Radio Supernovae and GRB 980425

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Study of radio supernovae (RSNe) over the past 20 years includes two dozen detected objects and more than 100 upper limits. From this work we are able to identify classes of radio properties, demonstrate conformance to and deviations from existing models, estimate the density and structure of the circumstellar material and, by inference, the evolution of the presupernova stellar wind, and reveal the last stages of stellar evolution before explosion. It is also possible to detect ionized hydrogen along the line of sight, to demonstrate binary properties of the stellar system, and to show clumpiness of the circumstellar material. More speculatively, it may be possible to provide distance estimates to radio supernovae.

The interesting and unusual radio supernova SN 1998bw, which is thought to be related to the γ-ray burst GRB 980425, is discussed in particular detail. Its radio properties are compared and contrasted with those of other known RSNe.

1. Introduction

A series of papers published over the past 20 years on radio supernovae (RSNe) has established the radio detection and/or radio evolution for approximately two dozen objects: 2 Type Ib supernovae (SNe), 5 Type Ic SNe, and the rest Type II SNe. A much larger list of more than 100 additional SNe have low radio upper limits (Table 1).

In this extensive study of the radio emission from SNe, several effects have been noted: 1) Type Ia SNe are not radio emitters to the detection limit of the VLA \dagger ; 2) Type Ib/c SNe are radio luminous with steep spectral indices (generally $\alpha < -1$; $S \propto \nu^{+\alpha}$) and a fast turn-on/turn-off, usually peaking at 6 cm near or before optical maximum; and 3) Type II SNe show a range of radio luminosities with flat spectral indices (generally $\alpha > -1$) and a relatively slow turn-on/turn-off, usually peaking at 6 cm significantly after optical maximum. Type Ib/c may be fairly homogeneous in their radio properties, while Type II, as in the optical, are quite diverse.

There are a large number of physical properties of SNe which we can determine from radio observations. VLBI imaging shows the symmetry of the explosion and the local CSM, estimates the speed and deceleration of the SN shock propagating outward from the explosion and, with assumptions of symmetry and optical line/radio sphere veloci-

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ties, allows independent distance estimates to be made (see, *e.g.,* [Marcaide](#page-18-0) *et al.* 1997, [Bartel](#page-17-0) *et al.* 1985).

Measurements of the multi-frequency radio light curves and their evolution with time show the density and structure of the CSM, evidence for possible binary companions, clumpiness or filamentation in the presupernova wind, mass-loss rates and changes therein for the presupernova stellar system and, through stellar evolution models, estimates of the ZAMS presupernova stellar mass and the stages through which the star passed on its way to explosion. It has also been proposed by Weiler *et al.* (1998) that the time from explosion to 6 cm radio maximum may be an indicator of the radio luminosity and thus an independent distance indicator.

A summary of the radio information on SNe can be found at *[http://rsd-www.nrl.navy.](http://rsd-www.nrl.navy.mil/7214/weiler/sne-home.html) [mil/7214/weiler/sne-home.html](http://rsd-www.nrl.navy.mil/7214/weiler/sne-home.html)*.

2. Models

All known RSNe appear to share common properties of: 1) nonthermal synchrotron emission with high brightness temperature; 2) a decrease in absorption with time, resulting in a smooth, rapid turn-on first at shorter wavelengths and later at longer wavelengths; 3) a power-law decline of the flux density with time at each wavelength after maximum flux density (optical depth ≈ 1) is reached at that wavelength; and 4) a final, asymptotic approach of spectral index α to an optically thin, nonthermal, constant negative value([Weiler](#page-19-0) *et al.* 1986, [Weiler, Panagia, & Sramek 1990\)](#page-19-0). Chevalier (1982a,b)

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has proposed that the relativistic electrons and enhanced magnetic field necessary for synchrotron emission arise from the SN shock interacting with a relatively high density circumstellar medium (CSM) which has been ionized and heated by the initial $UV/X-ray$ flash. This CSM is presumed to have been established by a constant mass-loss (M) rate, constant velocity (w) wind (*i.e.*, $\rho \propto r^{-2}$) from a red supergiant (RSG) progenitor or companion. This ionized CSM is also the source of the initial absorption. A rapid rise in the observed radio flux density results from the shock overtaking more and more of the wind material, leaving progressively less of it along the line of sight to the observer to absorb the more slowly decreasing synchrotron emission from the shock region.

2.1. *Parameterized Radio Light Curves*

The parameterized model of Weiler *et al.* (1986), Weiler, Panagia, & Sramek (1990), and Montes, Weiler, & Panagia (1997) may be written as:

$$
S(\text{mJy}) = K_1 \left(\frac{\nu}{5 \text{ GHz}}\right)^{\alpha} \left(\frac{t - t_0}{1 \text{ day}}\right)^{\beta} e^{-\left(\tau + \tau''\right)} \left(\frac{1 - e^{-\tau'}}{\tau'}\right),\tag{2.1}
$$

where

$$
\tau = K_2 \left(\frac{\nu}{5 \text{ GHz}}\right)^{-2.1} \left(\frac{t - t_0}{1 \text{ day}}\right)^{\delta},\tag{2.2}
$$

$$
\tau' = K_3 \left(\frac{\nu}{5 \text{ GHz}}\right)^{-2.1} \left(\frac{t - t_0}{1 \text{ day}}\right)^{\delta'},\tag{2.3}
$$

and

$$
\tau'' = K_4 \left(\frac{\nu}{5 \text{ GHz}}\right)^{-2.1}.\tag{2.4}
$$

 K_1 , K_2 , and K_3 correspond, formally, to the unabsorbed flux density (K_1) , and the uniform (K_2) and non-uniform (K_3) optical depths in the surrounding CSM at 5 GHz one day after the explosion date t_0 . K_4 represents a non-time dependent HII absorption along the line-of-sight to the radio emitting region (EM = $8.93 \times 10^7 K_4 [T_e/10^4 K]^{1.35}$ pc cm⁻⁶, where T_e is the electron temperature of the ionized absorbing region; Eq. 1 – 223 of Lang 1986). The term $e^{-\tau}$ describes the attenuation of a local medium with optical depth τ and time dependence δ that uniformly covers the emitting source ("uniform external absorption"); the term $(1 - e^{-\tau'}) \tau'^{-1}$ describes the attenuation produced by an inhomogeneous medium with optical depths distributed between 0 and τ' ("clumpy absorption") and time dependence δ' ; and the term $e^{-\tau''}$ describes an absorption along the line-of-sight which is sufficiently far removed from the radio generating region to be constant with time. All absorbing media are assumed to be purely thermal, ionized hydrogen with opacity $\propto \nu^{-2.1}$.

A cartoon of the expected structure of the SN and its surrounding media is presented in Fig. 1. The radio emission is expected to arise near the outgoing shock ([Chevalier & Fransson 1994\)](#page-17-0).

3. Results

The success of the basic parameterization and model description can be seen in the relatively good correspondence between the model fits and the data for all three subtypes

Figure 1. Cartoon, not to scale, of the SN and its shocks along with the stellar wind established CSM and more distant ionized material. The radio emission is thought to arise near the outgoing shock with the expected location of the several absorbing terms in Eqs. $2.2 - 2.4$ illustrated.

Figure 2. Type Ib SN 1983N at 6 cm (4.9 GHz; squares, solid line) and 20 cm (1.5 GHz; stars, dashed line).

of RSNe, *e*.*g*., Type Ib SN 1983N (Fig. 2), Type Ic SN 1990B (Fig. 3), and Type II SN 1979C (Fig. 4a) and SN 1980K (Fig. 4b). (Note that after day ∼ 4000, the evolution of the radio emission from both SN 1979C and SN 1980K deviates from the expected model evolution; see §4 for discussion of these changes.)

Figure 3. Type Ic SN 1990B at 3.4 cm (8.4 GHz; circles, solid line), 6 cm (4.9 GHz; squares, dashed line), and 20 cm (1.5 GHz; stars, dash-dot line) .

FIGURE 4. Shown are the radio light curves of Type II SN 1979C (Fig. 4a, left) at 6 cm (circles) and 20 cm (crosses) as observed over a period of about 18 years together with the best-fit model curves (solid and dashed curves, respectively). The model light curves for SN 1979C include the effects due to a possible binary companion in an eccentric orbit (Weiler et al. 1991, 1992a). Note the increase in flux density of SN 1979C, with respect to the expected, continuing decline, starting at ∼4300 days (Montes et al. 2000). Also shown, with the same notation at the same frequencies, are the radio light curves of Type II SN 1980K (Fig. 4b, right). Note the sudden drop in the flux density of $\overline{S}N$ 1980K, with respect to the expected, continuing decline, which occurs at ∼3700 days (Montes et al. 1998).

3.1. *Mass-loss Rate & Change in Mass-loss Rate*

From the Chevalier (1982a,b) model, the turn-on of the radio emission for RSNe provides a measure of the presupernova mass-loss-rate to stellar-wind-velocity ratio. Using the formulation of Weiler *et al.* (1986; Eq. 16), we can write

FIGURE 5. Mass-loss rate of the presumed red supergiant progenitor to SN 1993J vs. time before the explosion (Van Dyk et al. 1994).

$$
\frac{\dot{M}(M_{\odot} \text{ yr}^{-1})}{(w/10 \text{ km s}^{-1})} = 3 \times 10^{-6} K_2^{0.5} m^{-1.5} \left(\frac{v_i}{10^4 \text{ km s}^{-1}}\right)^{1.5} \left(\frac{1}{45 \text{ days}}\right)^{1.5m} \left(\frac{T}{10^4 \text{ K}}\right)^{0.68} (3.5)
$$

where \dot{M} is the presupernova mass-loss rate, w is the presupernova wind velocity, K_2 is the same as in Eq. 2.2, m is the SN shock deceleration index (shock radius $\propto t^m$), v_i is the initial SN shock velocity ($\sim 13,000 \text{ km s}^{-1}$), and T is the temperature of the circumstellar material $(\sim 30,000 \text{ K})$.

From Eq. 3.5 the mass-loss rates from SN progenitors are generally estimated to be $\sim 10^{-6}$ M_☉ yr⁻¹ for Type Ib/c SNe and $\sim 10^{-4}$ M_☉ yr⁻¹ for Type II SNe. For the specific case of SN 1993J, where detailed radio observations are available starting just a few days after explosion, Van Dyk *et al.* (1994) find evidence for a changing massloss rate (Fig. 5) for the presupernova star, which was as high as $\sim 10^{-4}$ M_☉ yr⁻¹ approximately 1000 years before explosion and decreased to $\sim 10^{-5}$ M_☉ yr⁻¹ just before explosion. Recently Fransson $&$ Björgsson (1998) have shown that the observed behavior of the free-free absorption for SN 1993J could alternatively be explained in terms of a systematic decrease of the electron temperature in the circumstellar material as the SN expands. It is not clear, however, what the physical process is which determines why such a cooling occurs efficiently in some SNe and not in others.

3.2. *Clumpiness of the Presupernova Wind*

In their study of the radio emission from SN 1986J, Weiler, Panagia, & Sramek (1990) found that the simple Chevalier (1982a,b) model could not describe the relatively slow turn-on. They therefore added terms described mathematically by τ' in Eqs. 2.1 and 2.3. This extension greatly improved the quality of the fit and was interpreted by Weiler, Panagia, & Sramek (1990) to represent the possible presence of filamentation or clumpiness in the CSM.

Such a clumpiness in the wind material was again required for modeling the radio data from SN 1988Z [\(Van Dyk](#page-18-0) *et al.* 1993) and SN 1993J([Van Dyk](#page-18-0) *et al.* 1994). Since that

time, evidence for filamentation in the envelopes of SNe has also been found from optical and UV observations [\(Filippenko, Matheson, & Barth 1994,](#page-17-0) [Spyromilio 1994\)](#page-18-0).

3.3. *Binary Systems*

In the process of analyzing a full decade of radio measurements from SN 1979C, Weiler *et al.* (1991, 1992a) found evidence for a significant, quasi-periodic, variation in the amplitude of the radio emission at all wavelengths of \sim 15 % with a period of 1575 days or \sim 4.3 years (see Fig. 4a at age <4300 days). They interpreted the variation as due to a minor ($\sim 8\%$) density modulation, with a period of ~ 4000 years, on the larger, relatively constant presupernova stellar mass-loss rate. Since such a long period is inconsistent with most models for stellar pulsations, they concluded that the modulation may be produced by interaction of a binary companion in an eccentric orbit with the stellar wind from the presupernova RSG. This concept was strengthened by more detailed calculations for a binary model from Schwarz & Pringle (1996). Since that time, the presence of binary companions has been suggested for the progenitors of SN 1993J [\(Podsiadlowski](#page-18-0) *et al.* 1993) and SN 1994I [\(Nomoto](#page-18-0) *et al.* 1994), indicating that binaries may be common in presupernova systems.

3.4. *HII Along the Line-of-Sight*

A reanalysis of the radio data for SN 1978K from Ryder *et al.* (1993) clearly shows flux density evolution characteristic of normal Type II SNe. Additionally, the data indicate the need for a time-independent, free-free absorption component along the line-of-sight. Montes, Weiler, & Panagia (1997) interpret this constant absorption term as indicative of the presence of HII along the line-of-sight to SN 1978K, perhaps a part of an HII region or a distant circumstellar shell associated with the SN progenitor. SN 1978K had already been noted for its lack of optical emission lines broader than a few thousand km s[−]¹ since its discovery in 1990([Ryder](#page-18-0) *et al.* 1993), indeed suggesting the presence of slowly moving circumstellar material.

To determine the nature of this absorbing region, a high-dispersion spectrum of SN 1978K at the wavelength range $6530 - 6610$ Å was obtained by Chu *et al.* (1999). The spectrum shows not only the moderately broad $H\alpha$ emission of the supernova ejecta, but also narrow nebular H α and [N II] emission. The high [N II] 6583/H α ratio of 0.8 – 1.3 suggests that this radio absorbing region is a stellar ejecta nebula. The expansion velocity and emission measure of the nebula are consistent with those seen in ejecta nebulae of luminous blue variables. Previous low-dispersion spectra have detected a strong [N II] 5755Å line, indicating an electron density of $(3-12) \times 10^5$ cm⁻³. These data suggest that the ejecta nebula detected towards SN 1978K is probably part of the pre-shock dense circumstellar envelope of SN 1978K. Another possible example of this type of system may be SN 1997ab, which looks in its optical spectrum like a young version of SN 1978K.

4. Rapid Pre-Supernova Stellar Evolution

SN radio emission that preserves its spectral index while deviating from the standard model is taken to be evidence for a change of the average circumstellar density behavior from the canonical r^{-2} law expected for a pre-SN wind with a constant mass-loss rate, \dot{M} , and a constant wind velocity, w. Since the radio luminosity of a SN is proportional to $(\dot{M}/w)^{(\gamma-7+12m)/4}$ [\(Chevalier 1982a\)](#page-17-0) or, equivalently, to the same power of the circumstellar density (since $\rho_{\text{CSM}} \propto M/w$), a measure of the deviation from the standard model provides an indication of deviation of the circumstellar density from the r^{-2} law. Monitoring the radio light curves of RSNe also provides a rough estimate of the time scale of deviations in the presupernova stellar wind density. Since the SN shock travels through the CSM roughly 1000 times faster than the stellar wind velocity which established the CSM ($v_{\text{shock}} \sim 10,000 \text{ km s}^{-1}$ vs. $w_{\text{wind}} \sim 10 \text{ km s}^{-1}$) one year of radio light curve monitoring samples roughly 1000 years of stellar wind mass-loss history.

4.1. *Radio Evidence for CSM Structure*

SN 1979C (Type IIL) prior to 1991 (age <4300 days; \sim 12 years) follows a standard, albeit sinusoidally modulated, declining radio emission (see $\S 3.3$). However, for age >4300 days a slow increase in the radio light curve occurs at all wavelengths (see Fig. 4a). By day ∼ 7100, this change in evolution implies an *excess* in flux density by a factor of \sim 1.7 with respect to the standard model, or a density enhancement by a factor of \sim 1.34 over the expected density at that radius. This may be understood as a change of the average CSM density profile from the r^{-2} law which was applicable until day ~4300, to an appreciably flatter behavior of $\sim r^{-1.4}$ ([Montes](#page-18-0) *et al.* 2000).

SN 1980K (Type IIL) prior to epoch \sim 3700 days (\sim 10 years) is also well behaved. However, more recent measurements show a steep *decline* in flux density at all wavelengths by a factor of \sim 2 occurring between day \sim 3700 and day \sim 4900 (see Fig. 4b). Such a sharp decline in flux density implies a *decrease* in ρ_{CSM} by a factor of ~ 1.6 below that expected for a r^{-2} CSM density profile [\(Montes](#page-18-0) *et al.* 1998).

SN 1988Z (Type IIn), similarly to SN 1980K, shows a sharp drop in its flux density with respect to its expected radio evolution at an age of a few thousand days (several years). Although the parameters of the change are yet to be quantified, it appears to also have evolved rapidly in the last several thousand years before explosion ([Lacey](#page-18-0) *et al.* 2000).

SN 1987A (Type II) is the best studied RSN because its proximity makes it easily detectable even at very low radio brightness. The progenitor to SN 1987A was in a blue supergiant (BSG) phase at the time of explosion and had ended a RSG phase some ten thousand years earlier. After an initial, very rapidly evolving radio outburst ([Turtle](#page-18-0) *et al.* 1987) which reached a peak flux density at 6 cm \sim 3 orders-of-magnitude fainter than other known Type II RSNe (presumably due to sensitivity limited selection effects), the radio emission declined to a low radio brightness within a year. However, at an age of ∼ 3 years the radio emission started increasing again and continues to increase at the present time (see Ball *[et al.](#page-17-0)* 1995, [Gaensler](#page-17-0) *et al.* 1997). Although its extremely rapid development resulted in the early radio data at higher frequencies being almost non-existent, the evolution of the initial radio outburst is roughly consistent with the models described above in Eqs. $2.1 - 2.4$ (*i.e.*, a shock front expanding into a spherically symmetric circumstellar envelope). The density implied by such modeling is appropriate to a pre-SN mass-loss rate of $\sim 10^{-7}$ M_☉ yr⁻¹ for a wind velocity of ~ 150 km s⁻¹. Because the Hubble Space Telescope (HST) can actually image the denser regions of the CSM around SN 1987A, we know that the current rise in radio flux density is caused by the interaction of the SN shock with the diffuse material at the inner edge of the well known inner circumstellar ring [\(Gaensler](#page-17-0) *et al.* 1997). Since the density increases as the SN shock interaction region moves deeper into the main body of the optical ring, the flux density is expected to continue to increase steadily at all wavelengths. Recently, increases at optical and X-ray have also been reported ([Garnavich, Kirshner, & Challis 1997, Hasinger, Aschenbach, & Truemper 1996\)](#page-17-0). Best estimates are that the shock/CSM interaction will reach a maximum by \sim 2003.

4.2. *Discussion of CSM Structure*

For at least four supernovae, namely SN 1979C, SN 1980K, SN 1988Z, and SN 1987A, we have significant changes in radio flux density occurring a few years after the explosion. Since the SN shock is moving about 1000 times faster than the wind material of the RSG progenitor (*i.e.*, $\sim 10,000 \text{ km s}^{-1}$ vs. $\sim 10 \text{ km s}^{-1}$), such a time interval implies a significant change in the pre-supernova stellar wind properties several thousand years before the explosion. Such an interval is short compared to the lifetimes of typical RSN progenitors (say, $10 - 30$ Myrs) but is a sizeable fraction of its red supergiant phase $(t_{RSG} \sim 2-5 \times 10^5 \text{ yrs})$, suggesting that a significant transition occurs in the evolution of pre-supernova stars just before the final explosive event.

Since the radio emission is determined by the mass-loss-rate to stellar-wind-velocity ratio (M/w) , one of these quantities, or both are required to change by as much as a factor of 2 over the last few thousand years before the SN explosion. Such a time is too short (for H and He burning), or too long (for C and heavier element burning) to correspond to any of the known nuclear burning phases and, therefore, it is unlikely that the stellar luminosity (which determines the mass-loss rate, $\dot{M} \propto L^{1-1.5}$) can vary on a time scale needed to account for the observed changes.

On the other hand, the wind velocity, w , is roughly proportional to the square of the effective temperature ($w \propto T_{\text{eff}}^2$, *e.g.*, [Panagia & Macchetto 1982\)](#page-18-0) so that a change of a factor of ~ 2 in w requires a change of a factor of only ~ 1.4 in T_{eff} , *e.g.*, from $\sim 3,500$ K to \sim 5,000 K or, correspondingly, a change from an early M to an early K supergiant spectrum. Such a transition would define a loop in the HR diagram reminiscent of the blue loops which are characteristic of the evolution of moderately massive stars (*e.g.,* [Brocato & Castellani 1993](#page-17-0), [Langer & Maeder 1995\)](#page-18-0). However, the apparent transition implied by these CSM density changes cannot be classical blue loops, since classical blue loops are much slower and more extreme processes occurring several $\times 10^5$ years before the terminal stages of an RSG and involving temperature excursions from $\sim 3,500$ K to $> 10,000$ K.

The smaller temperature changes which we infer from the radio data require a star to change only from a very red to a moderately red spectrum, and back, corresponding to a transition in the HR diagram which is more appropriately dubbed a *"pink loop."* The cause of such loops is not obvious, but may be similar to the not-so-well understood phenomenon that caused the SN 1987A progenitor to move in the HR diagram from being a red supergiant to a blue supergiant some $10⁴$ years before explosion.

Another possibility for explaining these implied CSM density changes around at least some presupernova stars derives from a recent study by Panagia & Bono (this Conference). They find from modeling that the pulsational instability of stars in the mass range $10 - 20$ M_{\odot} may, in some cases, be of suitable period and magnitude to account for the changes of the pre-supernova mass-loss rates implied by radio observations of RSNe.

5. Peak Radio Luminosities and Distances

Our long-term monitoring of the radio emission from supernovae shows that the radio "light curves" evolve in a systematic fashion with a distinct peak flux density (and thus, in combination with a distance, a peak spectral luminosity) at each frequency and a well-defined time from explosion to that peak. Studying these two quantities at 6 cm wavelength, peak spectral luminosity ($L_{6 \text{ cm peak}}$) and time after explosion date (t_0) to reach that peak $(t_{6 \text{ cm peak}} - t_0)$, we find that they appear related (Fig. 6; see also

FIGURE 6. Peak 6 cm luminosity, $L_{6 \text{ cm peak}}$, of RSNe vs. time, in days, from explosion to peak 6 cm flux density ($t_{6 \text{ cm peak}} - t_0$) for Type II SNe. The *dashed line* (given by Eq. 5.6 in the text) is the unweighted, best fit to the 12 available Type II RSNe. Error bars are based on best estimates. Where no error or only a stub of a line is shown, the error in that direction is indeterminate (from Weiler et al. 1998).

[Weiler](#page-19-0) *et al.* 1998). In particular, based on twelve objects, Type II supernovae appear to obey a relation

$$
L_{6 \text{ cm peak}} \simeq 5.5 \times 10^{23} \ (t_{6 \text{ cm peak}} - t_0)^{1.4} \ \text{erg s}^{-1} \text{Hz}^{-1}
$$
 (5.6)

with time measured in days. Thus, if this relation is supported by further observations, it provides a means for determining distances to supernovae, and thus to their parent galaxies, from purely radio continuum observations.

Although there are still relatively few objects to which this techniques can be applied, RSNe could eventually provide a powerful and independent technique for investigating the long-standing problem of distance estimates in astronomy. With such intrinsically bright Type II RSNe as SN 1988Z and SN 1986J, the technique can be applied to distances of at least 100 Mpc with current VLA technology. With future sensitivity improvements and planned, new, more sensitive radio telescopes, the technique could be extended to large distances, even for less luminous RSNe. For example, with a sensitivity of $1 \mu Jy$, a SN of the same class as SNe 1988Z and 1986J could be detected to a redshift of ~ 1 , while a relatively radio faint Type II SN, such as SN 1980K, could be studied to a redshift of $> 0.1.$

6. Sphericity of an SN explosion

It has often been suggested that SN explosions are non-spherical, and there is evidence in a number of stellar systems for jets, lobes, and other directed mass-loss phenomena. Also, the presence of polarization in the optical light from SNe (including SN 1993J) has been interpreted for non-sphericity (see, *e.g.,* [Hoeflich](#page-17-0) *et al.* 1996) and probably the most obvious evidence for non-spherical structure in an SN system is the very prominent inner ring around SN 1987A. However, our most direct evidence for the structure of at least

Figure 7. VLBI radio images of SN 1993J at 6 cm wavelength. Images on the left-hand side are normalized to the same peak brightness to emphasize structural changes. Images on the right-hand side are on a single brightness scale to illustrate the decrease in brightness with time (from Marcaide et al. 1997).

the shock wave from an SN explosion and the CSM with which it is interacting is from VLBI measurements on SN 1993J. A series of images taken by Marcaide and co-workers (Fig. 7; [Marcaide](#page-18-0) *et al.* 1997) over a period of two years from 1994 September through 1996 October show only a very regular ring shape indicative of a relatively spherical shock wave expanding into a relatively uniform CSM. The cause of such apparently conflicting results is still to be resolved.

7. Summary of RSN Studies

Arising from one of the most energetic phenomena in the Universe, the radio emission from supernovae appears to be relatively well understood in terms of shock interaction with a structured circumstellar medium as described by the Chevalier (1982a,b) model and its modifications [\(Weiler](#page-19-0) *et al.* 1986, [Weiler, Panagia, & Sramek 1990,](#page-19-0) and [Weiler](#page-19-0) *et al.* 1991). With this modeling, the radio emission can be used to estimate the circumstellar density, the pre-SN mass loss rate and changes therein, to show the existence of filamentation in the pre-SN stellar wind, to indicate the possible presence of binary companions, and to measure the symmetry of the explosion and the CSM with which it is interacting. More speculatively, radio observations may also lead to a more physical classification system for SNe and provide a new technique for estimating distances to SNe and their parent galaxies.

However, the recent suggestion of an association of the γ -ray burst GRB 980425 with the Type Ic supernova SN 1998bw provides evidence for yet a new phenomenon which may arise in at least some types of SN explosions. Since SN 1998bw is a strong radio emitter, it is important to consider how it compares with the known properties of RSNe discussed above.

8. Gamma-Ray Bursts and SN 1998bw

8.1. *Gamma-ray Burst Afterglows*

Gamma-ray bursts (GRBs) are "mysterious" flashes of high-energy radiation that appear from random directions in space and typically last a few seconds. They were first discovered by U.S. Air Force Vela satellites in the 1960s and, since then, numerous theories of their origin have been proposed. NASA's Compton Gamma-Ray Observatory (CGRO) satellite has detected several thousand bursts so far, with an occurrence rate of approximately one per day. The uniform distribution of the bursts on the sky has led theoreticians to suggest that their sources are either very near, and thus uniformly distributed around the solar system, are in an unexpectedly large halo around the Galaxy, or are at cosmological distances – not very restrictive proposals.

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The principal limitation to understanding the origin of the bursts has been the difficulty in pinpointing their direction on the sky in order to obtain the multi-wavelength observations necessary to constrain physical models. Gamma-rays are exceedingly difficult to focus on to a position sensitive detector, and the bursts' short duration exacerbates the problem. Only with the launch of the Italian/Dutch satellite BeppoSAX in 1996 has it been possible to couple a quick response pointing system with relatively high precision position sensitive detectors for γ -rays and hard X-rays. This quick response, high accuracy position information has finally permitted rapid and accurate follow-up observations with the world's powerful ground-based and space-based telescopes, and has led to the discovery of long-lived "afterglows" of the bursts in soft X-rays, visible and infrared light, and radio waves. Although the γ -ray bursts generally last only seconds, their afterglows have, in a few cases, been studied for minutes, hours, days, or even weeks after discovery. These longer wavelength observations have allowed observers to probe the immediate environment of γ -ray burst sources and to assemble clues as to their nature.

The first GRB related optical transient was identified for GRB 970228 by Groot *et al.* (1997) and followup with *HST* by Sahu *et al.* (1997) demonstrated that the GRB was associated with a faint (thus probably distant) late-type galaxy. A few months later Fruchter & Bergeron 1997; see also Pian *[et al.](#page-18-0)* 1998) imaged the afterglow of another γ-ray burst, GRB 970508, with the *HST WFPC2* finding this source to be associated with a late-type galaxy at a redshift of $z = 0.835$. GRB 970508 was also the first GRB to be detected in its radio afterglow([Frail & Kulkarni 1997](#page-17-0)).

Heise *et al.* (1997) detected the very energetic γ -ray burst GRB 971214 on 1997 December 14 with the BeppoSAX satellite and provided sufficient positional accuracy for Halpern *et al.* (1997) to identify a visible light afterglow using the KPNO 2.1 m telescope. As the visible light from the burst afterglow faded, an extremely faint galaxy ($R = 25.6 \pm$ 0.2) was detected at its position. Using the 10-meter Keck II telescope on Mauna Kea, Hawaii, Kulkarni *et al.* (1998a) measured a redshift of $z = 3.42$. Subsequent images taken with the *HST* ([Odewahn](#page-18-0) *et al.* 1998) confirmed the association of the burst afterglow and the redshift of this faint galaxy. For such a large distance, Odewahn *et al.* (1998) estimated that the amount of energy released in the γ-ray flash was extremely high, \sim 3×10^{53} erg. Thus, it appears that at least some GRB sources are very energetic explosions (hypernovae?; [Paczynski 1998,](#page-18-0) [Iwamoto](#page-17-0) *et al.* 1998) occurring at cosmological distances.

8.2. *GRB 980425 and SN 1998bw*

8.2.1. *Background*

While still generally accepted that "most" GRBs are extremely distant and energetic, the discovery of GRB 980425 [\(Soffitta](#page-18-0) *et al.* 1998) on 1998 April 25.90915 and its possible association with a bright supernova, SN 1998bw at $RA(J2000) = 19^h35^m03^s31$, Dec(J2000) = $-52°50'44''$. (Tinney *et al.* 1998), in the relatively nearby spiral galaxy ESO 184-G82 at $z = 0.0085$ (distance ~ 38 Mpc for $H_0 = 65$ km s⁻¹ Mpc⁻¹; Galama *et al.* 1998, [Lidman](#page-18-0) *et al.* 1998, [Tinney](#page-18-0) *et al.* 1998, [Sadler](#page-18-0) *et al.* 1998), has introduced the possibility of multiple origins for GRBs. The estimated explosion date of SN 1998bw in the interval 1998 April 21 – 27 [\(Sadler](#page-18-0) *et al.* 1998) corresponds rather well with the time of GRB 980425. Iwamoto *et al.* (1998) feel that they can restrict the core collapse date for SN 1998bw even more from hydrodynamical modeling of exploding $C + O$ stars and, assuming that the SN 1998bw optical light curve is generated by ⁵⁶Ni as in Type Ia SNe, they then restrict the coincidence between the core collapse of SN 1998bw to within $+0.7/-2$ days of the detection of GRB 980425.

Classified initially as an SN optical Type Ib([Sadler](#page-18-0) *et al.* 1998), then Type Ic (Patat & Piemonte 1998), then peculiar Type Ic (Kay, Halpern, & Leighly 1998, Filippenko

1998), then later, at an age of 300 - 400 days, again as a Type Ib([Patat](#page-18-0) *et al.* 1999), SN 1998bw presents a number of optical spectral peculiarities which strengthen the suspicion that it may be the counterpart of the γ -ray burst.

However, some doubt remains concerning the association of GRB 980425 with SN 1998bw. When the more precise BeppoSAX NFI was pointed at the BeppoSAX error box 10 hours after the detection of GRB 980425, two X-ray sources were present (Pian *[et al.](#page-18-0)* 1999). One of these, named S1 by Pian *et al.* (1999), is coincident with the position of SN 1998bw and declined slowly between 1998 April and 1998 November. The second X-ray source, S2, which was ~ 4' from the position of SN 1998bw, was, at best, only marginally detected at $\lt 3\sigma$ six days after the initial detection, and not detectable again in follow up observations in 1998 April, May, and November (Pian *[et al.](#page-18-0)* 1999). Even though the *a posteriori* statistics indicate a very low probability($\sim 10^{-4}$) of a GRB being nearly coincident in space and time with a SN outburst, the concern remains that the Pian source S2 was the brief afterglow from GRB 980425 rather than the Pian source S1 associated with SN 1998bw.

8.2.2. *Radio emission*

Since the peak absolute magnitude of Type Ib/c SN 1998bw, while bright at M_B \sim -19.5 is not much brighter than Type Ib SN 1966J ($M_{\rm B} \sim -19$, converted from $H_0 = 75$ km s⁻¹ Mpc⁻¹ to $H_0 = 65$ km s⁻¹ Mpc⁻¹, [Miller, & Branch 1990\)](#page-18-0) and less luminousthan the Type Ic SN 1992ar, with $M_B \sim -20$ ([Hamuy](#page-17-0) *et al.* 1992), much of the argument for the unusual nature of SN 1998bw rests on the radio observations. (N.B.: SN 1966J may have been misclassified. [Van Dyk, Hamuy, & Filippenko 1996](#page-18-0) indicate in a *Note Added in Proof* that D. Branch has reclassified SN 1966J as a Type Ia.)

The radio emission from SN 1998bw reached an unusually high 6 cm spectral luminosity at peak of $\sim 8 \times 10^{28}$ erg s⁻¹ Hz⁻¹, *i.e.*, about 3 times higher than any of the relatively well studied radio RSNe and $\sim 30 - 40$ times higher than a typical Type Ib/c SN at peak (see Table 2 and [Weiler](#page-19-0) *et al.* 1998). Unfortunately, it is not clear how significant is this "excess" radio luminosity, since only 6 other examples of radio emitting Type Ib/c SNe are known (see Table 1). Also, one must keep in mind that, contrary to the often stated opinion that SN 1998bw is "the most luminous radio supernova ever observed," SN 1998bw is still exceeded in peak 6 cm spectral luminosity by the poorly studied, presumed supernova, SN 1982aa [\(Green 1994\)](#page-17-0) in the starburst galaxy NGC 6052 (Markarian 297). SN 1982aa is estimated to have peaked at a 6 cm spectral luminosity of $\sim 1 \times 10^{29}$ erg s⁻¹ Hz⁻¹. Although SN 1982aa was not optically identified and, therefore, has no optical spectral type classification, its radio evolution strongly resembles that of Type II RSNe ([Yin 1994\)](#page-19-0).

Figure 8. Approximate model 6 cm luminosity vs. time "light" curves for radio supernovae (RSNe). Derived from best fits to observations, these model curves smooth out the many "bumps and wiggles" seen in actual data to show the general character of the time evolution rather than the details. Both Type Ib/c (SN 1983N, SN 1994I, SN 1998bw) and Type II (SN 1979C, SN 1982aa, SN 1986J, SN 1987A, SN 1993J) SNe are shown.

As a further check for unusual characteristics of SN 1998bw, we can compare a smoothed 6 cm light curve for SN 1998bw with model 6 cm light curves for other RSNe. This is illustrated in Fig. 8. Inspection of the figure shows that SN 1998bw is unusual in its radio emission, but not extreme. For example, the time from explosion to peak 6 cm luminosity for both SN 1987A and SN 1983N was faster and, as mentioned above, the 6 cm spectral luminosity of SN 1998bw at peak is exceeded by that of SN 1982aa. However, as is clear from Fig. 8, SN 1998bw is the most luminous Type Ib/c RSN ever observed by a factor of ∼ 30, and it reached a higher radio luminosity earlier than any RSN known.

8.2.3. *Brightness temperature*

Although unique in neither the speed of evolution nor in radio luminosity, SN 1998bw is certainly unusual in the combination of these two factors – very radio luminous very soon after explosion. Kulkarni *et al.* (1998b,c) have used these observed qualities, together with the lack of interstellar scintillation at early times, brightness temperature estimates, and physical arguments to conclude that the shock wave from SN 1998bw giving rise to the radio emission must have been expanding relativistically. On the other hand, Waxman & Loeb (1999) argue that a sub-relativistic shock can generate the observed radio emission. However, both sets of authors agree that a very high expansion velocity $(\geq 0.3c)$ is required for the radio emitting region under a spherical geometry.

Simple arguments confirm this high velocity since, to avoid the well-known "Compton Catastrophe," Kellermann & Pauliny-Toth (1969) have shown that $T_{\rm B} < 10^{12}$ K must hold, and Readhead (1994) has better defined this limit to $T_B < 10^{11.5}$ K. From geometrical arguments, such a limit requires the radiosphere of SN 1998bw to have expanded at $\geq 200,000$ km s⁻¹, at least during the first few days after explosion. While such a value is still only mildly relativistic ($\gamma \sim 1.5$), it seems very high. However, measurements by Gaensler *et al.* (1997) have demonstrated that the radio emitting regions of SN 1987A have expanded at an *average* velocity of $\sim 35,000 \text{ km s}^{-1}$ over the 3 years

FIGURE 9. A plot of the 6 cm luminosity at peak vs. the time to reach that peak for all of the known RSNe. The individual RSNe are labeled and their types are indicated by their symbols; Type Ib, filled squares, Type Ic, filled diamonds, and Type II filled triangles. The lines of constant expansion velocity are shown for a brightness temperature of $10^{11.5}$ K.

from 1987 February to mid-1990, so that, in a very low density environment such as one finds around Type Ib/c SNe, very high shock velocities may be possible.

This is illustrated graphically in Fig. 9 where, for an adopted brightness temperature of $10^{11.5}$ K, the lines of constant expansion velocity are shown on a plot of the 6 cm spectral luminosity at peak *vs.* the time to reach that peak for a number of RSNe. Although expected, it is noteworthy that all Type II SNe, which have relatively dense circumstellar envelopes, have the lowest expansion velocities, while the Type Ib/c SNe, with their relatively less dense CSM, have significantly higher expansion rates. Once again, SN 1998bw appears to represent a more extreme form of Type Ib/c RSNe.

8.2.4. *Radio light curves*

A final, obvious comparison of SN 1998bw with other RSNe is the evolution of its radio flux density at multiple frequencies. The radio data for the first 80 days are plotted in Kulkarni *et al.* (1998c), up to day 250 on *[http://www.narrabri.atnf.csiro.au/public/grb](http://www.narrabri.atnf.csiro.au/public/grb/grb980425/) [/grb980425/](http://www.narrabri.atnf.csiro.au/public/grb/grb980425/)*, and have been kindly supplied to us in tabular form by D. A. Frail (private communication). SN 1998bw shows an early peak at higher frequencies ($\nu \geq 2.5 \text{ GHz}$), which reaches a maximum as early as day $10 - 12$ at 8.64 GHz, drops to a minimum almost simultaneously for the higher frequencies at day $\sim 20 - 24$, and then reaches a secondary, somewhat lower peak at later times after the first dip. An interesting characteristic of this "double humped" structure is that it dies out at lower frequencies and is relatively inconspicuous in the 1.4 GHz radio measurements (see Fig. 10). Such a structure is not as prominent for other known radio supernovae on such a short time scale, although the Type Ic SN 1994I (S. D. Van Dyk, private communication) shows a dip in its 15 GHz flux density, also at an age of ~ 20 days.

Li & Chevalier (2000) propose an initially synchrotron self-absorbed (SSA), rapidly expanding shock wave in a $\rho \propto r^{-2}$ circumstellar wind model to describe the radio light curve. This is in many ways similar to the Chevalier (1998) model for Type Ib/c SNe, which also included SSA, and the structure described in §2.1, which includes only thermal

FIGURE 10. The radio light curves of SN 1998bw at 8.64 GHz (3.5 cm; cross, dash-double dot line), 4.80 GHz (6.3 cm; open triangle, dash-dot line), 2.50 GHz (12 cm; open square, dotted line) and 1.38 GHz (21.7 cm; open circle, solid line). The curves are derived from a best fit model described by the equations in §2.1 and the parameters listed in Table 3.

free-free initial absorption. However, to improve the quality of the fit, Li $\&$ Chevalier (2000) introduce the additional free parameters of a boost of shock energy by a factor of \sim 2.8 on day \sim 22 in the observer's time frame. This provides the energy necessary to produce the second peak in the radio light curves.

While is not possible to rule out such complexities, we have attempted to describe the radio light curve by a relatively straightforward, two-component model, very similar to those used successfully for previous SNe described above in §2.1. Such an approach has no requirement for shock re-acceleration. Also, although an attempt was made to include the effects of SSA at early times, the fit was not improved by such an addition. The two component model fit which we obtained using only synchrotron emission and thermal, free-free absorption is shown as the lines in Fig. 10, and its parameter values are listed in Table 3. The "double humped" structure of the radio light curves for SN 1998bw is reproduced by a single energy shock wave encountering regions of differing CSM density as it travels rapidly outward.

Since Li $\&$ Chevalier (2000) do not give a quantitative indication of the quality of their

fit, it is impossible to compare the two models directly. However, a visual comparison of Fig. 10 here with their Fig. 9 indicates that the fits are of similar quality at late times and low frequencies, where the initial absorption mechanisms have become less important. This is not surprising, since they are based on the same models from Chevalier (1982a,b). Both our model and the Li & Chevalier (2000) model have difficulty adequately describing the dip at all frequencies near day 20. However, at early times and high frequencies the free-free absorption model shown in Fig. 10 gives a clearly superior fit to the data to that of Li & Chevalier (2000).

Note that our fit requires essentially no diffuse/uniform absorption $(K_2 = 0; \text{ see Table})$ 3 and Eqs. $2.1 - 2.4$, so that all of the free-free absorption either is due to a clumpy medium or is internal to the emitting zones (which has the same mathematical form), both of which contribute to a K_3 term in Table 3 and Eqs. 2.1 – 2.4. These results, combined with the estimate of a high shock velocity, suggest that the CSM around SN 1998bw is highly clumped in numerous and dense knots with little, if any, intra-knot gas. The clump filling factor has to be high enough to intercept a considerable fraction of the shock energy and still be low enough to let radiation escape from any given knot without being appreciably absorbed by any other knot. This can be somewhat quantified by postulating that the covering factor (*i.e.,* the fraction of solid angle occupied by clumps) has to be less than ∼1/4 and, perhaps, greater than ∼1/10. In this scenario the shock front can easily move at a speed which is a significant fraction of the speed of light, because it is moving essentially in a vacuum. However, one still has strong energy dissipation and relativistic electron acceleration at the knot surfaces facing the SN explosion center. If the knots are dense and relatively opaque to radio emission, we mainly observe radiation produced at the surfaces of the knots in the CSM on the farside of the SN in which some *internal* absorption is also occurring. The radiation from near-side knots is probably absorbed internally by the knots themselves and, therefore, lost from the signal we detect.

The presence of two components, as evidenced by the presence of two peaks in the radio light curve, implies the existence of two regimes within the clumpy CSM that surrounds the SN progenitor with the transition between the two regimes occurring at about 10 to 20 light-days from the star, i.e., at about 3×10^{16} cm or \sim 3000 AU from the stellar progenitor. This distance may be somewhat speculatively interpreted as the separation of the exploding primary from a lower-mass binary companion, which is reminiscent of the binary structure inferred for SN 1979C (Weiler *et al.* 1992a, Boffi & Panagia 1996). In the case of SN 1998bw a mass at explosion of about \sim 14 M_☉ and an original progenitor mass of ∼30 – 40 M[⊙] has been proposed (Danziger *et al.*, this Conference). A binary hypothesis is also the best explanation for the large mass loss that the progenitor star must have suffered to expose the H-free layers typical of Type Ib/c supernovae before exploding. Within this framework, one may argue that the CSM within the SN progenitor Roche lobe was mostly determined by the progenitor mass-loss itself, whereas at larger distances the CSM was largely determined by the interaction of the progenitor wind with the companion wind, thus leading to a two-component CSM structure.

Clearly, there is much more complexity in the physics of the GRB phenomenon and the structure of the SN 1998bw system than can be described by simple models, and none proposed is completely satisfactory as yet. However, while the γ -ray emission itself appears to require relativistic boosting, the radio emission from the best-studied possible example, SN 1998bw, need not be interpreted as proof of relativistic beaming, highly relativistic shock waves, or other esoteric phenomena. Only mildly relativistic processes and thermal absorption by the ionized CSM appear at least satisfactory and the arguments for a SN 1998bw/GRB 980425 connection are correspondingly weakened.

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8.2.5. *Summary of SN 1998bw/GRB 980425 relations*

On balance, SN 1998bw appears to be a relatively normal, if rather over-bright example of the SN Type Ib/c phenomenon. Many observers tend to accept that it is associated with GRB 980425, and it is impossible to disprove that postulate. On the other hand, neither the optical nor radio emission are sufficiently unusual to firmly establish a connection, and the Pian *et al.* (1999) X-ray source S2 in the GRB field remains a distinct possibility for the location of GRB 980425. We can only hope that both the continued study of the GRB phenomenon and its (sometimes) associated afterglows, and the slowly increasing statistics of observations of Type Ib/c SNe, will be able to establish the true nature of both phenomena and any possible relation.

8.3. *Acknowledgments*

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REFERENCES

- Ball, L., Campbell-Wilson, D., Crawford, D. F. & Turtle, A. J. 1995, Astrophys. J. 453, 864
- Bartel, N. et al. 1985, Nature 318, 25

BOFFI, F. R. & PANAGIA, N. 1996. In Radio Emission from the Stars and the Sun (ed. A. R. Taylor & J. M. Paredes). Astr. Soc. Pacific Conf. Series, vol. 93, p. 153

- Bono, G. & Panagia, N. 2000, in preparation.
- Brocato, E. & Castellani, V. 1993, Astrophys. J. 410, 99

Chevalier, R. A. 1982a, Astrophys. J. 259, 302

- Chevalier, R. A. 1982b, Astrophys. J. Lett. 259, L85
- Chevalier, R. A. 1998, Astrophys. J. 499, 810
- Chevalier, R. A. & Fransson, C. 1994, Astrophys. J. 420, 268
- Chu, Y.-H., Caulet, A., Montes, M. J., Panagia, N., Van Dyk, S. D., & Weiler, K. W. 1999, Astrophys. J. Lett. **512**, L51.

Filippenko, A. 1998, IAUC 6969

- FILIPPENKO, A., MATHESON, T., & BARTH, A. 1994, Astron. J. 108, 222
- Frail, D. A. & Kulkarni, S. R. 1997, IAUC 6662
- FRANSSON, C. & BJÖRGSSON, C.-I. 1998, Astrophys. J. 509, 861
- FRUCHTER, A. & BERGERON, L. 1997, IAUC 6674
- Gaensler, B. M., Manchester, R. N., Staveley-Smith, L., Tzioumis, A. K., Reynolds, J. E., & KESTEVEN, M. J. 1997, Astrophys. J. 479, 845
- Galama, T. J. et al. 1998, IAUC 6895
- Garnavich, P., Kirshner, R., & Challis, P. 1997, IAUC 6710
- Green, D. W. E. 1994, IAUC 5953
- Groot, P. J. et al. 1997, IAUC 6584
- Halpern, J. et al. 1997, IAUC 6788
- HASINGER, G., ASCHENBACH, B., & TRUEMPER, J. 1996, Astron. Astrophys. 312, 9
- Heise, J. et al. 1997, IAUC 6787
- HOEFLICH, P., WHEELER, J. C., HINES, D. C., & TRAMAELL, S. R. 1996, Astrophys. J. 459, 307
- Hamuy, M. et al. 1992, IAUC 5574
- Iwamoto, K. et al. 1998, Nature 395, 672
- Kay, L. E., Halpern, J. P., & Leighly, K. M. 1998, IAUC 6969
- KELLERMANN, K. I. & PAULINY-TOTH, I. I. K. 1969, Astrophys. J. Lett. 155, L71
- Kulkarni, S. et al. 1998a, Nature 393, 35
- Kulkarni, S. R., Bloom, J. S., Frail, D. A., Ekers, R., Wieringa, M., Wark, R., & Higdon, J. L. 1998b, IAUC 6903
- Kulkarni, S. R., Frail, D. A., Wieringa, M. H., Ekers, R. D., Sadler, E. M., Wark, R. M., Higdon, J. L., Phinney, E. S., & Bloom, J. S. 1998c, Nature 395, 663
- Lacey, C. K., Weiler, K. W., Sramek, R. A., Panagia, N., & Van Dyk, S. D. 2000, in preparation
- Lang, K.R. 1986. In Astrophysical Formulae, 47. Springer-Verlag
- LANGER, N. & MAEDER, A. 1995, Astron. Astrophys. 295, 685
- Li, Z.-Y. & Chevalier, R. A. 2000, in press (also [astro-ph/9903483\)](http://arxiv.org/abs/astro-ph/9903483)
- LIDMAN, C. et al. 1998, IAUC 6895
- Marcaide, J. M. et al. 1997, Astrophys. J. Lett. 486, L31
- Miller, D. L. & Branch, D. 1990, Astron. J. 100, 530
- Montes, M. J., Weiler, K. W., & Panagia, N. 1997, Astrophys. J. 488, 792
- Montes, M. J., Van Dyk, S. D., Weiler, K. W., Sramek, R. A., & Panagia, N. 1998, Astrophys. J. 506, 874
- Montes, M. J., Weiler, K. W., Van Dyk, S. D., Sramek, R. A., Panagia, N., & Park, R. 2000, Astrophys. J., in press (also [astro-ph/9911399](http://arxiv.org/abs/astro-ph/9911399))
- Nomoto, K., Yamaoka, H., Pols, O. R., van den Heuvel, E., Iwamoto, K., Kumagai, S., & Shigeyama, T. 1994, Nature 371, 227
- Odewahn, S. C. et al. 1998, Astrophys. J. 509, 5
- PACZYNSKI, B. 1998, Astrophys. J. Lett. 494, L45
- PANAGIA, N. & MACCHETTO, F. 1982, Astron. Astrophys. 106, 266
- PATAT, F., CAPPELLARO, E., RIZZI, L., TURATTO, M., & BENETTI, S. 1999, IAUC 7215
- PATAT, F. & PIEMONTE, A. 1998, IAUC 6918
- PIAN, E. et al. 1998, Astrophys. J. Lett. 492, L103
- PIAN, E. et al. 1999, Astron. Astrophys. Suppl. Ser. 138, 463
- PODSIADLOWSKI, P., HSU, J., JOSS, P., & ROSS, R. 1993, Nature 364, 509
- READHEAD, A. C. S. 1994, Astrophys. J. 426, 51
- Ryder, S., Staveley-Smith, L., Dopita, M., Petre, R., Colbert, E., Malin, D., & Schlegel, E. 1993, Astrophys. J. 417, 167
- Sadler, E. M., Stathakis, R. A., Boyle, B. J., & Ekers, R. D. 1998, IAUC 6901
- SAHU, K. C. et al. 1997, Astrophys. J. Lett. 489, L127
- SCHWARZ, D. H. & PRINGLE, J. E. 1996, Mon. Not. R. Astr. Soc. 282, 1018
- SOFFITTA, P. et al. 1998, IAUC 6884
- SPYROMILIO, J. 1994, Mon. Not. R. Astr. Soc. 266, 61
- Tinney, C., Stathakis, R., Cannon, R., & Galama, T. 1998, IAUC 6896
- TULLY, R. B. 1988. In Nearby Galaxies Catalogue. Cambridge Univ. Press.
- Turtle, A. J., Campbell-Wilson, D., Bunton, J. D., Jauncey, D. L., Kesteven, M. J., MANCHESTER, R. N., NORRIS, R. P., STOREY, M. C., & REYNOLDS, J. E. 1987, Nature 327, 38
- Van Dyk, S. D., Sramek, R. A., Weiler, K. W., & Panagia, N. 1993, Astrophys. J. Lett. 419, L69
- Van Dyk, S. D., Weiler, K. W., Sramek, R. A., Rupen, M., & Panagia, N. 1994, Astrophys. J. Lett. 432, L115
- Van Dyk, S. D., Hamuy, M., & Filippenko, A. V. 1996, Astron. J. 111, 2017
- Waxman, E. & Loeb, A. 1999, Astrophys. J. 515, 721
- Weiler, K. W., Sramek, R. A., Panagia, N., van der Hulst, J. M., & Salvati, M. 1986, Astrophys. J. 301, 790
- Weiler, K. W., Panagia, N., & Sramek, R. A. 1990, Astrophys. J. 364, 611
- Weiler, K. W., Van Dyk, S. D., Panagia, N., Sramek, R. A., & Discenna, J. 1991, Astrophys. J. 380, 161
- Weiler, K. W., Van Dyk, S. D., Pringle, J., & Panagia, N. 1992a, Astrophys. J. 399, 672
- Weiler, K. W., Van Dyk, S. D., Panagia, N., & Sramek, R. A. 1992b, Astrophys. J. 398, 248
- Weiler, K. W., Van Dyk, S. D., Montes, M. J., Panagia, N., & Sramek, R. A. 1998, Astrophys. J. 500, 51
- Yin, Q. F. 1994, Astrophys. J. 420, 152

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