

# GI2T/REGAIN spectro-interferometry with a new infrared beam combiner

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## ABSTRACT

We have built an infrared beam combiner for the GI2T/REGAIN interferometer of the Observatoire de la Cote d'Azur. The beam combiner allows us to record spectrally dispersed Michelson interference fringes in the near-infrared J-, H- or K-bands. The beam combiner has the advantage that Michelson interferograms can simultaneously be recorded in about 128 different spectral channels. The tilt of the spectrally dispersed fringes is a measure of the instantaneous optical path difference. We present the optical design of the beam combiner and GI2T/REGAIN observations of the Mira star R Cas with this beam combiner in the spectral range of  $2.00\ \mu\text{m} - 2.18\ \mu\text{m}$  (observations on 22 and 25 August 1999; variability phase 0.08; V-magnitude approximately 6; seven baselines between 12 m and 24 m; reference stars Vega and  $\beta$  Peg). The spectrograph of the beam combiner consists of an anamorphic cylindrical lens system, an image plane slit, and a grism. The detector is a 256x256 pixel Rockwell PICNIC array camera. The shortest possible exposure time is 10 ms. A system of digital signal processors calculates the ensemble average power spectrum of the spectrally dispersed Michelson interferograms, the instantaneous optical path difference error, and several other useful parameters in real time. From the observed R Cas visibilities at baselines 12.0 m, 13.8 m and 13.9 m, a  $2.1\ \mu\text{m}$  uniform-disk diameter of  $25.3\ \text{mas} \pm 3.3\ \text{mas}$  was derived. The unusually high visibility values at baselines  $\geq 16$  m show that the stellar surface of R Cas is more complex than previously assumed. The visibility values at baselines  $\geq 16$  m can be explained by high-contrast surface structure on the stellar surface of R Cas or other types of unexpected center-to-limb variations. The R Cas observations were compared with theoretical Mira star models<sup>1,2</sup>. We obtained the following results for R Cas at variability phase 0.08:

Angular Rosseland radius  $R^a$ :  $12.1\ \text{mas} \pm 1.7\ \text{mas}$

Linear Rosseland radius  $R$ :  $276\ R_{\odot} \pm 66\ R_{\odot}$  (using the HIPPARCOS parallax of  $9.36\ \text{mas} \pm 1.10\ \text{mas}$ )

Effective temperature:  $2685\ \text{K} \pm 238\ \text{K}$  (derived from the angular Rosseland radius and the JHKLM-photometry).

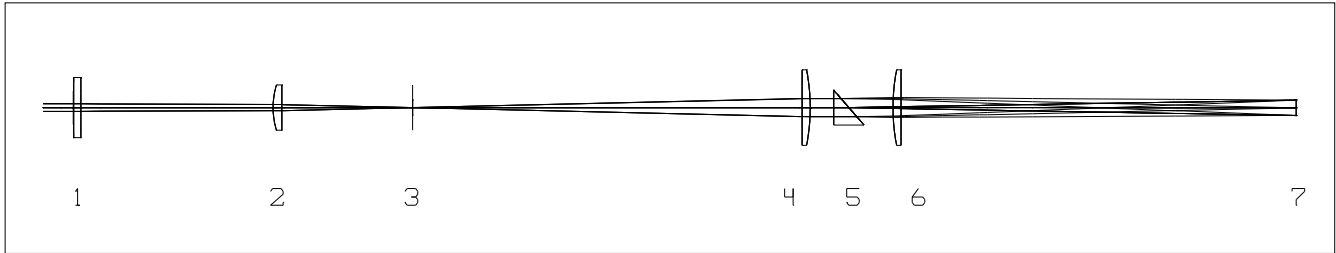
**Keywords:** interferometry - infrared - spectroscopy - evolved stars - Mira stars

## 1. INTRODUCTION

The GI2T/REGAIN interferometer<sup>3,4</sup> is an optical interferometer of two 1.5 m telescopes. For this interferometer we have built an infrared beam combiner and used it to record spectrally dispersed infrared Michelson interferograms of the Mira star R Cas. In this paper we present the design of our new infrared beam combiner and R Cas observations obtained in August 1999. This beam combiner allows us to simultaneously record Michelson fringes in about 128 different spectral channels from 2.00 to 2.18  $\mu\text{m}$ . The tilt of the spectrally dispersed fringes is a measure of the instantaneous optical path difference. The R Cas observations reported in this paper are the first NIR interferometry observations with large 1.5 m telescopes. The aim of our Mira star project is to resolve the stellar disk of Mira stars, to reveal photospheric asymmetries and surface structures, and to study the wavelength and phase dependence of the diameter. Previous speckle or long-baseline interferometry observations of Mira stars were, for example, reported in Refs. 5-16. Theoretical studies<sup>1,2,17-19</sup> show that interferometric diameter measurements can considerably improve our understanding of cool stellar atmospheres.

## 2. INSTRUMENT

Figure 1 shows the optical layout of our new NIR beam combiner built at the MPI for Radioastronomy. It consists of an anamorphic lens system, an image plane slit, a grism, a shutter, a PICNIC detector, a data storage computer, and an array of digital signal processors for data processing. The DSPs can calculate the power spectrum and the instantaneous optical path difference in real-time. The typical frame rate is 3 frames per second ( $256 \times 256$  pixels per frame).



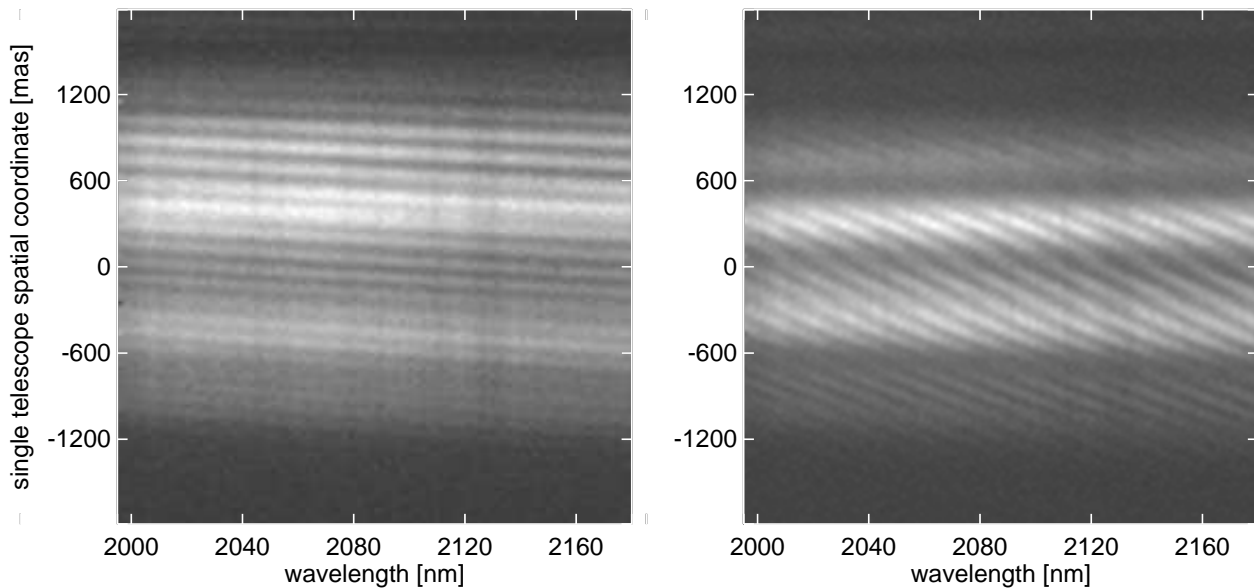
**Figure 1.** Optical layout of the new NIR beam combiner (1 beam combiner lens with 750 mm focal length; 2, 4 and 6 cylindrical lenses; 3 image plane slit and slit viewer camera; 5 grism; 7 PICNIC detector; anamorphic compression factor 9).

## 3. R CAS OBSERVATIONS AND DATA PROCESSING

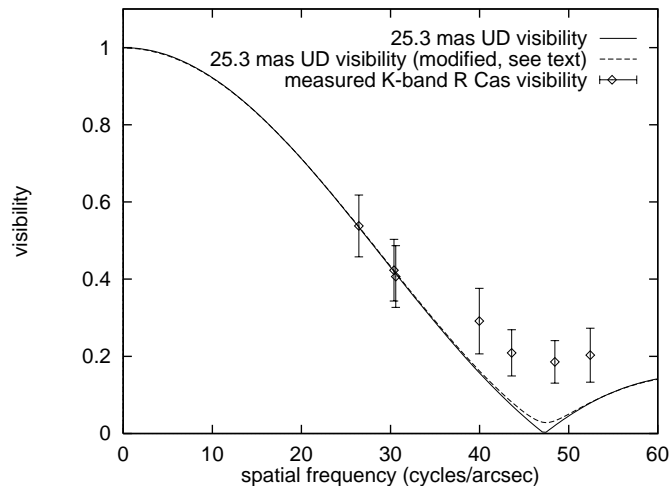
The first infrared observations with our new beam combiner mounted to the GI2T/REGAIN interferometer were carried out on August 22 and 25, 1999. The observational parameters of the R Cas and reference star observations are as follows:

|                                   |  |
|-----------------------------------|--|
| Projected R Cas baselines:        | 12.01 m, 13.80 m, 13.88 m, 18.14 m, 19.79 m, 21.99 m, 23.79 m  |
| Date of R Cas observations:       | 22 Aug. 1999 (baselines 12.01 m, 13.80 m),<br>25 Aug. 1999 (baselines 13.88 m, 18.14 m, 19.79 m, 21.99 m, 23.79 m) |
| Reference stars:                  | Vega, $\beta$ Peg  |
| Number of frames per baseline:    | 500  |
| Frame rate:                       | 3 frames/s   |
| Filter:                           | center wavelength $2.1 \mu\text{m}$ , FWHM bandwidth $0.3 \mu\text{m}$   |
| Recorded wavelength band:         | $2.00 \mu\text{m} - 2.18 \mu\text{m}$  |
| Number of spectroscopic channels: | 128  |
| Anamorphic projection factor:     | 9  |
| Exposure time per frame:          | 100 ms   |
| K-band seeing:                    | 2 arcsec   |

Figure 2 shows two of several thousand recorded interferograms of R Cas. The interferograms of R Cas and the reference stars were flatfielded and sky-subtracted, and the visibilities of each spectral channel and baseline were derived by calculating the ensemble average power spectra. The method described by Mourard et al.<sup>20</sup> was applied to derive visibility ratios of the object and reference star observations and to obtain calibrated R Cas visibilities. Figure 3 shows the derived R Cas visibilities. The solid line is the visibility function of a uniform-disk of a star with 25.3 mas diameter. The dashed curve is the uniform-disk visibility fit curve which is required for our observations with large 1.5 m telescopes. This dashed visibility fit function has no zeros since an average of many baselines is measured rather than only one single baseline if the telescope pupils are large. If the projected baseline from mirror center to mirror center is for example 10 m, all baselines between 8.5 m and 11.5 m are simultaneously measured. The



**Figure 2.** Two of several thousand recorded interferograms of the Mira star R Cas (spectral range 2.00 to 2.18  $\mu\text{m}$ ; baseline 13.80 m). In the left interferogram the fringes are nearly parallel to the dispersion direction since the optical path difference error is almost zero. In the right interferogram the fringes are tilted due to a small optical path difference error.



**Figure 3.** GI2T/REGAIN visibility measurements of R Cas with our new NIR beam combiner (baselines 12.01 m, 13.80 m, 13.88 m, 18.14 m, 19.79 m, 21.99 m, 23.79 m).

R Cas visibilities in Fig. 3 show that the center-to-limb variation of R Cas is not a uniform-disk function. The large visibility values at spatial frequencies larger than  $\sim 40$  cycles per arcsec can be explained by high-contrast surface structure on the stellar surface of R Cas or by other types of unexpected center-to-limb variations. A uniform-disk fit diameter of 25.3 mas  $\pm$  3.3 mas is obtained if only the first three low-frequency visibility points (projected baselines 12.01 m, 13.80 m, and 13.88 m) are used for the uniform-disk fit. The error bars of our first IR observations

are relatively large because the weather situation was not favorable and the control system (Mourard et al., this proceedings<sup>21</sup>) of the GI2T/REGAIN (Mourard et al., this proceedings<sup>22</sup>) was not fully operational. Under normal observing conditions the error bars will be much smaller.

## 4. COMPARISON OF THE OBSERVATIONS WITH MIRA STAR MODELS

### 4.1. The stellar filter radius and Rosseland radius of R Cas

In this section we derive various types of angular diameters from the measured visibilities of R Cas by applying the different theoretical center-to-limb intensity variations (hereafter CLV) of different Mira star models (Bessel, Scholz, and Wood 1996 = BSW96<sup>1</sup>, Hofmann, Scholz and Wood 1998 = HSW98<sup>2</sup>). From these angular diameters (Fig. 4) and the bolometric flux, we derive effective temperatures (Fig. 6). All Mira star models used in this paper are from BSW96 (D and E series) and from HSW98 (P, M and O series). They were developed as possible representations of the prototype Mira variable o Ceti, and hence have periods  $P$  very close to the 332 day period of this star. They differ in pulsation mode, assumed mass  $M$  and assumed luminosity  $L$ . The BSW96 models differ from the more advanced HSW98 models with respect to the pulsation modelling technique. The five models represent stars pulsating in the fundamental mode ( $f$ ; D, P and M models) or in the first-overtone mode ( $o$ ; E and O models). Table 1 lists the properties of these Mira model series. Table 2 provides the link between the 22 abscissa values (model-phase combinations  $m$ ) in Figs. 4 - 6, and the models.  $R_p$  denotes the Rosseland radius (below) of the non-pulsating parent star of the Mira variable (BSW96, HSW98). Table 2 additionally lists the variability phase, the relative Rosseland and stellar K-band radius, and the effective temperature. We compare predictions of these models for different phases and cycles with our observations.

*Monochromatic radius  $R_\lambda$  and Rosseland radius  $R$ .* We use the conventional stellar radius definition where the monochromatic radius  $R_\lambda$  of a star at wavelength  $\lambda$  is given by the distance from the star's center at which the optical depth equals unity ( $\tau_\lambda = 1$ ). In analogy, the photospheric stellar radius  $R$  (Rosseland radius) is given by the distance from the star's center at which the Rosseland optical depth equals unity ( $\tau_{\text{Ross}} = 1$ ). This radius has the advantage of agreeing well (see Table 6 in HSW98 for deviations sometimes occurring in very cool stars) with measurable near-infrared continuum radii and with the standard boundary radius of pulsation models with  $T_{\text{eff}} \propto (L/R^2)^{1/4}$ .

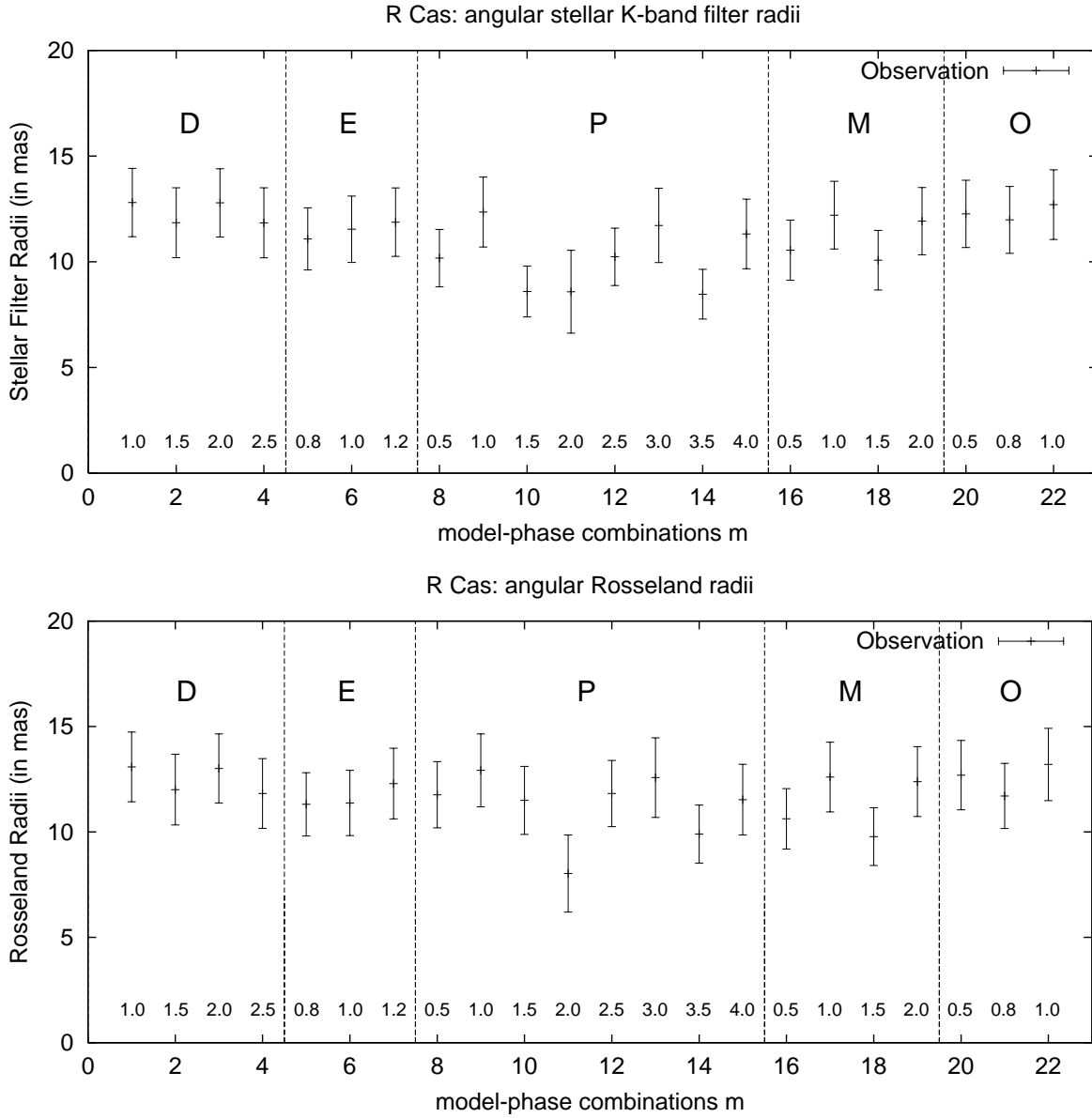
*Stellar filter radius  $R_f$ .* For the K-band filter used for the observations, we have calculated the theoretical CLVs of the above mentioned five Mira star models at different phases and cycles. The stellar radius for filter transmission  $f_\lambda$  is the intensity- and filter-weighted radius  $R_f = \int R_\lambda I_\lambda f_\lambda d\lambda / \int I_\lambda f_\lambda d\lambda$ , which we call *stellar filter radius  $R_f$*  after Scholz & Takeda's definition<sup>23</sup>. In this equation  $R_\lambda$  denotes the above monochromatic  $\tau_\lambda = 1$  radius,  $I_\lambda$  the central intensity spectrum and  $f_\lambda$  the transmission of the filter.

### 4.2. Angular R Cas radii

The observed angular stellar K-band radii  $R_{K,m}^a$  of R Cas corresponding to the various model-phase combinations  $m$ , were derived by least-squares fits between the first three visibility values (baselines 12.01 m, 13.80 m and 13.88 m) shown in Fig. 3 and the visibilities of the different theoretical K-band CLVs of different model-phase combinations  $m$ . Additionally, the observed angular Rosseland radii  $R_m^a$  of R Cas corresponding to the model-phase combination  $m$  were derived from the observed angular stellar K-band radii  $R_{K,m}^a$  and the theoretical radius ratios  $R_m/R_{K,m}$  from Table 2 (Table 2 provides theoretical  $R$  and  $R_K$  values for each model-phase combination  $m$ ). The derived angular stellar filter radii  $R_{K,m}$  and angular Rosseland radii  $R_m$  are shown in Fig. 4.

**Table 1.** Properties of Mira model series<sup>1,2</sup> (see text)

| Series | Mode | $P$ (days) | $M/M_\odot$ | $L/L_\odot$ | $R_p/R_\odot$ | $T_{\text{eff}}/\text{K}$ |
|--------|------|------------|-------------|-------------|---------------|---------------------------|
| D      | f    | 330        | 1.0         | 3470        | 236           | 2900                      |
| E      | o    | 328        | 1.0         | 6310        | 366           | 2700                      |
| P      | f    | 332        | 1.0         | 3470        | 241           | 2860                      |
| M      | f    | 332        | 1.2         | 3470        | 260           | 2750                      |
| O      | o    | 320        | 2.0         | 5830        | 503           | 2250                      |



**Figure 4.** Observed angular stellar K-band radii  $R_{K,m}^a$  (top) and Rosseland radii  $R_m^a$  (bottom) of R Cas derived from the measured R Cas visibilities by fitting the theoretical CLVs of the 22 model-phase combinations  $m$ . Table 2 shows the link between the abscissa values and the models and the variability phases.

**Table 2.** Link between the 22 model-phase combinations  $m$  in Figs. 4 - 6, and the models. The variability phase  $\Phi_{\text{vis}}$ , the Rosseland radius  $R$  and the K-band radius  $R_{\text{K}}$  in units of the non-pulsating parent star radius  $R_p$  (see BSW96), and the effective temperature  $T_{\text{eff}}(R)$  associated to the Rosseland radius are additionally given.

| Model  | $\Phi_{\text{vis}}$ | $R/R_p$ | $R_{\text{K}}/R_p$ | $T_{\text{eff}}(R)$ | $m$ |
|--------|---------------------|---------|--------------------|---------------------|-----|
| D27520 | 1+0.0               | 1.04    | 1.02               | 3020                | 1   |
| D27760 | 1+0.5               | 0.91    | 0.90               | 2710                | 2   |
| D28760 | 2+0.0               | 1.04    | 1.02               | 3030                | 3   |
| D28960 | 2+0.5               | 0.91    | 0.91               | 2690                | 4   |
| E8300  | 0+0.83              | 1.16    | 1.14               | 2330                | 5   |
| E8380  | 1+0.0               | 1.09    | 1.10               | 2620                | 6   |
| E8560  | 1+0.21              | 1.17    | 1.14               | 2610                | 7   |
| P71800 | 0+0.5               | 1.20    | 1.04               | 2160                | 8   |
| P73200 | 1+0.0               | 1.03    | 0.99               | 3130                | 9   |
| P73600 | 1+0.5               | 1.49    | 1.12               | 1930                | 10  |
| P74200 | 2+0.0               | 1.04    | 1.11               | 3060                | 11  |
| P74600 | 2+0.5               | 1.17    | 1.02               | 2200                | 12  |
| P75800 | 3+0.0               | 1.13    | 1.06               | 3060                | 13  |
| P76200 | 3+0.5               | 1.13    | 0.96               | 2270                | 14  |
| P77000 | 4+0.0               | 1.17    | 1.14               | 2870                | 15  |
| M96400 | 0+0.5               | 0.93    | 0.92               | 2310                | 16  |
| M97600 | 1+0.0               | 1.19    | 1.15               | 2750                | 17  |
| M97800 | 1+0.5               | 0.88    | 0.90               | 2460                | 18  |
| M98800 | 2+0.0               | 1.23    | 1.19               | 2650                | 19  |
| O64210 | 0+0.5               | 1.12    | 1.09               | 2050                | 20  |
| O64530 | 0+0.8               | 0.93    | 0.95               | 2150                | 21  |
| O64700 | 1+0.0               | 1.05    | 1.01               | 2310                | 22  |

### 4.3. Linear R Cas radii

We have derived linear stellar radii of R Cas (in units of solar radii) from the measured angular stellar K-band radii  $R_{\text{K},m}^a$  and Rosseland radii  $R_m^a$  (Fig. 4) by using the R Cas HIPPARCOS parallax of  $9.36 \text{ mas} \pm 1.10 \text{ mas}^{24}$ . Fig. 5 shows the obtained R Cas radii for all model-phase combinations  $m$ . The theoretical Rosseland radii of the M and of the P model series at nearly all available near-maximum phases (1.0, 3.0, 4.0) are close (within the error bars) to the measured Rosseland radii. The theoretical Rosseland radii of the first-overtone models E and O are clearly too large compared with measured Rosseland radii. The theoretical radii of the D model series are slightly too small compared with the measured Rosseland radii. The same conclusions are also valid for the linear stellar filter radii  $R_{\text{K}}$  (Fig. 5).

If we calculate average linear radii by averaging the radii obtained with all available *near-maximum* M models (i.e.,  $m = 17, 19$ ) and/or *near-maximum* P models (i.e.,  $m = 9, 11, 13, 15$ ) we obtain:

Average theoretical M model Rosseland radius:  $315 R_{\odot}$

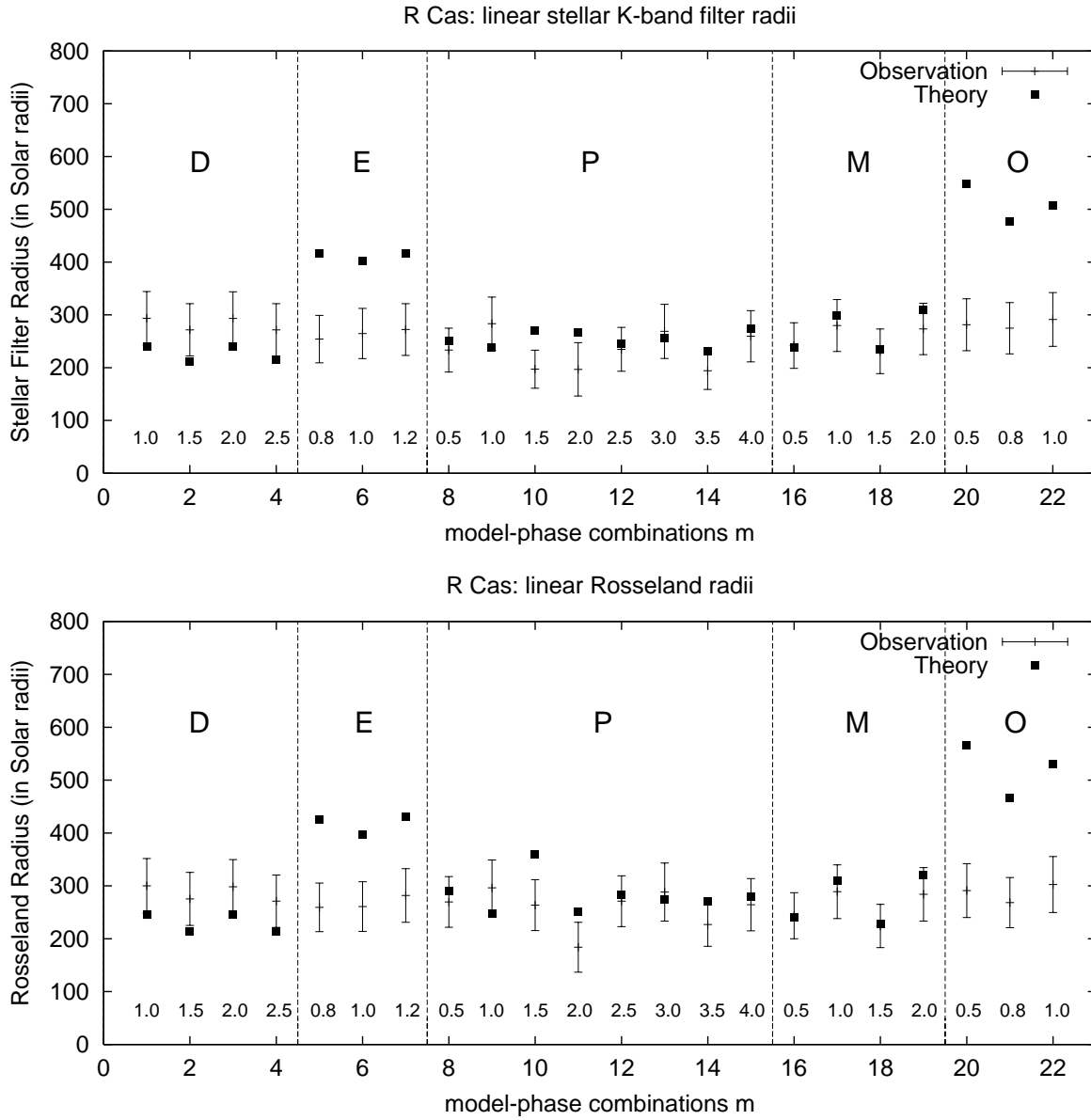
Average measured M model Rosseland radius:  $287 R_{\odot} \pm 51 R_{\odot}$  (obtained with  $m = 17$  and 19)

Average theoretical P model Rosseland radius:  $263 R_{\odot}$

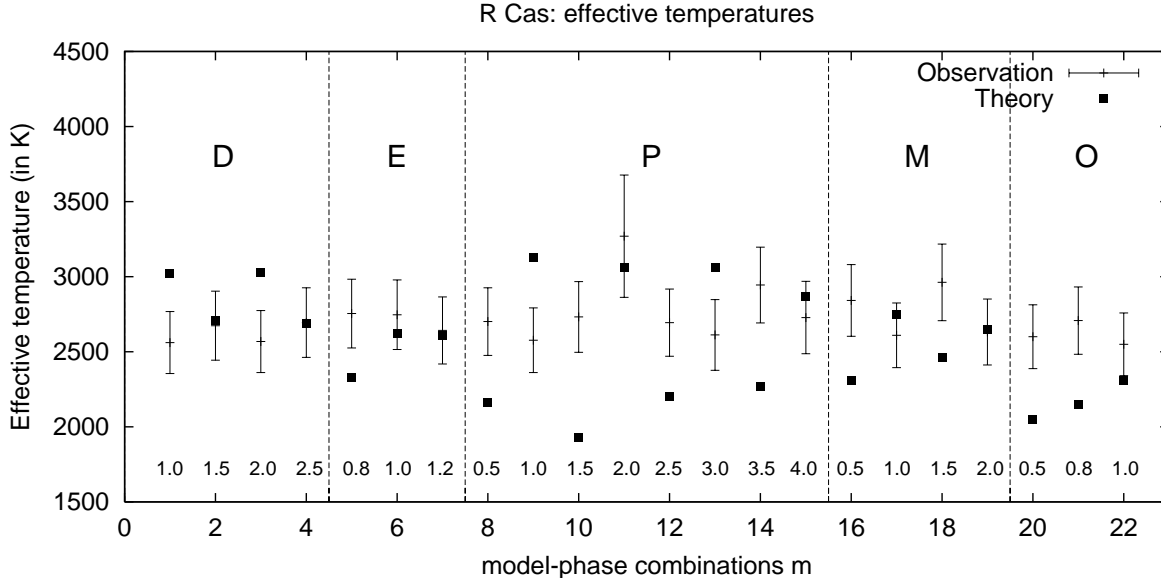
Average measured P model Rosseland radius:  $264 R_{\odot} \pm 82 R_{\odot}$  (obtained with  $m = 9, 11, 13$  and 15)

Average theoretical model Rosseland radius:  $289 R_{\odot}$

Average measured model Rosseland radius:  $276 R_{\odot} \pm 66 R_{\odot}$  ( $m = 9, 11, 13, 15, 17, 19$ ; M and P models)



**Figure 5.** Comparison of observed R Cas radii (crosses; see Sect. 4.3) and theoretical model radii (filled squares; D, E, P, M and O model for different phases; see Table 2) plotted versus all 22 model-phase combinations  $m$  (top: stellar K-band radii  $R_{K,m}$ ; bottom: Rosseland radii  $R_m$ ).



**Figure 6.** Comparison of model effective temperatures  $T_{\text{eff},m}$  (plotted versus the 22 model-phase combinations  $m$ ; see Sect. 4.1) and the measured R Cas effective temperatures derived from measured angular Rosseland radii  $R_m^a$  (see Sect. 4.2) and JHKLM-photometry. Table 2 shows the link between the abscissa values  $m$  and the models and phases.

#### 4.4. Effective temperatures of R Cas

Effective temperatures of R Cas were derived from its angular Rosseland radii  $R_m^a$  (Sect. 4.2) and its bolometric flux using the relation

$$T_{\text{eff}} = 2341 \text{ K} \times (F_{\text{bol}}/\phi^2)^{1/4}, \quad (1)$$

where  $F_{\text{bol}}$  is the apparent bolometric flux in units of  $10^{-8} \text{ erg cm}^{-2} \text{ s}^{-1}$  and  $\phi = 2R_m^a$  is the angular Rosseland diameter in mas. The bolometric flux was derived from JHKLM-band observations carried out 7 days after the visibility observations. For cool stars such as LPVs, where most of the luminosity is emitted at near-infrared wavelengths, a convenient approximation for calculating bolometric magnitudes is to use a blackbody function to interpolate between photometric observations in the J, H, K, L and M bands. For estimating the bolometric flux we used the photometric JHKLM measurements of B. Yudin which were carried out with the 1.25 m telescope at the Crimean station of the Sternberg Astronomical Institute in Moscow seven days after our visibility observations. The derived bolometric flux of R Cas on 29 August 1999 was  $980.6 \pm 180 \times 10^{-8} \text{ erg cm}^{-2} \text{ s}^{-1}$ .

**Table 3.** Observational R Cas data and measured effective temperature.

| Star  | Date         | $\Phi_{\text{vis}}$ | $K$<br>[mag] | $F_{\text{bol}}$<br>[ $10^{-8} \text{ erg/cm}^2 \text{ s}$ ] | $R^a$<br>[mas] | $T_{\text{eff}}$<br>[K] |
|-------|--------------|---------------------|--------------|--|----------------|-------------------------|
| R Cas | 99 August 29 | 0.08                | -2.04        | $980.6 \pm 180$  | $12.1 \pm 1.7$ | $2685 \pm 238$          |

Fig. 6 shows a comparison of measured and theoretical  $T_{\text{eff},m}$ -values. The theoretical and measured (phase 0.08)  $T_{\text{eff}}$ -values are in agreement, within the  $1\sigma$  error bar, with the E models at near-maximum phases 1.0 and 1.21, with the P models at phases 2.0 and 4.0, and with the M models at phases 1.0 and 2.0. Table 3 lists the measured bolometric flux, the average measured angular Rosseland radius  $R^a$  (see Sect. 4.2) and the average measured effective



temperature of R Cas. The average measured effective temperature and angular Rosseland radius is the average over all  $T_{\text{eff},m}$ - and  $R_m^a$ -values corresponding to  $m$ -values with phases close to the phase of our observations (i.e.,  $m = 1, 3, 6, 9, 11, 13, 15, 17, 19, 22$  were used for averaging).

#### 4.5. Pulsation mode

Adopting the above (Sect. 4.3) phase-averaged (over models M and P at near-maximum phases) linear Rosseland radius of the non-pulsating parent star,  $R_p$ , of  $240 R_\odot \pm 59 R_\odot$  for R Cas (derived from the measured  $R$  and the theoretical ratios given in Table 2), we find for the pulsation constant  $Q = P(M/M_\odot)^{1/2}(R/R_\odot)^{-3/2}$  a value of  $Q=0.116 \pm 0.042$  for a  $1 M_\odot$  Mira with period  $P=430$  days. This  $Q$  value agrees within the  $1\sigma$  error with the theoretical value ( $Q=0.097$ ) for fundamental pulsation mode for  $1 M_\odot$  AGB stars with a period of  $\sim 430$  days (Fox & Wood<sup>25</sup>). The corresponding  $Q$  value of first overtone pulsation mode is  $Q=0.056$ . Note, however, that no direct measurement of a Mira mass exists and that a 20% uncertainty of  $M$  would for example result in a 10% uncertainty of  $Q$ .

### 5. CONCLUSION

We have observed the Mira star R Cas with the GI2T/REGAIN interferometer and our new infrared beam combiner. A uniform-disk (UD) K-band ( $2.1 \mu\text{m}$ ) diameter of  $25.3 \text{ mas} \pm 3.3 \text{ mas}$  was derived from the interferograms obtained with baselines between 12.0 m and 13.9 m at near-maximum variability phase 0.08. The unusually high visibility values at baselines 18.1 m, 19.8 m, 22.0 m, and 23.8 m show that the stellar surface of R Cas is more complex than previously assumed. Some of the theoretical models discussed above have an unusual wing-like visibility shape (e.g., P76200 in HSW98). Huge convection cells (predicted by Schwarzschild<sup>26</sup>) could also explain the observed visibility function. The visibility function of R Leo observed by Perrin et al.<sup>15</sup> with the IOTA interferometer has a similar wing-like shape as the R Cas visibility. Perrin et al. discuss several physical phenomena which may explain the excess of visibility at high frequencies.

The R Cas UD diameter measured at wavelength  $1.04 \mu\text{m}$  at near-minimum phase 0.63 is  $29.9 \text{ mas} \pm 3.0 \text{ mas}$  (HBSW2000<sup>16</sup>), i.e., considerably larger than the above  $25.3 \text{ mas} \pm 3.3 \text{ mas}$  UD diameter measured at  $2.1 \mu\text{m}$  at near-maximum phase 0.08. The reason for this difference is not known and unexpected from the theoretical models discussed in the previous sections. The different variability phase of the two observations and/or other unknown effects, for example time-variable surface structure (e.g., supergranulation<sup>26</sup>), are possibly the cause of the diameter difference.

An angular R Cas Rosseland radius  $R^a$  of  $12.1 \text{ mas} \pm 1.7 \text{ mas}$  at phase 0.08 was derived from the  $2.1 \mu\text{m}$  visibilities measured with projected baselines between 12.0 m and 13.9 m by fitting theoretical center-to-limb variation profiles of five recent Mira star models (BSW96, HSW98). From the above mentioned  $1.04 \mu\text{m}$  observation an angular Rosseland radius  $R^a$  of  $16.5 \text{ mas} \pm 1.7 \text{ mas}$  at phase 0.63 (HBSW2000), which is larger than the the near-maximum Rosseland radius reported in this paper, was obtained (HBSW2000; see above discussion).

The effective temperature of  $2685 \text{ K} \pm 238 \text{ K}$  at near-maximum phase 0.08 was derived from the measured angular Rosseland radius and JHKLM-photometry carried out only seven days after the visibility observations.

For R Cas a good HIPPARCOS parallax ( $9.36 \text{ mas} \pm 1.10 \text{ mas}$ ) is available and it is therefore possible to compare measured linear Rosseland and stellar filter radii with the theoretical radii of the BSW96 and HSW98 models. The measured radii were derived by fitting theoretical (BSW96, HSW98) center-to-limb intensity variations to the low-frequency visibility data. In the following table we compare measured and theoretical values:

|  |                          |             |                          |             |
|--|--------------------------|-------------|--------------------------|-------------|
| Measured linear Rosseland R Cas radii $R$ :        | $286 \pm 51 R_\odot$     | (M model*); | $264 \pm 82 R_\odot$     | (P model**) |
| Theoretical linear Rosseland radii $R$ :           | $315 R_\odot$            | (M model*); | $263 R_\odot$            | (P model**) |
| Measured linear stellar K-band R Cas radii $R_K$ : | $277 \pm 50 R_\odot$     | (M model*); | $252 \pm 68 R_\odot$     | (P model**) |
| Theoretical linear stellar K-band radii $R_K$ :    | $304 R_\odot$            | (M model*); | $259 R_\odot$            | (P model**) |
| Measured effective R Cas temperature:              | $2621 \pm 217 \text{ K}$ | (M model*); | $2797 \pm 275 \text{ K}$ | (P model**) |
| Theoretical effective temperature:                 | $2700 \text{ K}$         | (M model*); | $3030 \text{ K}$         | (P model**) |

(\* average over phases 1.0, 2.0; \*\* average over phases 1.0, 2.0, 3.0, 4.0; derived from visibilities measured at baselines between 12.0 m and 13.9 m)

The comparison of these K-band ( $2.1 \mu\text{m}$ ) observations with theoretical models suggests that R Cas is well represented by the fundamental mode M and P model (BSW96, HSW98), whereas the above mentioned  $1.04 \mu\text{m}$  observations

suggested first-overtone pulsation. However, observations in more filters than just one continuum filter may be necessary for safely distinguishing a well-fitting model from an accidental match (cf. Ref. 16).

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