

Derivation of the Galactic rotation curve using space velocities

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Abstract. We present rotation curves of the Galaxy based on the space-velocities of 197 OB stars and 144 classical cepheids, respectively, which range over a galactocentric distance interval of about 6 to 12 kpc. No significant differences between these rotation curves and rotation curves based solely on radial velocities assuming circular rotation are found. We derive an angular velocity of the LSR of $\Omega_0 = 5.5 \pm 0.4$ mas/a (OB stars) and $\Omega_0 = 5.4 \pm 0.5$ mas/a (cepheids), which is in agreement with the IAU 1985 value of $\Omega_0 = 5.5$ mas/a. If we correct for probable rotations of the FK5 system, the corresponding angular velocities are $\Omega_0 = 6.0$ mas/a (OB stars) and $\Omega_0 = 6.2$ mas/a (cepheids). These values agree better with the value of $\Omega_0 = 6.4$ mas/a derived from the VLA measurement of the proper motion of Sgr A*.

Key words: Galaxy: kinematics and dynamics – Stars: kinematics – Reference systems

1. Introduction

The galactic rotation curve has been determined for the inner parts of the galactic disk, interior to the solar annulus, from H I-measurements using the tangential point method (Burton & Gordon 1978), whereas the outer rotation curve has been determined using radial velocities of objects with individually known distances, e. g. OB stars (Fich et al. 1989), planetary nebulae (Schneider & Terzian 1983), young open clusters (Hron 1987) and carbon stars (Metzger & Schechter 1994). An alternative method is based on the vertical thickness of the galactic H I-layer (Merrifield 1992). Recently Brand & Blitz (1993) have re-derived the outer rotation curve from CO radial velocities of OB stars associated with H II regions, and Pont et al. (1994) have used new radial velocity measurements of classical cepheids for this purpose. All these methods rely on

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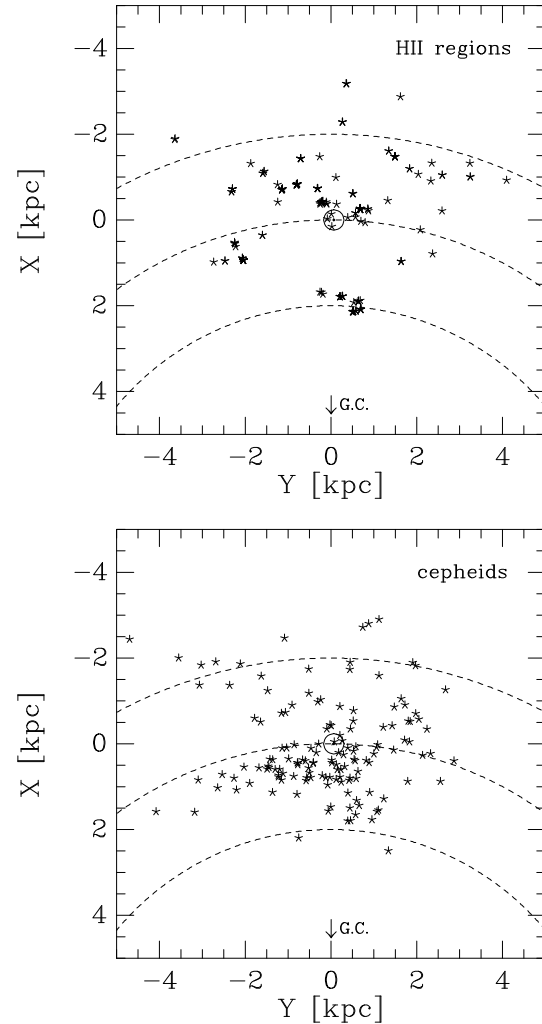


Fig. 1. Positions of the H II regions (upper panel) and the cepheids (lower panel), for which the proper motions are well-known, projected onto the galactic plane. The position of the Sun is in the centre of the panels. The dashed lines indicate circles around the galactic centre with radii 6.5, 8.5 and 10.5 kpc, respectively.

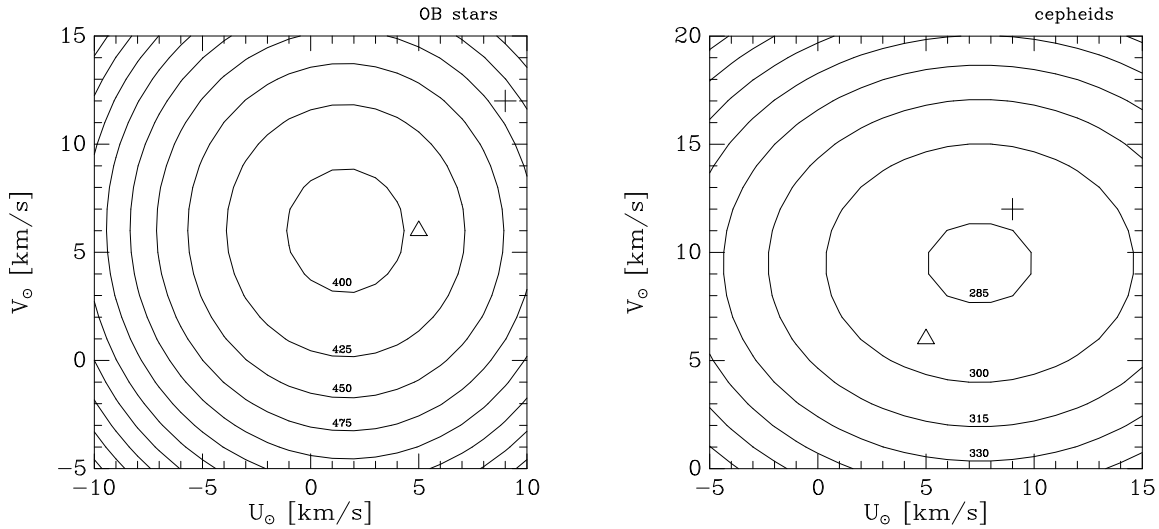


Fig. 2. Contourmaps of the numerical value of χ^2 as a function of the solar motion U_0 and V_0 . A cross indicates the standard value of $U_0 = 9$ km/s, $V_0 = 12$ km/s, a triangle the value $U_0 = 5$ km/s, $V_0 = 6$ km/s used in the present study. Note that the contours are steeper in the fit to the OB star data (left panel) than in the fit to the cepheid data (right panel).

the assumption of circular orbits around the galactic centre, so that radial velocities can be converted to circular velocities. Obviously proper motions of the objects may provide independent information on the rotation curve. The PPM catalogue which has recently been compiled at the Astronomisches Rechen-Institut (Röser & Bastian 1991, Bastian et al. 1993, Röser et al. 1994) is well suited as a broad data base of proper motions of high accuracy for such purposes.

2. Data

2.1. OB stars

Brand & Blitz (1993) give a list containing radial velocities of H II regions and their associated molecular cloud complexes which is the basis of our analysis. The exciting OB stars in the northern hemisphere are tabulated by Georgelin (1975) and others (see Blitz et al. 1982 for references) and can be identified by cross reference numbers. For the exciting OB stars of the H II regions in the southern hemisphere finding charts are given by Brand (1986). Using cross reference numbers, spectral types, magnitudes or accurate stellar positions, which we derived in an intermediate identification step using the HST Guide Star Catalog (Lasker et al. 1990), we have identified as many stars from the source lists in the PPM Star Catalogue as possible.

In total we have been able to identify 228 OB stars associated with 71 H II regions.

2.2. Cepheids

Radial velocities and distances of classical cepheids are taken from the recent work of Pont et al. (1994). Using again accurate stellar positions and cross reference numbers, which we obtained from the HIPPARCOS Input Catalogue (Turon et al. 1992) and from Kholopov et al. (1985-1987), we were able to identify 152 cepheids in the PPM Star Catalogue.

The PPM Star Catalogue is tied into the FK5 system (Fricke et al. 1988). Lindegren et al. (1995) have shown by a systematic comparison of the FK5 system with preliminary HIPPARCOS data that the FK5 positional system has still deficiencies, in particular in a strip at about $\delta \approx -40^\circ$, corresponding to $l \approx 260^\circ$, $b \approx 0^\circ$. Unfortunately a number of H II regions and cepheids fall into this area, which we have omitted from our analysis because of this systematic uncertainty, leaving us with 197 OB stars associated with 59 H II regions and 144 cepheids with well-determined proper motions for our final analysis. Tables 1 and 2 give the identification numbers of these stars in the PPM catalogue.

Using the positions and proper motions of the stars given in the PPM Star Catalogue and the distances and the radial velocities given by Brand & Blitz (1993) or Pont et al. (1994), respectively, we have calculated the positions and the velocities of the stars in galactic coordinates. Fig. 1 shows the projection of the positions of the objects onto the galactic plane. X and Y are the cartesian spatial coordinates of the stars relative to the Sun. The X -axis points towards the galactic centre and the Y -axis into the direction of galactic rotation.

Table 1. H II regions and their associated OB stars. The first column gives the Sharpless or Brand identification numbers of the H II regions. The second column gives the identification numbers of the OB stars in this region which could be found in the PPM Star Catalogue.

H II	PPM	H II	PPM	H II	PPM	H II	PPM
S8	296225	S140	23638	S234	70368	BBW16	727432
	296206		23640		70374		252138
S11	296337	S142	41076	S236	70266		727439
S25	267779		41098		70271		727444
	267782	S154	23983		70273	BBW17B	252139
	267822	S155	24016	S238	119824		252148
	267797		24060	S252	95519		252158
S29	267950		24070	S263	148818	BBW23	252308
S31	267973		24074	S264	149155		252289
S32	267965		24030		149166		252363
	267970		24072	S273	151033		252304
	267964		23979		151058	BBW29	252486
S27	231915		24019		151028	BBW104B	284824
S41	234340		24021		151013	BBW106	740844
	234237		24036		151053	BBW127	285005
	234243		24043		151030		740995
	234273		24049		151073		740981
	234280		24098		151050		740980
	234293		24093	S275	150705	BBW133	285078
	234337		24117		150694		741033
	234362		24148		150692	BBW283	769065
S44	234275		24150		150670		338612
S45	234399		24162		150682	BBW300B	338995
	234410		24169		150706		339034
S46	234023		24185	S277	188303		339041
S49	234332		24186	S279	188224		338930
	234333	S157	24306	S281	187839	BBW316D	339247
	234345	S161	24309		175945	BBW347	339851
	234348		24329		188455	BBW348A	358562
S54	234320	S162	24384		175888		358560
	234299	S170	11863		188218	BBW362A	358835
	234306	S173	12143		188223		358846
	234321	S184	25788		188225		358849
	234336		25791		188149		358855
	234352	S190	13731		215598		358857
	234357		13702	S292	218092		358862
S86	109578		13720	S293	218026		358863
	109560		13721	S295	218051		358865
	109575		13723	S296	218372		358869
S101	83984		13712		218096		358872
S112	60147		13718		218138		358875
S117	60726	S199	28316		218164		358876
S119	61260		28326		218171		358883
S124	39725	S202	14174		218242		358884
S126	88031		14185		218262	BBW362C	358747
S129	39225		14227		218324		358742
S132	40485	S206	28874	S297	218121	BBW362F	358755
S134	40324	S220	68961	S310	252114		
S137	23309	S232	70744	S311	253358		
	23333	S234	70403		253404		

Table 2. Cepheids used to calculate the rotation curve.

cepheid	PPM	cepheid	PPM	cepheid	PPM	cepheid	PPM
η Aql	168843	SU Cas	13918	V1334 Cyg	86379	U Sgr	234663
U Aql	202954	SW Cas	41496	β Dor	354837	W Sgr	267817
SZ Aql	167110	SZ Cas	27633	ζ Gem	96982	X Sgr	267303
TT Aql	167242	XY Cas	12507	W Gem	122711	Y Sgr	234421
FF Aql	135550	DL Cas	12258	V Lac	41123	WZ Sgr	234281
FM Aql	135861	FM Cas	25159	X Lac	41132	XX Sgr	234503
FN Aql	167384	V636 Cas	13051	Y Lac	40284	YZ Sgr	235075
V336 Aql	167002	V Cen	342919	Z Lac	40952	AP Sgr	268062
V496 Aql	202574	UZ Cen	358897	RR Lac	40959	AY Sgr	719227
V600 Aql	167670	XX Cen	342137	BG Lac	62336	BB Sgr	268971
Y Aur	48141	BB Cen	359040	GH Lup	343690	V350 Sgr	268853
RT Aur	71665	BK Cen	358996	T Mon	150465	RV Sco	295723
RX Aur	69838	V378 Cen	360023	SV Mon	150342	RY Sco	296879
SY Aur	47840	V381 Cen	342310	R Mus	359566	KQ Sco	762230
RY CMa	218422	V419 Cen	340152	S Mus	371417	V482 Sco	296427
RZ CMa	713898	δ Cep	40731	RT Mus	358941	V500 Sco	296821
SS CMa	252386	CR Cep	41067	UU Mus	359025	V636 Sco	322879
TV CMa	713601	AX Cir	361050	S Nor	344832	X Sct	234646
TW CMa	713915	R Cru	359375	U Nor	344085	Y Sct	201965
VZ CMa	727576	S Cru	341409	Y Oph	201153	Z Sct	202059
RW Cam	28771	T Cru	359350	BF Oph	266398	RU Sct	202038
RX Cam	28898	X Cru	341282	RS Ori	122354	SS Sct	202078
ι Car	357533	VW Cru	359483	SV Per	47393	EV Sct	707164
U Car	339614	AG Cru	341197	SX Per	46949	ST Tau	121352
V Car	356744	BG Cru	341066	VX Per	27145	SZ Tau	120081
Y Car	339156	X Cyg	85419	AW Per	69651	R Tra	361350
UW Car	339046	SU Cyg	109630	V440 Per	27565	S Tra	361800
UX Car	339090	SZ Cyg	60114	X Pup	252643	U Tra	361877
XX Car	358358	TX Cyg	60815	RS Pup	284941	α UMi	431
XY Car	358418	VX Cyg	60748	VX Pup	252632	V Vel	337875
XZ Car	358450	VY Cyg	85963	VZ Pup	727776	SV Vel	339405
YZ Car	339070	VZ Cyg	62131	WX Pup	252971	BG Vel	337630
ER Car	339816	CD Cyg	84139	WZ Pup	728158	T Vul	112020
GI Car	339882	DT Cyg	86036	AQ Pup	253563	U Vul	109337
IT Car	358563	V386 Cyg	61152	AT Pup	284926	X Vul	110094
RY Cas	42304	V532 Cyg	61309	S Sge	137241	SV Vul	109871

3. Data reduction

3.1. Angular velocity of the LSR

In the FK5 system the velocities of the stars have a component of rigid rotation due to the motion of the LSR around the galactic centre. Assuming now that the stars move on circular orbits around the galactic centre and that the rotation curve is flat, one may fit a model of the form

$$\begin{aligned} U &= \Omega_0 R_0 \sin \varphi \\ V &= \Omega_0 R_0 (\cos \varphi - 1) \end{aligned} \quad (1)$$

to the space velocities of the stars. U and V correspond to the directions of the X - and Y -axis of Fig. 1 and denote the space velocities of the stars which have been corrected for the solar motion with respect to the LSR (cf. section

3.3). R_0 is the distance of the Sun from the galactic centre which we assume as 8.5 kpc throughout the present study, φ denotes the galactic azimuthal angle of a star.

Since some of the stars are fairly distant from the Sun we do not use Oort's approximation but adopt rigorous formulae describing a flat rotation curve. Deviations of the stars from the midplane are ignored.

From a χ^2 -fit of eq. (1) to the space velocities of the 197 OB stars we find

$$\Omega_0 = 5.5 \pm 0.4 \text{ mas/a} \quad (2)$$

for the angular velocity of the LSR which corresponds to a circular velocity of 223 ± 14 km/s in good agreement with the IAU 1985 value of 220 km/s.

Table 3. Effects of the correction of the constant of precession by $\Delta p_1 = -3.2 \text{ mas/a}$ and different corrections of the motion of the equinox Δe on the angular velocities Ω_0 , Ω_1 and Ω_2 . Ω_0 is the angular velocity of the LSR and $\sqrt{\Omega_1^2 + \Omega_2^2}$ is the tilting of the galactic plane which should be minimized by adjusting Δe . Only OB stars with distances greater than 800 pc from the sun are considered in order to avoid contamination by Gould’s Belt. The mean error of an angular velocity component is about 0.5 mas/a.

OB stars					cepheids				
Δe [mas/a]	Ω_0 [mas/a]	Ω_1 [mas/a]	Ω_2 [mas/a]	$\sqrt{\Omega_1^2 + \Omega_2^2}$ [mas/a]	Δe [mas/a]	Ω_0 [mas/a]	Ω_1 [mas/a]	Ω_2 [mas/a]	$\sqrt{\Omega_1^2 + \Omega_2^2}$ [mas/a]
0.0	7.19	1.26	-2.99	3.24	0.0	6.86	-0.43	-1.96	2.01
-1.0	6.77	0.59	-2.14	2.22	-1.0	6.43	-0.93	-1.21	1.53
-2.0	6.37	-0.06	-1.30	1.30	-2.0	6.02	-1.41	-0.47	1.49
-3.0	5.96	-0.72	-0.46	0.85	-3.0	5.59	-1.90	0.29	1.92
-4.0	5.55	-1.38	0.40	1.44	-4.0	5.18	-2.39	1.04	2.61
-2.9	5.98	-0.68	-0.50	0.84	-1.5	6.23	-1.17	0.84	1.44

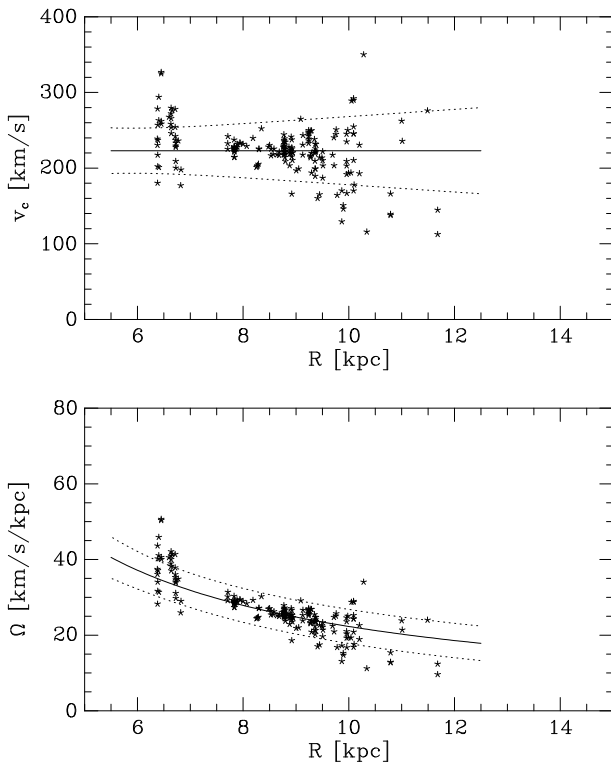


Fig. 3. Rotation curve derived from the OB star data using the full space velocities. The upper panel shows the circular velocity, whereas the lower panel shows the angular velocity of the 197 OB stars associated with 59 H II regions. The solid lines indicate the rotation law of a flat rotation curve. The dotted lines indicate error estimates based on the errors of the proper motions, radial velocities and distances of the stars.

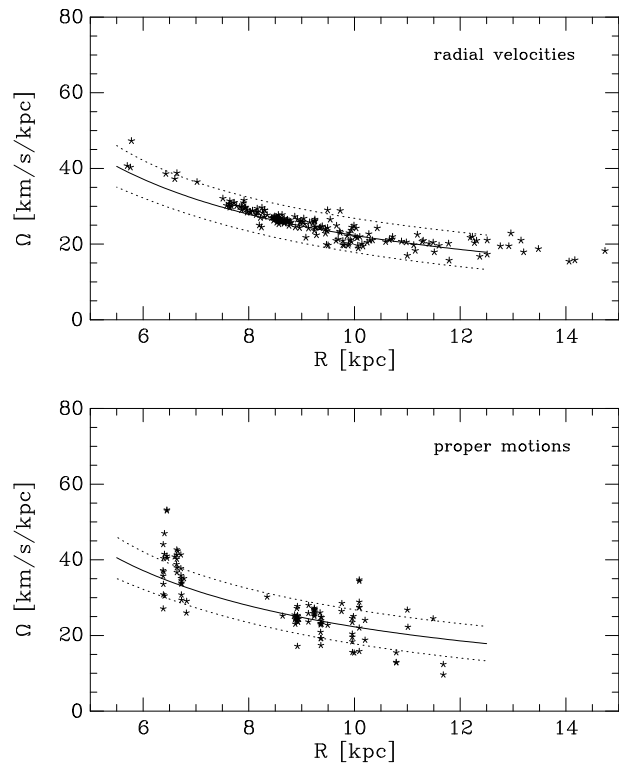


Fig. 4. Rotation curves derived from the OB star data using only radial or tangential velocity components, respectively, assuming circular orbits of the stars. There are 193 H II regions with measured radial velocities (upper panel; this is essentially the rotation curve derived by Brand & Blitz (1993)) and 104 OB stars with known proper motions and suitable projection angles.

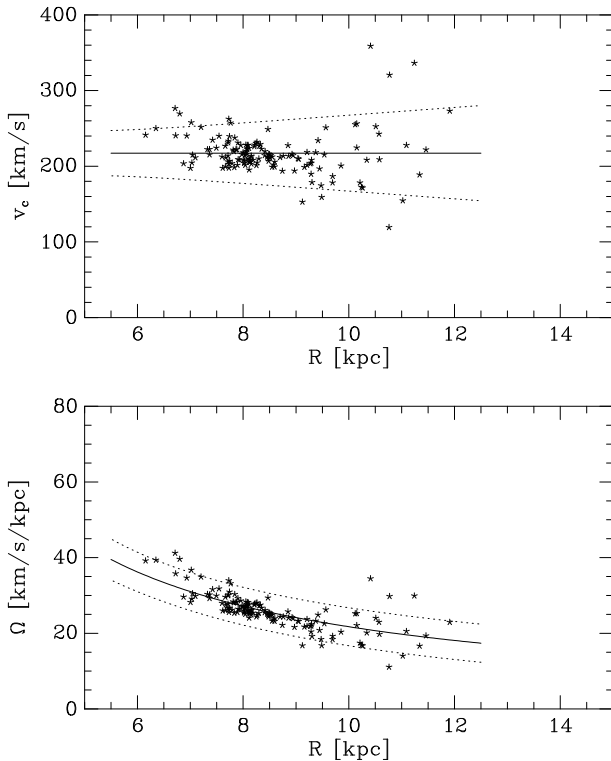


Fig. 5. Rotation curve derived from the cepheid data using the full space velocities of 144 cepheids. The representation is the same as in Fig. 3.

From the data of the 144 cepheids we obtain

$$\Omega_0 = 5.4 \pm 0.5 \text{ mas/a} \quad (3)$$

in good agreement with the OB stars.

The estimated error of Ω_0 has been calculated from the errors given individually for the proper motions of each star in the PPM catalogue and the errors of the radial velocities and the distances given in our reference lists. Furthermore we took into account the velocity dispersion of the stars relative to the circular orbits by an additional error of 6.5 km/s in both velocity components for the OB stars (Brand & Blitz 1993) and of 13 km/s in the U- and 9 km/s in the V-direction for the cepheids (Pont et al. 1994), respectively.

Judging from the numerical value of χ^2 and the statistical distribution of the velocity residuals we found that the error estimates obtained this way were too low and have increased the errors of the proper motions by 30%. This is apparently due to systematic errors of the proper motions in the PPM catalogue defined in the reference frame of the FK5 system, which are not fully represented by the individual errors given there.

3.2. Influence of the reference system

Moreover there is a further source of potentially serious errors of the proper motions which is related to non-physical

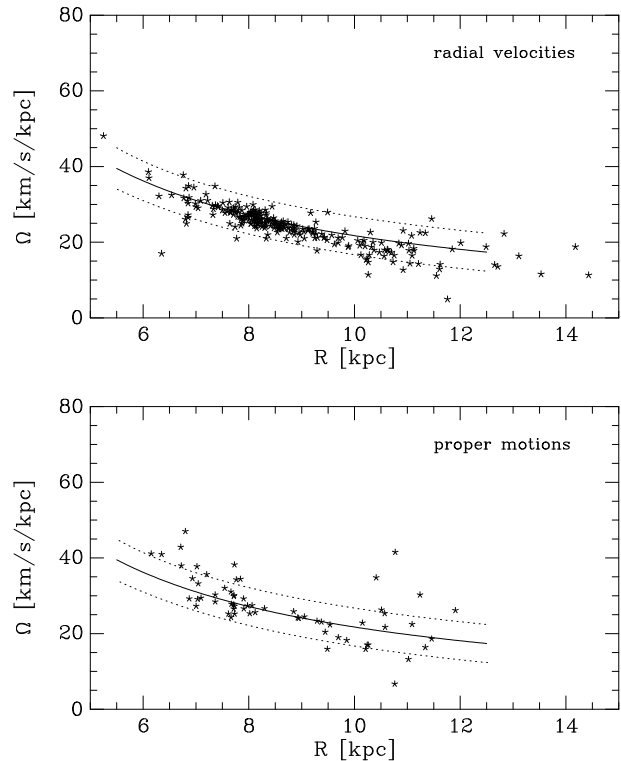


Fig. 6. Rotation curve derived from cepheid data using only radial velocities or proper motions, respectively. The upper panel shows essentially the rotation curve from Pont et al. (1994) using radial velocity components of 249 cepheids. The lower panel shows the rotation curve using proper motions of 63 cepheids with suitable deprojection angles.

global rotations of the reference system. There is now a general agreement that the IAU (1976) value of the constant of precession, proposed by Fricke (1977) and used in the construction of the FK5, has to be corrected by about $\Delta p = -3.2 \pm 0.3 \text{ mas/a}$ (Williams et al. 1994). This corresponds to a rigid rotation with a spin vector pointing to the ecliptical pole.

The immediate effects on our results are illustrated in Table 3. To each star the correction has been applied and both data sets have been reduced again according to the procedure described above. Ω_0 is again the angular velocity of the LSR with respect to the galactic centre. Ω_1 and Ω_2 are angular velocities of the mean rotation of all stars about axes lying in the galactic plane, pointing towards the galactic centre ($l = 0^\circ$) and the direction of galactic rotation ($l = 90^\circ$), respectively.

As can be seen from Table 3 the introduction of the correction of the constant of precession leads to an unacceptably large apparent tilting of the galactic plane. Following Fricke (1977) we have therefore considered a simultaneous correction of the motion of the vernal equinox Δe . This corresponds to a rigid rotation of the reference frame about an axis pointing towards the celestial pole. Table 3

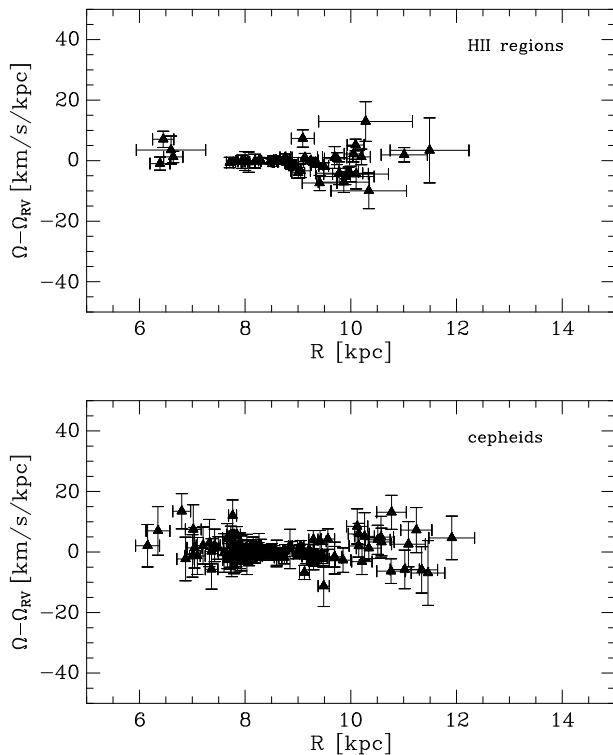


Fig. 7. The rotation curve derived solely from radial velocities assuming circular orbits around the galactic centre, subtracted from the rotation curve based on the space velocities of 48 H II regions (upper panel, where stars belonging to the same H II region have been grouped together) and 124 cepheids (lower panel). Stars in the direction of the galactic centre or anticentre have been excluded. Individual errors are indicated.

shows that the apparent tilting of the galactic plane can be minimized by adopting a value of $\Delta e = -2.9 \text{ mas/a}$ for the OB stars or of $\Delta e = -1.5 \text{ mas/a}$ for the cepheids. Nevertheless the remaining tilting is significantly higher than in the case where no correction at all was applied, i. e. 0.35 mas/a for OB stars with distances greater than 800 pc and 1.10 mas/a for cepheids. In all these cases Ω_0 agrees within 1 mas/a with the values given above. This discrepancy cannot be solved on the basis of the present material.

The corrections Δe of the motion of the equinox suggested here are of the same order of magnitude as those proposed by Miyamoto and Sôma (1993) and by Wielen (unpublished). They do not agree exactly mainly because of different samples of stars used. Miyamoto and Sôma derived $\Delta e = -1.2 \text{ mas/a}$ from K giants. Wielen obtained $\Delta e = -3.2 \text{ mas/a}$ from 512 FK5 stars which were used by Fricke (1977) for deriving the constant of precession and the motion of the equinox and which were re-investigated by Schwan (1988) after the FK5 was completed. We conclude that the spurious, non-physical rotations of the FK5 system seem to be in total of the order of $\pm 1 \text{ mas/a}$ in each component of the rotation vector. This is consistent with

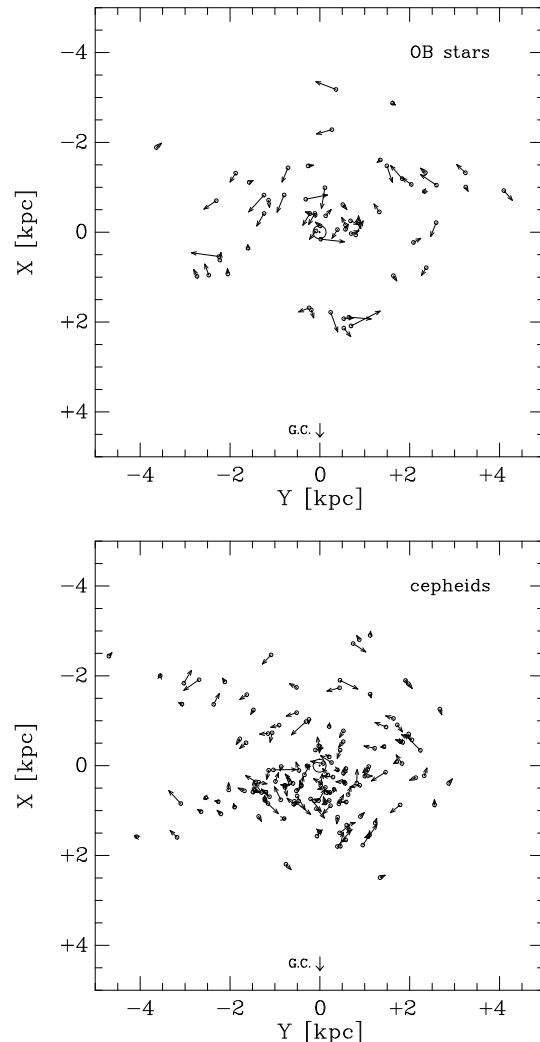


Fig. 8. Velocity residuals projected onto the galactic plane after subtraction of a flat rotation curve, normalized by the individual errors of the space velocities. A normalized residual of unit one corresponds to a vector with a length of 150 pc in the diagram. Notice the aligned velocity pattern in the Perseus spiral arm in the upper right quadrant for the OB stars (upper panel). The cepheids (lower panel) do not show a similar feature.

the claimed accuracy of the FK5 system with respect to non-physical rotations of about $\pm 0.7 \text{ mas/a}$ (Fricke 1977, Schwan 1988).

Finally we note that the VLA measurement of the proper motion of the Sgr A* radio source in the galactic centre of $-6.55 \pm 0.34 \text{ mas/a}$ (Backer 1996), implying after subtraction of the peculiar velocity of the Sun an angular velocity of the LSR of $\Omega_0 = 6.4 \text{ mas/a}$, deviates only insignificantly from the values found here.

3.3. Solar motion

Before applying Eq. (1) the space velocities have to be corrected for the solar motion with respect to the LSR. The standard values for this motion are $U_0 = 9$ km/s and $V_0 = 12$ km/s (Delhaye 1965).

We introduced U_0 and V_0 as additional free parameters in Eq. (1) and checked the goodness of the fit for various combinations of U_0 and V_0 . The results are shown in Fig. 2.

The χ^2 -fit to the OB star data rejects the standard values of 9 and 12 km/s at a 4σ confidence level, whereas the fit to the cepheid data is in good agreement with the classical values. The minimum of the numerical value of χ^2 for the cepheids however is quite flat and the errors are larger than those for the OB stars, so we decided to use values of $U_0 = 5$ km/s and $V_0 = 6$ km/s, which correspond within the errors simultaneously to the minima of χ^2 of both data sets.

Note that the value of V_0 is closely related to the asymmetric drift of the sample of stars under consideration. Jahreiß and Wielen (1983) found $V_0 = 5$ km/s relative to the youngest stars in the solar neighbourhood in close agreement with the value used here. The low value of U_0 reflects the apparent inward motion of stars relative to the LSR which was noted previously by Fich et al. (1989). This effect is usually interpreted as an outward motion of the LSR (Blitz & Spergel 1991).

3.4. Oort's constants

We have determined Oort's constants A and B using stars within a circle of 1 kpc around the Sun, assuming a constant radial gradient of the rotation curve near the Sun. By means of a χ^2 -fit to the circular velocity

$$v_c(R) = v_c(R_0) + \left(\frac{dv_c}{dR}\right)_0 (R - R_0) \quad (4)$$

we find for the OB stars $A = 14.0 \pm 1.2$ km/s/kpc and $B = -12.3 \pm 1.2$ km/s/kpc, which agree nicely with the flat shape of the rotation curve over larger distance intervals. The cepheids give $A = 15.8 \pm 1.6$ km/s/kpc and $B = -9.7 \pm 1.6$ km/s/kpc. Obviously Oort's constants only reflect the local behaviour of the rotation curve. Over larger distance intervals the rotation curves show a flatter shape than one would assume from the above values.

4. Results and Discussion

4.1. Rotation curves

Once the velocities have been corrected for the solar motion, it is straightforward to determine the circular velocity $v_c(R)$ for according to the formula

$$v_c = (U - \Omega_0 Y) \sin \varphi + (V + \Omega_0 X) \cos \varphi + \Omega_0 R, \quad (5)$$

where R is the distance of the star from the galactic centre. It is now no longer necessary to assume that the stars move

on circular orbits around the galactic centre, because the full space velocities are used.

Alternatively, assuming again circular orbits, one may derive rotation curves based solely on radial or tangential velocity components of the stars,

$$\Omega_0(R) = \frac{v_{\text{rad}}}{R_0 \sin l \cos b} + \Omega_0 \quad (6)$$

$$\Omega_0(R) = \frac{(\mu_l + \Omega_0)r \cos b}{R \cos(\varphi + l)} + \Omega_0, \quad (7)$$

where r denotes the distance of the star from the Sun, v_{rad} the radial velocity, and μ_l the proper motion in the direction of galactic longitude l . Both velocities have to be corrected again for the solar motion. r is the distance of the star from the Sun.

The resulting rotation curves determined using either the full space velocities or deprojected radial or tangential velocity components are shown in Figs. 3 to 6. They agree very closely and are all consistent with a flat shape of the rotation curve $\Omega(R) = \Omega_0 R_0 / R$.

Stars with unsuitable projection angles onto the supposed circular velocities have been excluded. In the case where only radial velocity data are used stars with $|\sin l| < 0.3$ have been rejected. If only proper motion data are used stars with $|\cos(\varphi + l)| < 0.7$ have been rejected. Therefore the overlap between these two samples is small and we cannot correlate directly the rotation curve derived from radial velocities with the rotation curve based on proper motions or both.

Instead, we show in Fig. 7 the deviations of circular velocities derived from the space velocities from circular velocities based solely on deprojected radial velocities of the stars illustrating again that both methods give consistent results.

4.2. Residual velocities

The orientations of the velocity residuals after subtraction of the systematic velocity components due to a flat rotation curve from the space velocities of the stars are shown in Fig. 8 projected onto the galactic plane. The velocity residuals are dominated by the errors of the proper motions. Most of the velocity residuals can be shown to be randomly orientated with the exception of the Perseus spiral arm. There is a trend of coherent motion along the spiral arm with the effect that the OB stars in the spiral arm tend to lag behind the general rotation of the disk. Exactly such a behaviour is predicted by the density wave theory of spiral structure for stars recently born in the shock front of the interstellar gas included by the spiral density wave (Shu et al. 1972). This is not observed for the cepheids. They are about 100 times older than the OB stars and their systematic flow pattern is already dissolved (Wielen 1979).

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