L}^{4} + g_{R}^{4} \right\} \right]}{\left[(2p_{1} \cdot p_{2} - m_{Z}^{2})^{2} + \Gamma_{Z}^{2} m_{Z}^{2} \right] \left[(2p_{3} \cdot p_{4} - m_{Z}^{2})^{2} + \Gamma_{Z}^{2} m_{Z}^{2} \right]}, \quad (2.3)$$

and

$$g_L = \frac{g_W}{\cos \theta_W} \left(-\frac{1}{2} + \sin^2 \theta_W \right), \qquad g_R = \frac{g_W}{\cos \theta_W} \sin^2 \theta_W, \quad \text{and} \quad v = (\sqrt{2}G_F)^{-1/2}, \tag{2.4}$$

where Γ_h and Γ_Z are total decay width of the Higgs boson and Z boson respectively. $k_{\perp 1}$ and $k_{\perp 2}$ are intrinsic transverse momentum of the initial gluons. ϕ is the azimuthal angle between transverse momentum of the initial gluons $\mathbf{k}_{\perp 1}$ and $\mathbf{k}_{\perp 2}$. m_Z and m_h are the Higgs boson and Z boson masses respectively. Partonic center of mass energy is denoted by \hat{s} . θ_W and g_W are weak mixing angle and coupling of weak interaction respectively.

The summation over polarization of off-shell initial gluon considered according to k_T -factorization prescription is

$$\sum \varepsilon^{\nu} \varepsilon^{*\mu} = \frac{\mathbf{k}_{\perp}^{\mu} \mathbf{k}_{\perp}^{\nu}}{\mathbf{k}_{\perp}^{2}}.$$
 (2.5)

Within the framework of k_T -factorization, cross section for the process $p(P_1) + p(P_2) \rightarrow h \rightarrow ZZ \rightarrow \ell(p_1)\bar{\ell}(p_2)\ell'(p_3)\bar{\ell}'(p_4)$ is written as

$$\sigma = \int \frac{dx_1}{x_1} \frac{dx_2}{x_2} \frac{d^2 \mathbf{k}_{\perp 1}}{\pi} \frac{d^2 \mathbf{k}_{\perp 2}}{\pi} \frac{1}{x_1 x_2 s(2^{12})(\pi)^8} \frac{d^3 p_1}{2 p_{10}} \frac{d^3 p_2}{2 p_{20}} \frac{d^3 p_3}{2 p_{30}} \frac{d^3 p_4}{2 p_{40}} \times |\mathcal{M}|^2 \delta^4(k_1 + k_2 - p_1 - p_2 - p_3 - p_4) f_g(x_1, \mathbf{k}_{\perp 1}^2) f_g(x_2, \mathbf{k}_{\perp 2}^2).$$
(2.6)

Simplifying Eq. (2.6) we obtained our final expression for cross section as

$$\sigma = \int dy_1 dy_2 dy_3 dy_4 d\mathbf{p}_{1T}^2 d\mathbf{p}_{2T}^2 d\mathbf{p}_{3T}^2 d\mathbf{k}_{\perp 1}^2 d\mathbf{k}_{\perp 2}^2 \frac{d\phi_1}{2\pi} \frac{d\phi_2}{2\pi} \times \frac{1}{(2^{12})\pi^5 (x_1 x_2 s)^2} |\mathcal{M}|^2 f_g(x_1, \mathbf{k}_{\perp 1}^2) f_g(x_2, \mathbf{k}_{\perp 2}^2),$$
(2.7)

with longitudinal momentum fraction x_1 and x_2 of initial gluons are

$$x_1 = \frac{|\mathbf{p}_{1T}|}{\sqrt{s}} e^{y_1} + \frac{|\mathbf{p}_{2T}|}{\sqrt{s}} e^{y_2} + \frac{|\mathbf{p}_{3T}|}{\sqrt{s}} e^{y_3} + \frac{|\mathbf{p}_{4T}|}{\sqrt{s}} e^{y_4}, \tag{2.8}$$

$$x_2 = \frac{|\mathbf{p}_{1T}|}{\sqrt{s}} e^{-y_1} + \frac{|\mathbf{p}_{2T}|}{\sqrt{s}} e^{-y_2} + \frac{|\mathbf{p}_{3T}|}{\sqrt{s}} e^{-y_3} + \frac{|\mathbf{p}_{4T}|}{\sqrt{s}} e^{-y_4}, \tag{2.9}$$

and

$$\mathbf{k}_{\perp 1} + \mathbf{k}_{\perp 2} = \mathbf{p}_{1T} + \mathbf{p}_{2T} + \mathbf{p}_{3T} + \mathbf{p}_{4T}, \tag{2.10}$$

where ϕ_1 and ϕ_2 are the azimuthal angle of $\mathbf{k}_{\perp 1}$ and $\mathbf{k}_{\perp 2}$ respectively. y and p_T are rapidity and transverse momentum of the final state leptons. Hadronic center of mass energy is denoted by s.

We have calculated cross section for the Higgs boson decay as a function of rapidity of four-leptons (y) and transverse momentum of the four-leptons (p_T) . We have used Eq. (2.7) together with off-shell matrix element given in Eq. (2.3) for process $g^*g^* \to h \to ZZ \to 4\ell$, $\ell = e, \mu$, to calculate differential cross section.

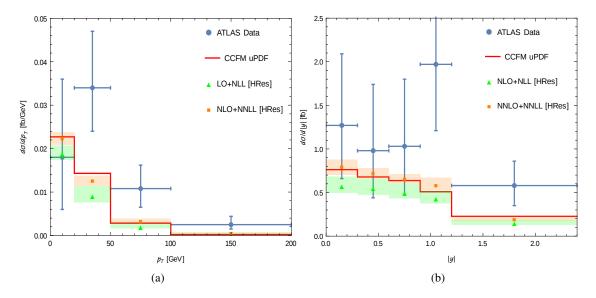


Figure 1: Differential cross section of the Higgs boson production in four-lepton decay channel at $\sqrt{s} = 8$ TeV. (a) and (b) are the differential distributions in transverse momentum of the four-leptons (p_T) and rapidity (y) of the four-leptons respectively. Solid line (red) is a results obtained using k_T -factorization approach with CCFM gluon uPDFs. Filled triangle and filled square points corresponds to estimated obtained using HRes tool up to NNLO+NNLL accuracy and shaded region corresponds to scale uncertainty in renormalization and factorization scale. Experimental data points are from ATLAS. The error bars on the data points shows total (statistical \oplus systematic) uncertainty.

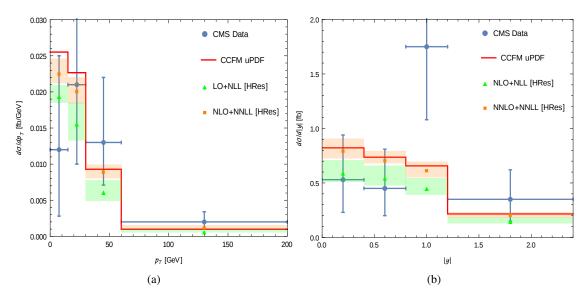


Figure 2: Differential cross section of the Higgs boson production in four-lepton decay channel at $\sqrt{s} = 8$ TeV. (a) and (b) are the plots of differential distributions in transverse momentum of the four-leptons (p_T) and rapidity (y) of the four-leptons respectively. Solid line (red) is a results obtained using k_T -factorization approach with CCFM gluon uPDFs. Filled triangle and filled square points corresponds to estimated obtained using HRes tool up to NNLO+NNLL accuracy and shaded region corresponds to scale uncertainty in renormalization and factorization scale. Experimental data points are from CMS. The error bars on the data points shows total (statistical \oplus systematic) uncertainty

3. Numerical Estimates

We have calculated differential cross section for the Higgs boson decay into four leptons at $\sqrt{s} = 8$ TeV. Total decay width and mass of the Higgs boson is set to be equal to 4.0 MeV and 125.09 GeV respectively [14]. Our results are compared with recent experimental data from AT-LAS and CMS collaborations [10, 11]. We have also compared our estimates with a results obtained using HRes tool [15] which gives a fixed order cross section calculated up to next to next to leading order plus next to next leading logarithm (NNLO+NNLL) accuracy within collinear factorization formalism.

In Figure 1, we have given an estimates obtained using k_T -factorization approach to compare with the ATLAS measurements [10]. Our results obtained using k_T factorization are close to NNLO+NNLL results obtained using HRes tool. We have done a comparison for both p_T and y differential distribution. In Figure 2, our results are compared for CMS experiment [11]. We see a similar behaviour in the comparison with the data from the CMS experiment as well. Our results are consistently close to NNLO+NNLL results which are fixed order calculation within collinear factorization approach. This can be explained considering the fact that the main part of higher order corrections included in the k_T -factorization approach [12].

4. Conclusion

Here we have presented our results of the differential cross section for the Higgs boson produc-

tion within k_T -factorization approach. We have compared our results with the fixed order estimates up to the order NNLO+NNLL within collinear factorization obtained using HRes tool. We have plotted our results against recent experimental measurements of the differential cross section for the Higgs boson production in four-lepton decay channel from the ATLAS and CMS Collaborations. In summary, we have done a phenomenological study for the case of the Higgs boson production in the four-lepton decay channel considering the framework of k_T -factorization. In this phenomenological study we have used CCFM unintegrated parton densities.

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