

# Quark Coalescence and Charm(onium) in QGP

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**Abstract.** The potential of heavy quarks as probes of the environment produced in hadronic and heavy-ion reactions is discussed. A key role is played by coalescence processes and/or resonance formation which are promising candidates to provide a comprehensive understanding of phenomena associated with reinteractions of both open and hidden heavy-quark states.

**PACS.** 12.38.Mh Quark-Gluon Plasma – 25.75.-q Relativistic Heavy-Ion Collisions – 14.40.Lb Charmed Mesons

## 1 Introduction

In hadronic and heavy-ion collisions, heavy quarks ( $Q=c, b$ ) are believed to be (almost) exclusively pair-produced ( $Q\bar{Q}$ ) upon first impact in hard partonic collisions [1]. This renders them excellent agents of the subsequently formed medium and their reinteractions within. The latter include: (a) coalescence with surrounding quarks as hadronization mechanism in addition to fragmentation, thereby probing the chemical and kinematic properties of the medium [2, 3, 4, 5, 6]; (b) energy loss of high-momentum  $Q$ -quarks [7, 8], which, with increasing interaction strength toward lower momentum, eventually leads to (c) thermalization [9, 10, 11, 12]; and, if the latter can be established, (d) in-medium dynamics of open and hidden heavy-flavor states [13, 14, 15, 16, 17], which is particularly exciting in view of recent QCD lattice calculations [18, 19, 20] indicating the survival of low-lying charmonia well into the Quark-Gluon Plasma (QGP). In this paper we will address the above issues essentially in that order.

## 2 Coalescence in Hadronic Collisions

In elementary hadronic reactions ( $pN, \pi N$ ) evidence for reinteractions of  $c$ -quarks arises from (large) flavor asymmetries in  $D$ -meson production yields. The asymmetries are most pronounced at forward rapidities (or  $x_F$ ), successfully being attributed to coalescence of  $c$ -quarks with valence quarks of the projectile [4]. The pertinent recombination cross section can be written as [2]

$$x^* \frac{d\sigma_D^{rec}}{dx_F} = \int \frac{dx_{\bar{q}}}{x_{\bar{q}}} \int \frac{dz}{z} \left( x_{\bar{q}} z^* \frac{d^2\sigma^{(c\bar{q})}}{dx_{\bar{q}} dz} \right) \mathcal{R}(x_q, z; x_F), \quad (1)$$

where the main elements are: (i) the  $c\text{-}\bar{q}$  production cross section composed of a 2-parton distribution function (2-PDF),  $f_{i\bar{q}}^{(2)}$  (where  $i=g, q, \bar{q}$  participates in the hard process

to produce the  $c\bar{c}$  pair), and the standard perturbative QCD (pQCD)  $c\bar{c}$  cross section, and (ii) the  $c\text{-}\bar{q} \rightarrow D$  recombination function,  $\mathcal{R}$ . The 2-PDF is usually factorized into two single PDFs with phase space correction,

$$f_{i\bar{q}}^{(2)} = C f_{\bar{q}}(x_{\bar{q}}) f_i(x_i) (1 - x_{\bar{q}} - x_i)^p, \quad (2)$$

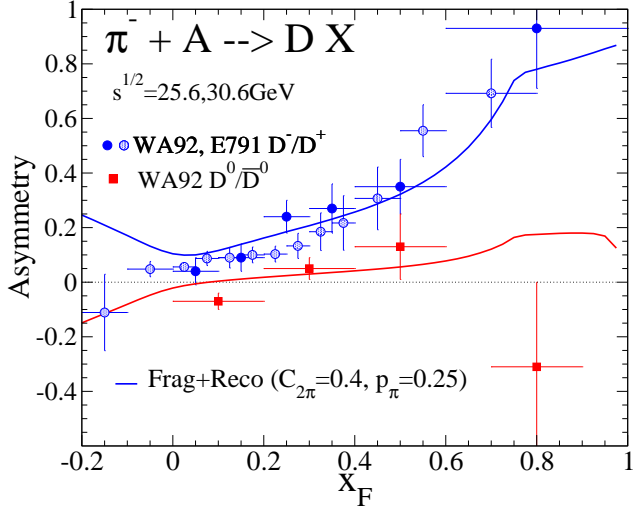
whereas  $\mathcal{R}$  represents a  $D$ -meson wave function which in Ref. [6] has been assumed to be Gaussian in rapidity space,

$$\mathcal{R}(y_{\bar{q}}, y_c, y) = \exp(\Delta y^2 / 2\sigma_y^2) / \sqrt{2\pi\sigma_y^2}. \quad (3)$$

This form of the recombination function [21] allows to generalize the coalescence formalism to include sea-quarks [6], and thus address flavor asymmetries also at central  $x_F$ , cf. Fig. 1. The experimentally observed asymmetries in inclusive yields ( $x_F > 0$ ) are quite appreciable, *e.g.*,  $D^-/D^+ = 1.35 \pm 0.05$  (versus 1 in isospin-symmetric fragmentation),  $D^0/\bar{D}^0 = 0.93 \pm 0.03$  (vs. 1) and  $D^\pm/(\bar{D}^0 + D^0) = 0.415 \pm 0.01$  (vs. 0.33) for fixed-target  $\pi^- N$  collisions (averaged over a weak energy dependence for  $\sqrt{s} = 19\text{-}34\text{ GeV}$ ) [23]. The data are rather well reproduced by a combined coalescence + fragmentation approach [6] (for a somewhat different framework based on power corrections, see Ref. [5]).

## 3 Open Charm in the QGP

Final-state interactions of heavy quarks are enhanced when embedding them into a heavy-ion collision, where, at ultrarelativistic energies, intense reinteractions of light partons are believed to form locally thermalized matter within a time of  $\tau \lesssim 1\text{ fm}/c$ . At high momenta  $c$ -quarks rescatter perturbatively inducing a softening of the primordially power-like  $p_t$ -spectra, with subsequent hadronization in the vacuum (fragmentation). The predicted suppression

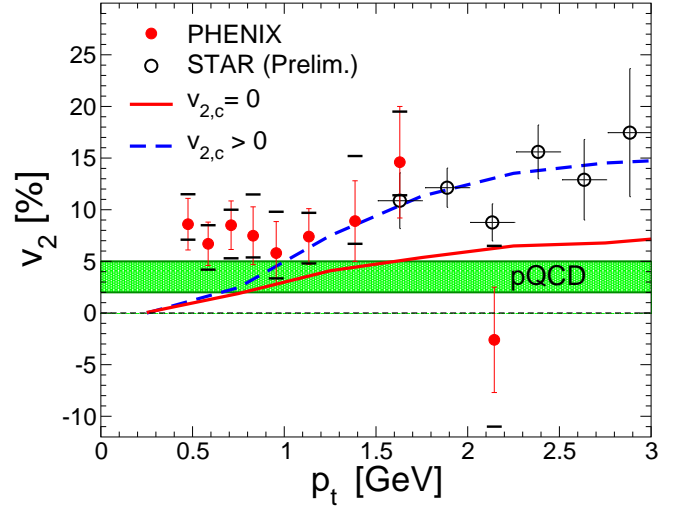


**Fig. 1.**  $D$ -meson flavor asymmetries,  $A = (N_{D_1} - N_{D_2}) / (N_{D_1} + N_{D_2})$ , in  $\pi^-$ - $A$  reactions [22,23] compared to coalescence + fragmentation calculations [6]. Upper data points and curves are for  $D_1 = D^-$  and  $D_2 = D^+$ , whereas lower data points and curves are for  $D_1 = D^0$  and  $D_2 = \bar{D}^0$ . “Leading” particles ( $D^- = \bar{c}d$ ,  $D^0 = c\bar{u}$ ) are defined as sharing a valence quark with the projectile ( $\pi^- = d\bar{u}$ ); note that the approximate absence of an asymmetry for  $D^0/\bar{D}^0$  is accounted for in the model due to the predominant production of  $c\bar{c}$  pairs in the forward direction via  $\bar{u}u$  annihilation, rendering the valence  $\bar{u}$  unavailable for recombination.

factors relative to  $p$ - $p$  collisions range from 0.2 [8] to 0.5 [7], with a rather small azimuthal asymmetry,  $v_2 \leq 5\%$  [24].

Toward lower  $p_t$ , the phase space density of the medium increases and coalescence with light quarks is expected to become competitive [25,26,27]. The same expression, Eq. (1), can be applied with the light quark distributions being replaced by thermal (+ quenched pQCD) ones as established from light hadron production systematics (also, the recombination function  $\mathcal{R}$  is typically substituted with a hadron wave function in transverse momentum). The extension to low  $p_t$  is, in principle, more controlled than for light-light ( $q$ - $\bar{q}$ ) coalescence, since at the scale of the hadronization temperature, secondary  $c$ -production is negligible. With previously determined light-quark distributions, charmed-hadron spectra become a sensitive probe of the dynamics of  $c$ -quarks in the QGP. This has first been quantified in the context of “charm-like” single-electron spectra in Ref. [25], showing that  $v_2^c(p_t)$ : (a) closely reflects the  $v_2$  of the parent  $D$ -meson, (b) exhibits a marked difference of more than a factor of 2 between the cases where the  $c$ -quark distributions are either taken from  $p$ - $p$  collisions, or assumed to follow the systematics of light quarks (including collective expansion), cf. Fig. 2. Current data at RHIC from PHENIX [28] and STAR (preliminary) [29] seem to favor the quasi-thermalized scenario. If confirmed, this raises at least two further questions:

(i) Is the predicted  $v_2^c$  consistent with pertinent  $p_t$ -spectra (*i.e.*, the ratio of central  $Au$ - $Au$  to collision-scaled  $p$ - $p$  spectra,  $R_{AA}$ )?

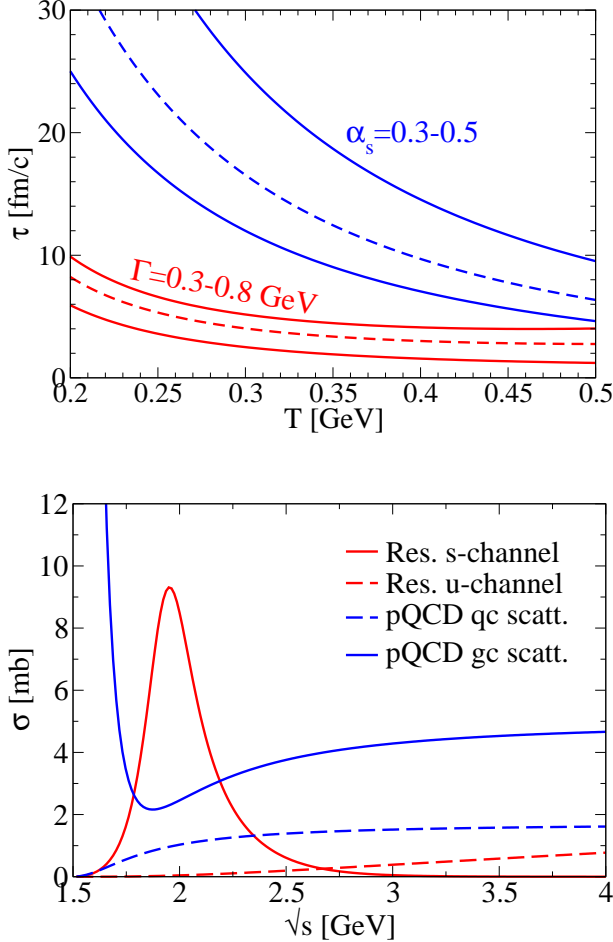


**Fig. 2.** Azimuthal asymmetry of “non-photonic” single- $e^\pm$  spectra in minimum bias  $Au$ - $Au$  ( $\sqrt{s_{NN}} = 200$  GeV) [28, 29] compared to coalescence model predictions [25] using  $c$ -quark distributions from either  $p$ - $p$  collisions ( $v_2^c = 0$ , solid line) or assuming a transverse flow and  $v_2$ -profile as determined for light quarks from fits to light-hadron spectra ( $v_2^c > 0$ , dashed line). The band indicates predictions from jet-quenching [24] applicable at sufficiently high  $p_t$ .

(ii) What are microscopic mechanisms for thermalization of  $c$ -quarks (or  $D$ -mesons)?

Concerning (i), it has been pointed out [30] that for single- $e^\pm$   $p_t$ -spectra in central  $Au$ - $Au$ ,  $N_{coll}$ -scaled  $D$ -meson spectra from  $p$ - $p$  collisions lead to results rather similar to a scenario based on full thermalization and collective flow close to hadronic freezeout ( $T \simeq 130$  MeV,  $v_\perp = 0.65$ ), due to large blue shifts with  $m_D = 1.87$  GeV (also, bottom-decay contributions become significant above  $p_t^c \simeq 3$  GeV). However, in hydrodynamic analysis [12] coupled with a Fokker-Planck treatment of  $c$ -quarks in the QGP, a  $v_2^c$  of  $\sim 10$ -15% is associated with  $R_{AA}^c(p_t \geq 3 \text{ GeV}) \leq 0.1$ . Coalescence model calculations [25], based on recombination at the phase boundary, imply a suppression factor similar to jet quenching,  $R_{AA}^D(p_t \simeq 3 \text{ GeV}) = 0.2$ -0.5, but with  $v_2^D(p_t \simeq 3 \text{ GeV}) \simeq 15\%$ . Note that when starting from  $c$ -quark spectra, fragmentation leads to a degradation, whereas coalescence to an increase, of the resulting  $D$ -meson  $p_t$ .

Concerning (ii), it has been known for a while [9] (and confirmed in Refs. [10,11]) that perturbative  $c$ -quark rescattering off quarks and gluons in the QGP implies kinetic relaxation times  $\tau_c^{therm} \gtrsim 10$  fm/c for  $T \simeq 400$  MeV, too long to achieve thermalization at RHIC. However, as shown recently [11], nonperturbative rescattering in the QGP can lead to a substantial acceleration of equilibration: implementing the notion of  $D$ -meson-like resonances within a Fokker-Planck equation, a reduction of  $\tau_c^{therm}$  by a factor of  $\sim 3$  as compared to using pQCD cross sections has been found (for  $T \leq 2T_c$ ), cf. upper panel of Fig. 3 (similar for  $b$ -quarks, but with absolute values  $\tau_b^{therm} \simeq 4\tau_c^{therm}$ ). The main difference in the two mechanisms resides not so much in the total cross sections (lower panel of Fig. 3), but in the



**Fig. 3.** Upper panel:  $c$ -quark equilibration times in QGP with pQCD interactions (upper band; upper [lower] line corresponds to  $\alpha_s=0.3[0.5]$ ) and when adding “ $D$ ”-meson resonance rescattering (lower band; the range of resonance widths indicates variations in the coupling constant of the  $c$ - $q$ - $D$  vertex with the upper [lower] line corresponding to  $\Gamma_D=0.3[0.8]$ GeV) [11]. Lower panel: underlying total  $c$ -parton cross sections.

isotropic angular distribution for the resonance case as opposed to forward-dominated pQCD scattering. It has also been noted [11] that the efficiency of this mechanism relies to a significant part on the  $D$ -states being located *above* the  $c$ - $q$  threshold (*i.e.*, not being boundstates, which renders them inaccessible in  $2 \rightarrow 2$  scattering, especially due to the thermal energies carried by the light quarks). It will be very valuable to check this in QCD lattice calculations, as well as whether previously found  $q$ - $\bar{q}$  and  $Q$ - $\bar{Q}$  states carry over to the  $Q$ - $\bar{q}$  sector. Furthermore, an increasing population of (colorless) “hadronic” states in the cooling process toward  $T_c$  could serve as a mechanism to put phenomenologically successful coalescence models on a firmer basis (also in the light-quark sector). The in-medium mass of open-charm states in the QGP also bears on the production of charmonia, as will be seen in the following section.

From a phenomenological point of view, it should be kept in mind that any process contributing to elastic  $c$ -quark scattering in the QGP,  $c + X_1 \rightarrow c + X_2$ , in principle also gives rise to secondary  $c\bar{c}$  production in the crossed channel,  $X_1 + \bar{X}_2 \rightarrow c + \bar{c}$ , which can be constrained experimentally by total  $c\bar{c}$  yields (including non-trivial centrality dependencies). *E.g.*, in Ref. [27] it has been pointed out that when upscaling the perturbative  $gc \rightarrow gc$  cross section by a factor of 3 (to generate an elliptic flow comparable to light quarks), secondary charm production is at the 40-50% level of the primordial yield in central  $Au$ - $Au$  ( $\sqrt{s}=200$  AGeV). This is expected to be less pronounced for heavier exchange particles, such as “ $D$ ”-mesons.

#### 4 Charmonium in the QGP

A central quantity in evaluating medium effects on quarkonium states,  $\Psi$ , in a heavy-ion collision are their inelastic cross sections,  $\sigma_{\Psi}^{diss}$ , with partons in the QGP, determining the pertinent dissociation rate as

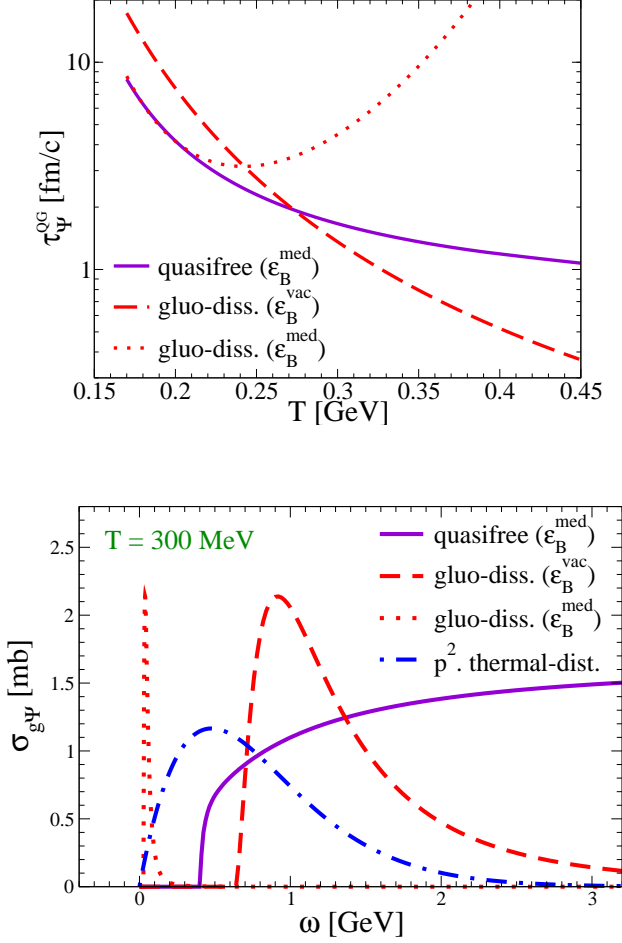
$$\Gamma_{\Psi} = (\tau_{\Psi})^{-1} = \int \frac{d^3k}{(2\pi)^3} f^{q,g}(\omega_k, T) v_{rel} \sigma_{\Psi}^{diss}(s). \quad (4)$$

A widely used model for  $\sigma_{\Psi}^{diss}$  is the gluon-absorption break-up [31,32],  $g + \Psi \rightarrow c + \bar{c}$ , characterized by a pronounced maximum at a gluon energy  $\omega_{max} \simeq 1.5\epsilon_B$  ( $\epsilon_B$ : quarkonium binding energy), see lower panel in Fig. 4. For  $J/\psi$  mesons with their free binding energy,  $\epsilon_B^{vac}=640$  MeV,  $\omega_{max}$  essentially coincides with thermal gluon energies,  $\omega=3T$ , for  $T \simeq 300$  MeV. Debye screening of the  $Q$ - $\bar{Q}$  potential in the QGP is, however, expected to substantially reduce  $\epsilon_B$  [34]. This renders gluodissociation an increasingly inefficient process at higher  $T$  due to a shrinking break-up kinematics, cf. dotted lines in Fig. 4. For small  $\epsilon_B$ , “quasifree” dissociation [33,15],  $g(q, \bar{q}) + \Psi \rightarrow c + \bar{c} + g(q, \bar{q})$ , albeit formally suppressed by one power of  $\alpha_s$ , has been identified as a more important mechanism due to much larger overlap with the thermal (quark + gluon) phase space (cf. solid and dash-dotted lines in the lower panel of Fig. 4).

If the number of heavy quarks in a heavy-ion collision is large enough, their recombination into quarkonia could become a significant (or even dominant) contribution to the final yield [35,36,37,33,38,39]. The conditions for this to happen can be assessed in terms of a simple rate equation for the time evolution of the number of  $\Psi$ ’s,

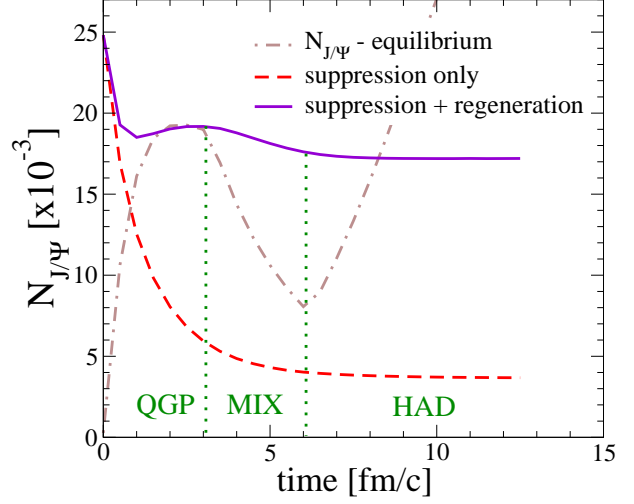
$$\frac{dN_{\Psi}}{dt} = -\Gamma_{\Psi} (N_{\Psi} - N_{\Psi}^{eq}). \quad (5)$$

Besides the reaction rate  $\Gamma_{\Psi}$ , the other quantity governing the evolution of  $N_{\Psi}$  is the equilibrium abundance,  $N_{\Psi}^{eq}(T; \gamma_c)$ , which determines  $\Psi$  regeneration, *i.e.*, the gain term in Eq. (5), as required by detailed balance.  $N_{\Psi}^{eq}(T; \gamma_c)$  is typically evaluated in the canonical ensemble with the total number of (primordial)  $c\bar{c}$  pairs fixed via a fugacity  $\gamma_c = \gamma_{\bar{c}} = e^{\mu_c/T}$ . This implies that  $N_{\Psi}^{eq}(T; \gamma_c)$  is sensitive

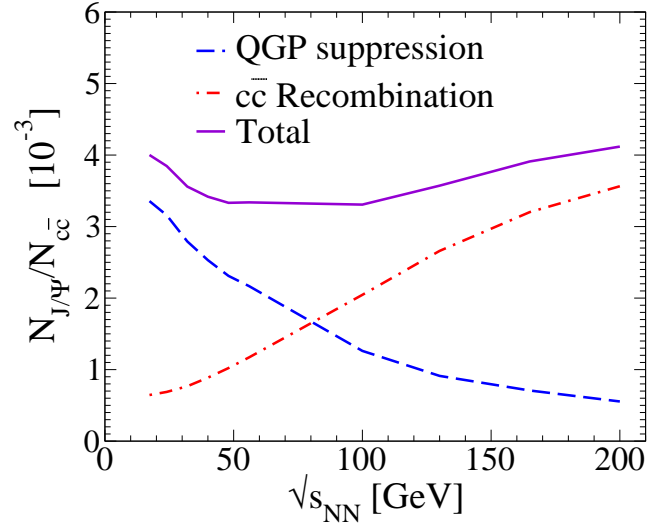


**Fig. 4.** Upper panel:  $J/\psi$  lifetimes in the QGP using gluodissociation [32] with vacuum (dashed line) and in-medium reduced (dotted line) binding energy, as well as quasifree dissociation [33] with in-medium reduced binding energy (solid line). Lower panel: pertinent cross sections (line identification as in upper panel) relative to thermal parton distribution functions (dash-dotted line).

to the open-charm spectrum, in particular (in-medium) masses of  $c$ -quarks (or  $D$ -mesons) [15,16]; *e.g.*, if  $m_c^*$  (or  $m_D^*$ ) is reduced in matter (with  $m_\psi$  constant),  $c$ - and  $\bar{c}$ -quarks are thermally favored to occur in open-charm states, thus reducing  $N_\psi^{eq}(T; \gamma_c)$ . Finally, the gain term depends on the  $c$ -quark momentum distributions; its particularly simple form in Eq. (5), based on thermalized  $c$ -quarks, illustrates the impact of  $c$ -quark rescattering (as discussed in the previous section) on charmonia. Therefore, thermalization of  $c$ -quarks opens the window on equilibrium properties of both open and hidden charm, *i.e.*, their masses encoded in  $N_\psi^{eq}(T; \gamma_c)$ , as well as charmonium widths ( $\Gamma_\psi$ ). A sensitive observable to distinguish direct and regenerated  $J/\psi$ 's turns out to be their elliptic flow,  $v_2^\psi$  [40,41,25,42]. If only suppression is operative,  $v_2^\psi$  reaches a maximal value of  $\sim 2\text{-}3\%$  [41], while it grows up to  $\sim 15\%$  at  $p_t^\psi \simeq 4\text{ GeV}$  for thermal  $c\bar{c}$  coalescence [25].

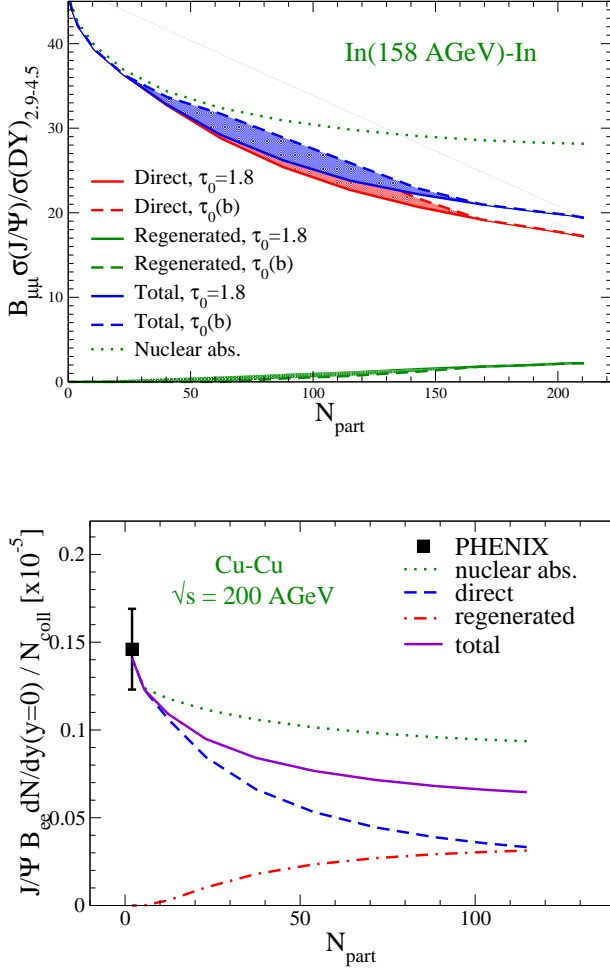


**Fig. 5.** Time evolution of the  $J/\psi$  abundance in central  $Au\text{-}Au(\sqrt{s_{NN}}=200\text{ GeV})$  based on a solution of the rate Eq. (5) in an expanding thermal fireball including in-medium effects on both open and hidden charm mesons [16]. Dashed line: suppression only (no gain term); dash-dotted line: temperature-dependent equilibrium number,  $N_{J/\psi}^{eq}(T; \gamma_c)$ ; solid line: total number  $N_{J/\psi}(t)$ .



**Fig. 6.** Theoretical predictions for the excitation function of  $J/\psi$  production in central  $Au\text{-}Au$  collisions. Suppression (dashed line) and regeneration (dash-dotted line) components combine into a rather flat energy dependence for the total yield (solid line) [33].

A calculation [16] of the time evolution of  $N_{J/\psi}$  in central  $Au\text{-}Au(\sqrt{s}=200\text{ AGeV})$  based on Eq. (5) including in-medium masses of open-charm and reduced  $J/\psi$  binding energies, as well as incomplete thermalization of  $c$ -quarks in the early stages, is displayed in Fig. 5. One finds that



**Fig. 7.** Theoretical predictions for the centrality dependence of  $J/\psi$  production in intermediate-size-ion collisions at SPS (upper panel) and RHIC (lower panel), including both suppression and regeneration processes [16]. The bands in the upper panel reflect uncertainties in the formation time which is expected to increase at lower collision centrality (dashed lines).

the  $J/\psi$  yield equilibrates close to the phase boundary, with the major contribution arising from regeneration in the QGP and little changes in the “mixed” and hadronic phase. Note that this result crucially hinges on the notion of the  $J/\psi$  surviving as a resonance in the QGP under RHIC conditions,  $T \leq 2T_c$ . The final yield is a factor of  $\sim 4$ -5 increased over a scenario with suppression only. The situation is quite different at SPS energies ( $\sqrt{s}=17.3$  AGeV): with an expected open-charm number  $N_{c\bar{c}} \simeq 0.2$  in central  $Pb-Pb$ , secondary charmonium formation is negligible and  $J/\psi$  suppression is the main mechanism at work. Obviously, this calls for mapping out the excitation function for  $\sqrt{s}=20$ -200 GeV (accessible at RHIC), as suggested in Ref. [33]. Based on Fig. 6 one expects a transition from a suppression-dominated regime (SPS or low RHIC energies) to a regeneration-dominated one at  $\sqrt{s} \gtrsim 100$  AGeV,

resulting in a rather flat energy dependence (possibly with a shallow minimum).

Complementary information on the interplay between primordial and secondary  $J/\psi$  production can be extracted by going to smaller nuclear collision systems. Pertinent predictions are shown in Fig. 7, reconfirming the absence of noticeable regeneration at SPS (as well as a smooth centrality dependence; upper panel), but an approximately equal amount of primordial and regenerated  $J/\psi$ 's for central  $Cu-Cu$  at RHIC (lower panel).

## 5 Conclusions

Hadrons containing heavy quarks are excellent probes of the environment formed in nuclear reactions. Evidence for coalescence mechanisms in elementary hadronic reactions finds its natural extension for both  $D$ -mesons and charmonia to heavy-ion collisions. In addition, at RHIC, the produced medium appears to interact strongly enough to thermalize  $c$ -quarks (but not  $b$ -quarks). If confirmed, “ $D$ ”-meson resonance formation in the QGP (coupled with pertinent coalescence at  $T_c$ ) might be the key to a simultaneous understanding of (suppressed)  $p_t$  spectra and (large) elliptic flow of  $D$ -mesons (and single electrons). The transition into a perturbative energy-loss picture could be shifted to higher  $p_t$  than for light hadrons. Resonance states in the QGP also have substantial impact on charmonium production, facilitating their regeneration in the  $1$ - $2T_c$  regime where inelastic collision rates are high. Here, thermalization of  $c$ -quarks would enable a rather direct window on spectral properties of open and hidden charm, *i.e.*, their masses and widths. Work in progress on  $\Upsilon$  production [43] seems to indicate, however, that even at LHC their suppression is prevalent, due to a lack of thermalization of bottom quarks. Thus, a simultaneous observation of  $\Upsilon$  suppression and the absence thereof for  $J/\psi$  at collider energies would provide strong evidence for secondary charmonium production.

Among the main challenges yet to be met is establishing connections of heavy-quark observables to (“pseudo”-) order parameters of the QCD phase transition [44]. With low-lying charmonia possibly surviving up to  $2T_c$ , their dissolution evades a direct relation to  $T_c$ . A suitable quantity could be their inelastic width, which in model calculations is typically quite different (smaller) in the hadronic compared to the QGP phase [15]. Quenched lattice calculations [20] indicate a similar trend, but unquenching has to be awaited for more definite conclusions. We also mention the recent work of Ref. [45], where an increase in transverse-momentum fluctuations of open-charm states has been linked to a first-order transition.

Looking into the future, it seems that the combined experimental and theoretical analysis of heavy-quark observables in ultrarelativistic heavy-ion collisions is on a promising path toward providing a milestone in the identification of the QGP.

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